

## Electromagnetic induction

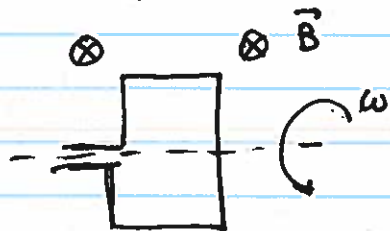
An emf is induced in a loop of wire by changing the magnetic flux through the loop

Magnitude from Faraday law:  $\mathcal{E} = - \frac{d\Phi_B}{dt}$

Direction from Lenz law:  
the induced current is in the direction that produces magnetic field opposing the change of magnetic flux

This is a source of ~~our~~ most of our power plants!

AC generator: wire loop rotating in a permanent magnet



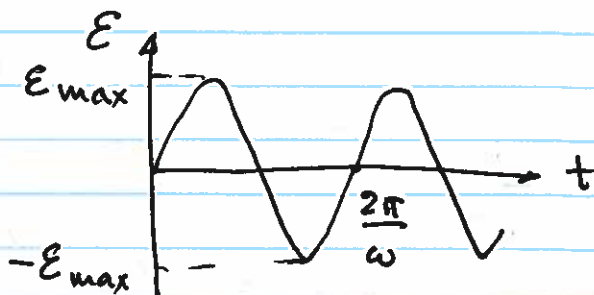
side view

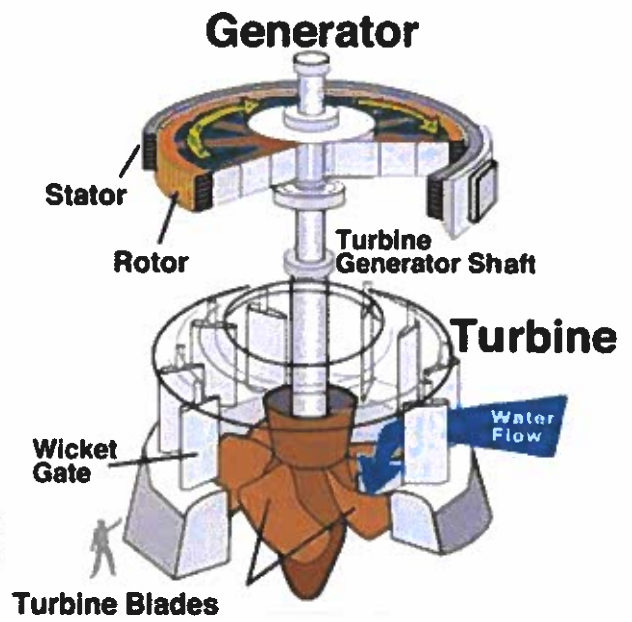
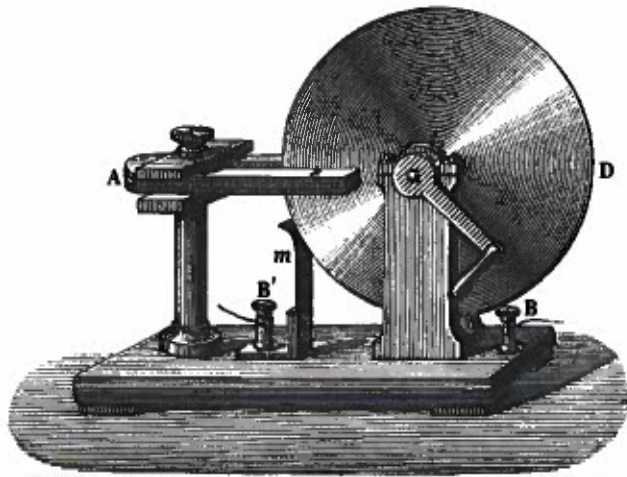
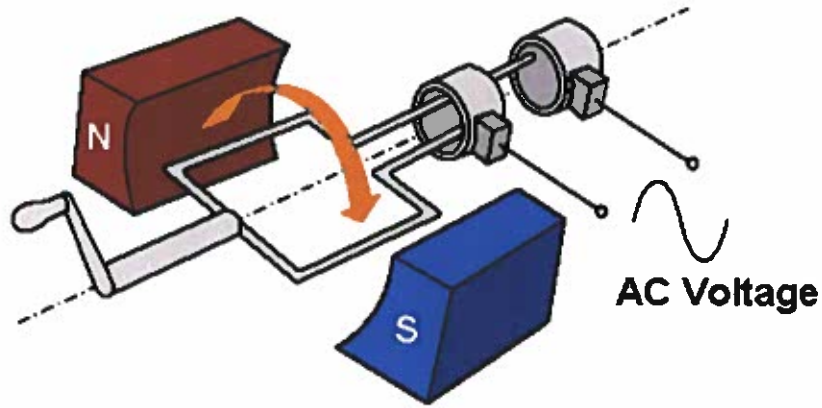


if  $\omega$  is the rotation rate  
 $\theta = \omega \cdot t$

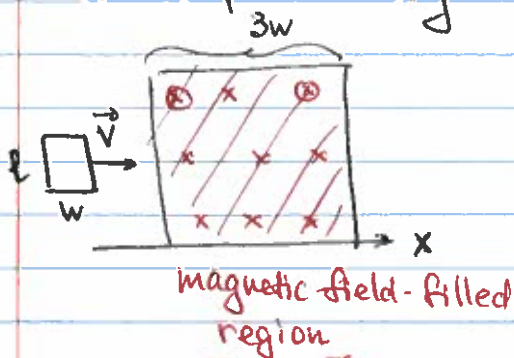
$$\Phi_B = B \cdot A \cdot \cos \theta = B \cdot A \cos \omega t$$

$$\mathcal{E} = - \frac{d\Phi_B}{dt} = \underbrace{BA\omega}_{\text{max instantaneous EMF}} \sin \omega t$$

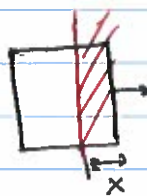
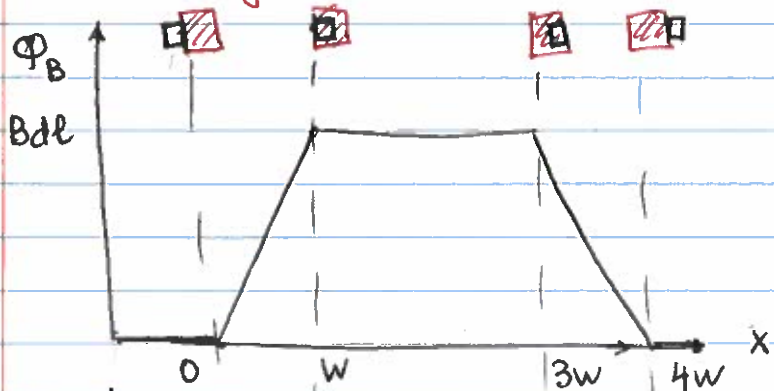




A loop moving through a magnetic field

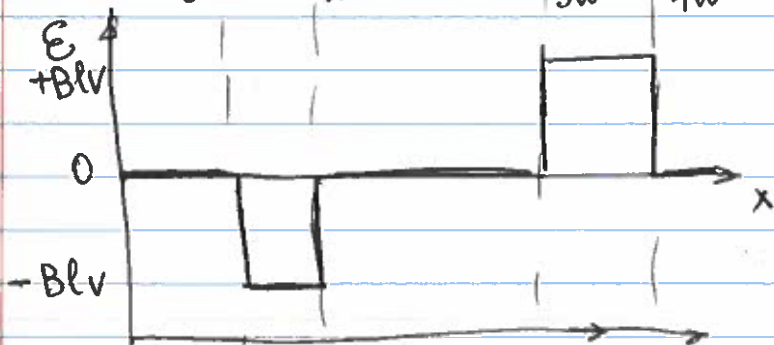


A rectangular loop moving with constant speed  $\vec{v}$  through a region of constant magnetic field  $B$ .



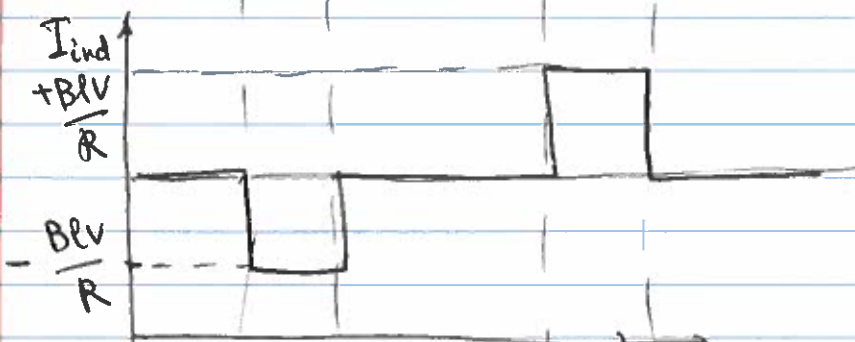
$$\Phi = Bl \cdot x$$

for  $x < w$   
 $x = v \cdot t$



$$\mathcal{E}_{\text{ind}} = - \frac{d\Phi}{dt} =$$

$$= - Bl \frac{dx}{dt} = \pm Blv$$



If  $R$  is the internal resistance of the loop

$$I = \frac{\mathcal{E}}{R} = \pm \frac{Blv}{R}$$

Energy lost to heat:  $P = I^2 R$   
 electric power



We must apply force to maintain constant speed

$$-l \cdot B \cdot I =$$

$$= - \frac{l^2 B^2 v}{R}$$

