

Thermodynamics → effects of temperature relations b/w internal (thermal) energy, work and heat

Liquids & solids → complex interacting systems, treated phenomenologically

Thermal expansion: $\frac{\Delta L}{L} = \alpha \Delta T ; \frac{\Delta V}{V} = \beta \Delta T$

\uparrow linear / volume coefficient of ~~heat~~ thermal expansion

Heating: $Q = m c \Delta T$ c - specific heat capacity

Phase transition: $Q = m \cdot L$

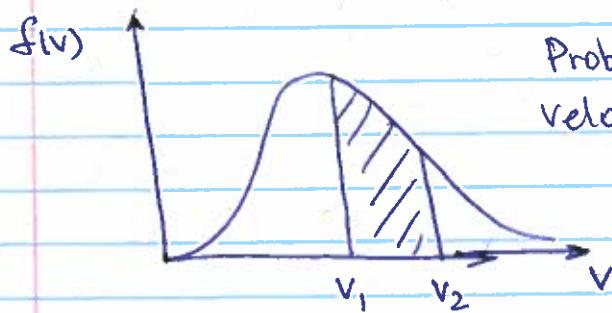
Entropy change
phase transition
 $\Delta S = mL/T$

$$\begin{aligned} dS &= \frac{dQ}{T} \\ &\text{heating / cooling} \\ S &= \int_{T_1}^{T_2} \frac{mLdT}{T} = mL \ln\left(\frac{T_2}{T_1}\right) \end{aligned}$$

Gases: ~~heat~~ simple non-interacting particles

Velocity distribution: (Maxwell-Boltzmann distribution)

Probability density $f(v) = 4\pi \left(\frac{m}{2\pi k_B T}\right)^{1/2} v^2 e^{-mv^2/2k_B T}$



Probability to find particle with velocity v $v_1 < v < v_2$

$$P = \int_{v_1}^{v_2} f(v) dv$$

Average velocity $\langle v \rangle = \int_0^\infty v f(v) dv = \sqrt{\frac{8k_B T}{\pi m}}$

Root-mean-square $v_{rms} = \sqrt{\langle v^2 \rangle} = \sqrt{\frac{3k_B T}{m}}$

Internal energy of an ideal gas

$$E_{\text{int}} = N \cdot \langle K \rangle_{\text{kinetic energy}}$$

$$\langle K \rangle = \left\langle \frac{\# \text{ of degrees of freedom}}{\# \text{ of degrees of freedom}} \right\rangle \cdot \frac{k_B T}{2}$$

Monatomic gas: 3 d.o.f

$$\langle K \rangle_{\text{mono}} = \frac{3}{2} k_B T \quad E_{\text{int}} = \frac{3}{2} N k_B T$$

Diatomic gas: 5 (or 7) d.o.f

$$\langle K \rangle_{\text{dia}} = \frac{5}{2} k_B T \quad (\text{air})$$

$$\text{or } \frac{7}{2} k_B T$$

Ideal gas law

$$PV = nRT = N \cdot k_B T$$

$$n = \frac{N}{N_A}$$

$$N_A = 6 \cdot 10^{23}$$

Avgadro number

$$k_B \cdot N_A = R \quad \text{universal gas constant}$$

The first law of thermodynamics

$$Q = \Delta E_{\text{int}} + W$$

$$\Delta E_{\text{int}} = \frac{[\# \text{ dof}]}{2} N k_B T = \frac{[\# \text{ dof}]}{2} n R_{\text{eff}} T$$

depends only on temperature change

$$\text{Work } W = \int_{V_1}^{V_2} \frac{P}{T} dP \quad \text{depends on the process.}$$

$$\text{Entropy change } dS = \frac{dQ}{T}$$

$$\text{Isothermal } Q = W = nRT \ln \frac{V_2}{V_1} \quad \Delta S = \frac{Q}{T} = nR \ln \frac{V_2}{V_1}$$

$$\text{Isobaric } Q = nC_V T$$

$$\Delta S = nC_V \int_{T_1}^{T_2} \frac{dT}{T} = nC_V \ln \frac{T_2}{T_1}$$

$$\text{Isobaric } Q = nC_P T$$

$$\Delta S = nC_P \ln \frac{T_2}{T_1}$$

$$\text{Adiabatic } \Delta S = 0$$

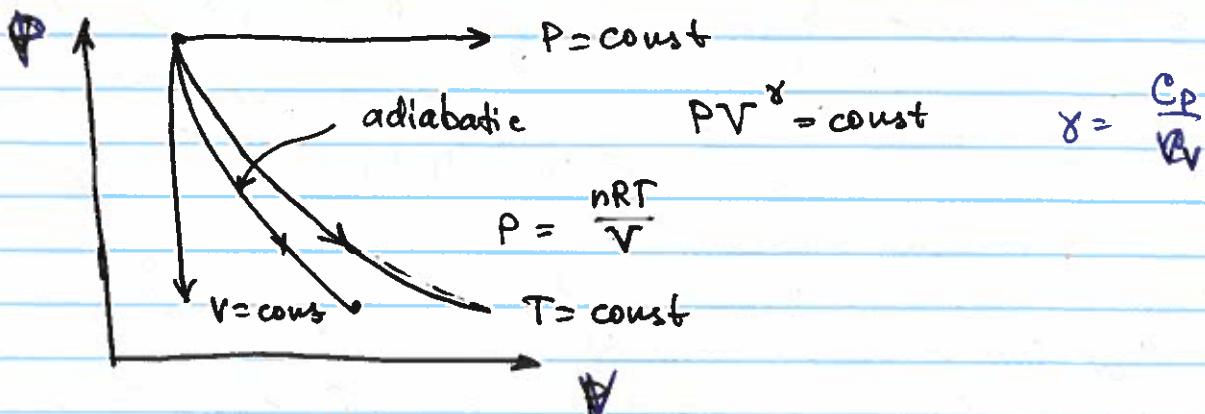
Let's gather together relevant information about different cycles

	ΔE_{int}	$\int PdV = nRT \ln \frac{V_2}{V_1}$	Q
Isothermal $T = \text{const}$	0	$nRT \ln \frac{V_2}{V_1}$	$nRT \ln \frac{V_2}{V_1}$
Isobaric $P = \text{const}$	$nC_V \cdot \Delta T$ [$\frac{3}{2}nR\Delta T$]	$P \Delta V$ $= nR \Delta T$	$\Delta E_{int} + W = nC_p \Delta T$ $nC_V \Delta T + nR \Delta T = n(C_V + R) \Delta T$
Isochoric $V = \text{const}$	$nC_V \cdot \Delta T$ [$\frac{3}{2}nR\Delta T$]	0	$nC_V \Delta T$
Adiabatic $Q = \text{const} = 0$ $PV^\gamma = \text{const}$	$nC_V \cdot \Delta T$ [$\frac{3}{2}nR\Delta T$] ↑ for monoatomic gas	$\int PdV = \frac{P_1V_1 - P_2V_2}{\gamma - 1}$	0

Adiabatic process : $W = \int PdV = P_1V_1 \int_{V_1}^{V_2} \frac{dV}{V^\gamma} =$

$$= P_1V_1^\gamma \left(-\frac{1}{\gamma-1} \right) \frac{1}{V^{\gamma-1}} \Big|_{V_1}^{V_2} = P_1V_1^{\frac{\gamma}{\gamma-1}} \left[\frac{1}{V_1^{\gamma-1}} - \frac{1}{V_2^{\gamma-1}} \right] =$$

$$= \frac{1}{\gamma-1} \left[\frac{P_1V_1^\gamma}{V_1^{\gamma-1}} - \frac{P_1V_1^\gamma}{V_2^{\gamma-1}} \right] = \frac{1}{\gamma-1} [P_1V_1 - P_2V_2]$$



Thermodynamical cycles : for each step calculate $W, \Delta E_{int}, Q = W + \Delta E_{int}$

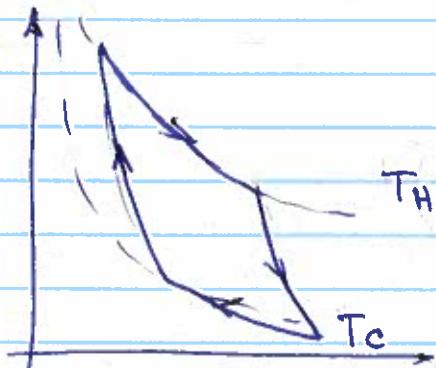
$$W_{\text{total}} = \sum W_{\text{each step}}$$

$Q > 0$ added heat $Q < 0$ extracted heat

$$\text{efficiency} = \frac{\text{useful outcome}}{\text{cost}}$$

Heat engine outcome	Heat pump	\Rightarrow Refrigerator
outcome W	Q_H	Q_C
cost Q_H	W	W
$e = \frac{W}{Q_H} = \frac{Q_H - Q_C}{Q_H}$	$COP = \frac{Q_H}{W} = \frac{ Q_H }{ Q_H - Q_{ct}}$	$COP = \frac{Q_C}{W} = \frac{Q_C}{ Q_H - Q_C}$

Ideal heat engine \rightarrow Carnot cycle (fully reversible)
 (two isothermal + two ideal adiabatic processes)



$$e_{\text{Carnot}} = 1 - \frac{T_C}{T_H}$$

max achievable efficiency
 for a heat engine