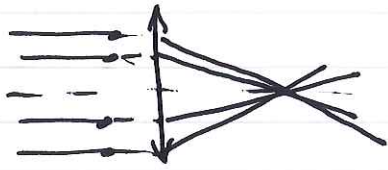


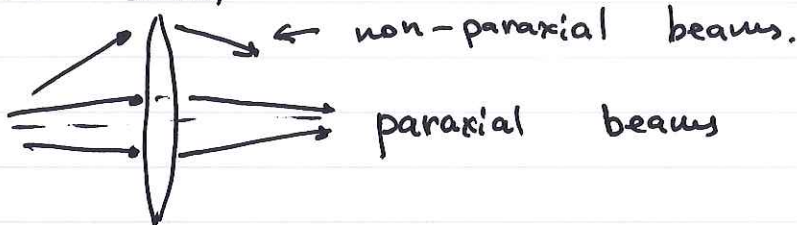
# Ideal lens vs Real lens



Ideal lens changes the beam direction without any displacements independently on where the beam hits the lens.

Thin lens - thickness is negligible

Paraxial approximation: the beams travel close to the optical axis, the angles involved are small



$$n_1 \sin \theta_1 = n_2 \sin \theta_2 \quad \text{Snell's law}$$

Paraxial approximation  $\sin \theta \approx \theta \quad (\text{rad})$

In reality  $\sin \theta \approx \theta - \frac{\theta^3}{6} + \frac{\theta^5}{5!} - \dots$

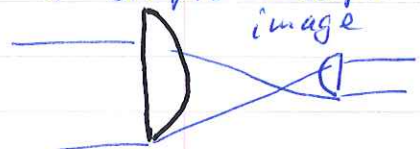
Larger angle - more ~~imperfect~~ deviation from an ideal thin lens.

From observations: what is wrong with a simple telescope

Flat surface looks spherical

Color distortions

Only the center is in focus.



# Distortions — lens aberrations

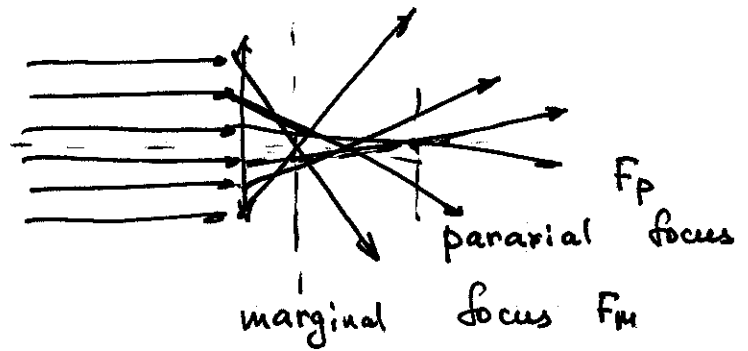
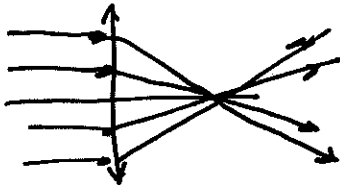
monochromatic  
(for each color)

chromatic  
(different behavior for  
different colors)

clarity of an image

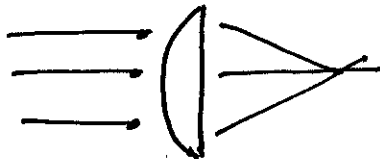
distortions → spherical curvature  
barrel/pincushion distortions

## 1. Spherical aberration

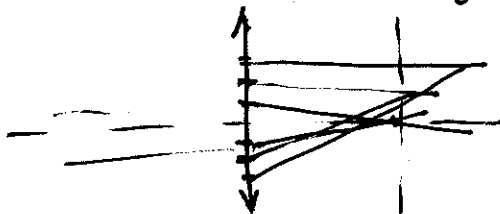


The larger is the distance b/w  $F_p$  and  $F_m$ , the larger is spherical aberration.

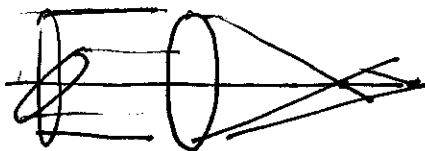
Life tip: for a plano-convex lens put a curved surface toward flat wavefront



## 2. Coma - different sections of a lens focus at different heights



## 3. Astigmatism



Dispersion: refractive index of a material depends on light & wavelength (frequency)

Refraction law: air-glass  $n_1 \sin \theta_1 = n_2(\lambda) \sin \theta_2(\lambda)$

Different wavelengths are focussed differently, distorting the colors

How to avoid these problems?

1. Restrict the size of the lens  
(better paraxial approximation, but dimmer images) — helps with some monochromatic aberrations
2. Use multiple lens compounds instead of a single lens (the parameters of the lenses can be optimized to minimize aberrations)
3. Use achromatic doublets — a pair of positive and negative lenses made out of different type of glass with different dispersion to correct chromatic aberrations
4. Use aspherical lens — specially designed lens shape to minimize aberrations.