

# ***Transversity in Two-Pion Semi-Inclusive Deep-Inelastic Scattering***

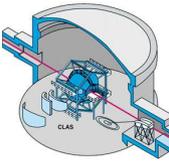
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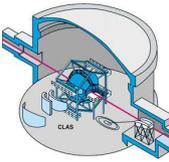
# Introduction



- Transversity:  $h_1(x)$  is the distribution of transversely polarized quarks inside a transversely polarized nucleon
- Tensor charge:  $\delta q = \int h_1(x) dx$
- Completely new information on nucleon structure
- Lattice and model calculations show that  $\delta q$  is not small
- Interference fragmentation functions offer one of the most promising ways to measure  $h_1(x)$
- JLab can do this



# The $h_1$ Structure Function



$$f_1 = \text{circle with a dot} \quad g_1 = \text{circle with a dot and a red arrow pointing right} - \text{circle with a dot and a red arrow pointing left} \quad h_1 = \text{circle with a dot and a red arrow pointing up} - \text{circle with a dot and a red arrow pointing down}$$

## Characteristics of $h_1$ :

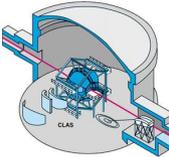
- leading twist -> on equal footing with  $f_1$  and  $g_1$
- chiral-odd -> can NOT be probed in inclusive DIS

Solution: couple  $h_1$  to chiral-odd fragmentation function

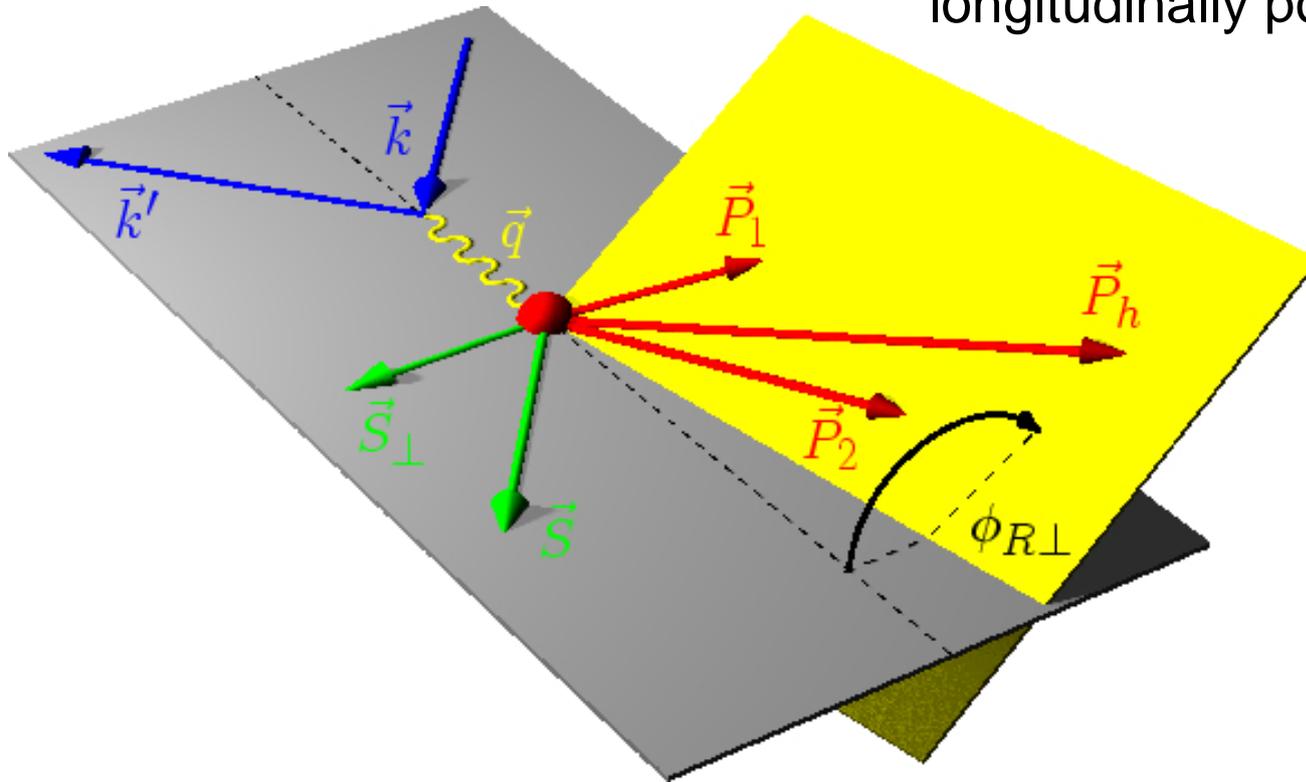
Two options: 1 or 2 particle semi-inclusive DIS



# Single Spin Asymmetry



longitudinally polarized deuterium target

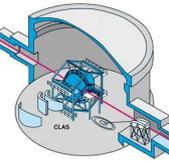


$$\vec{P}_h \equiv \vec{P}_1 + \vec{P}_2$$

$$A_{UL}(\phi_{R\perp}) = \frac{1}{|P_T|} \frac{N^{\rightarrow}(\phi_{R\perp})/L^{\rightarrow} - N^{\leftarrow}(\phi_{R\perp})/L^{\leftarrow}}{N^{\rightarrow}(\phi_{R\perp})/L^{\rightarrow} + N^{\leftarrow}(\phi_{R\perp})/L^{\leftarrow}}$$



# Asymmetries -Theory



A. Bacchetta, M. Radici, PRD 69, 0740XX (2004)

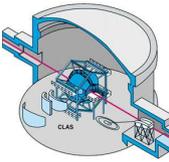
$$A'_{UT} \sim B(y) \sin(\phi_{R\perp} + \phi_S) h_1 H_1^{\triangleleft} + V(y) \sin(\phi_S) \frac{M}{Q} (\dots)$$

$$A'_{UL} \sim V(y) \sin(\phi_{R\perp}) \frac{M}{Q} (h_L H_1^{\triangleleft} + g_1 \tilde{G}^{\triangleleft})$$

$T/L \implies$  target spin defined w.r.t. virtual photon

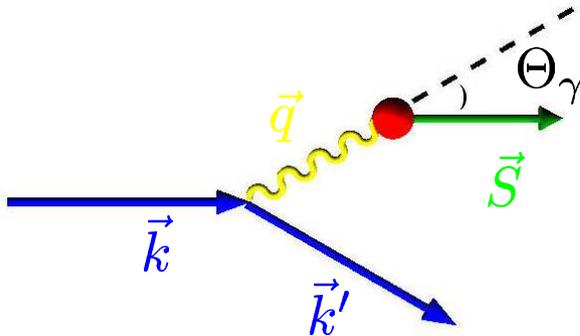


# Asymmetries - Experiment



$$A_{UL} \simeq A'_{UL} - \sin \Theta_\gamma A'_{UT}$$

target spin defined w.r.t. beam



target spin w.r.t. virtual photon

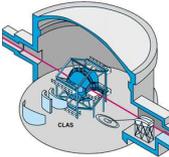
$$\langle \sin \Theta_\gamma \rangle = \left\langle \frac{2Mx}{Q} \sqrt{1-y} \right\rangle \simeq 0.045$$

if  $H_1^\Delta \neq 0$ :

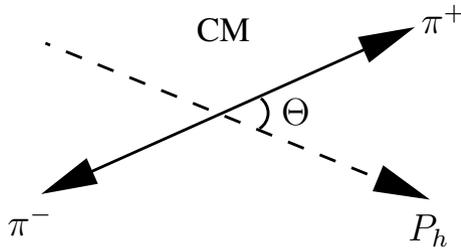
$\implies$  2 hadron fragmentation can probe transversity!



# Interference FF

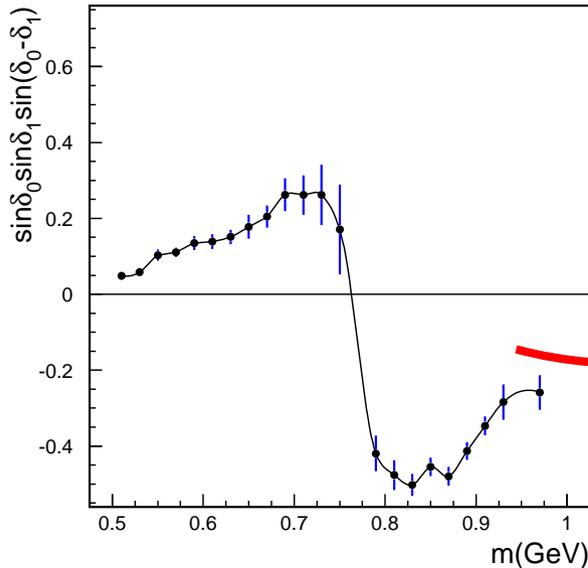


$$H_1^\triangleleft(z, \cos \Theta, M_{\pi\pi}^2) = H_1^{\triangleleft,sp}(z, M_{\pi\pi}^2) + \cos \Theta H_1^{\triangleleft,pp}(z, M_{\pi\pi}^2)$$



$\langle \cos \Theta \rangle \approx 0 \implies H_1^{\triangleleft,pp}$  drops out!

Jaffe et al. [hep-ph/9709322]:



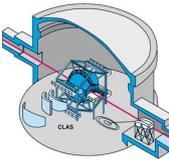
$$H_1^{\triangleleft,sp}(z, M_{\pi\pi}^2) = \frac{\sin \delta_0 \sin \delta_1 \sin(\delta_0 - \delta_1) H_1^{\triangleleft,sp'}(z)}{\delta_0 (\delta_1) \rightarrow \text{S(P)-wave phase shifts}}$$

$$= \mathcal{P}(M_{\pi\pi}^2) H_1^{\triangleleft,sp'}(z)$$

$\implies A_{UL}$  might depend strongly on  $M_{\pi\pi}$



# Analysis method

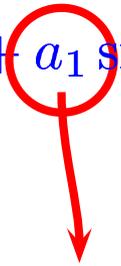


Fitting method:

$$A_{UL}(\phi) \sim \frac{N^{\rightarrow} - N^{\leftarrow}}{N^{\rightarrow} + N^{\leftarrow}}$$

fit with  
←

$$f(\phi_{R\perp}) = a_0 + a_1 \sin \phi + b_1 \cos \phi + \dots$$


$$A_{UL}^{\sin \phi}$$

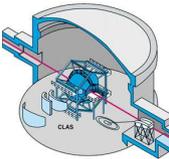
Weighting method:

$$A_{UL}^{\sin \phi} \sim \frac{\sum_{i=1}^{N^{\rightarrow}} \sin \phi_i - \sum_{i=1}^{N^{\leftarrow}} \sin \phi_i}{\frac{1}{2}(N^{\rightarrow} + N^{\leftarrow})}$$

← weighting is sensitive to detector acceptance



# comparison to model prediction



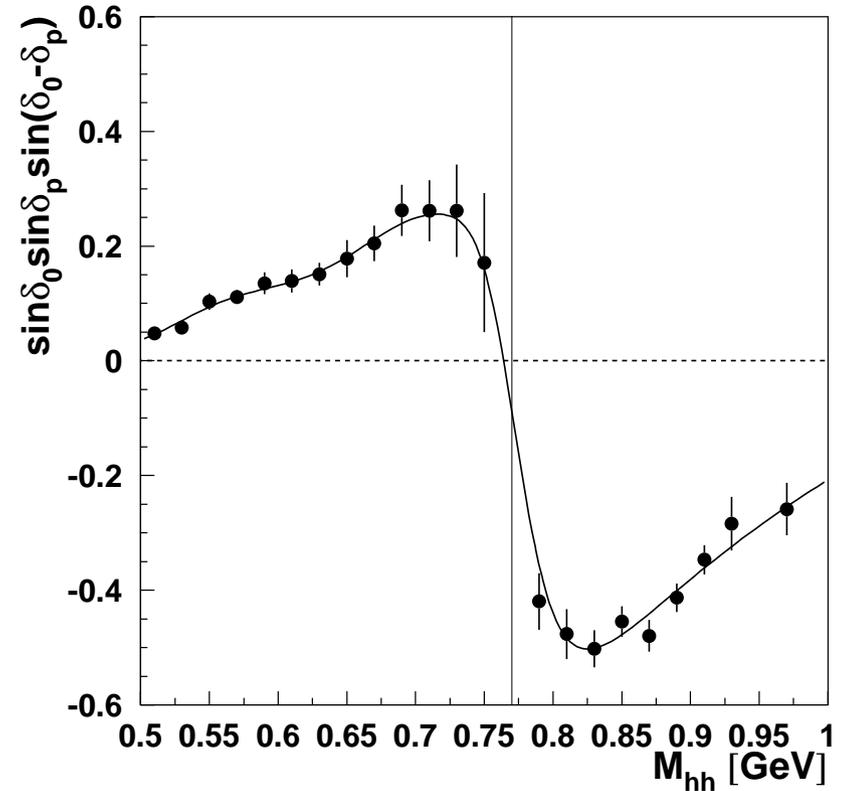
Model by Jaffe et al.:

- predicts mass dependence
- NO statements on size/sign of the asymmetry

Fit data with:

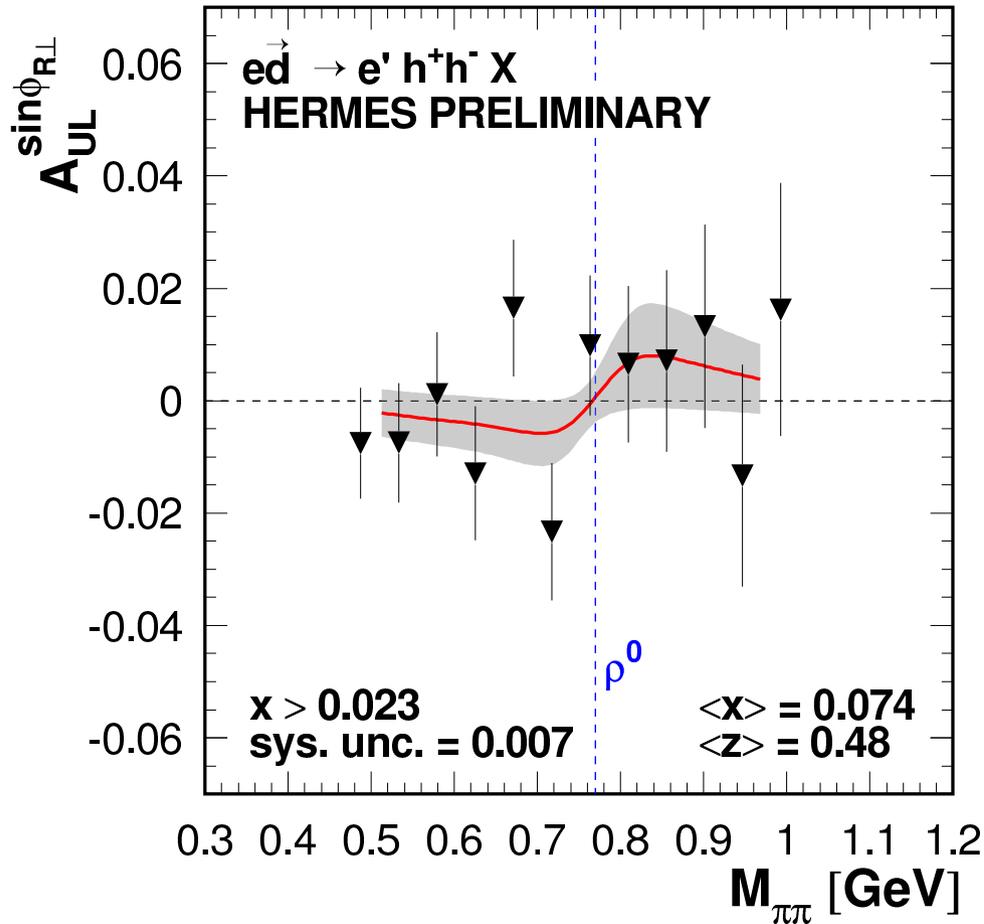
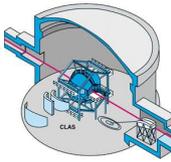
$$g(M_{\pi\pi}^2) \simeq c_1 \mathcal{P}(M_{\pi\pi}^2) + c_2$$

by extracting  $c_1$  &  $c_2$  a qualitative comparison can be made to the model prediction





# comparison to model prediction



$$c_1 = 0.040 \pm 0.036$$

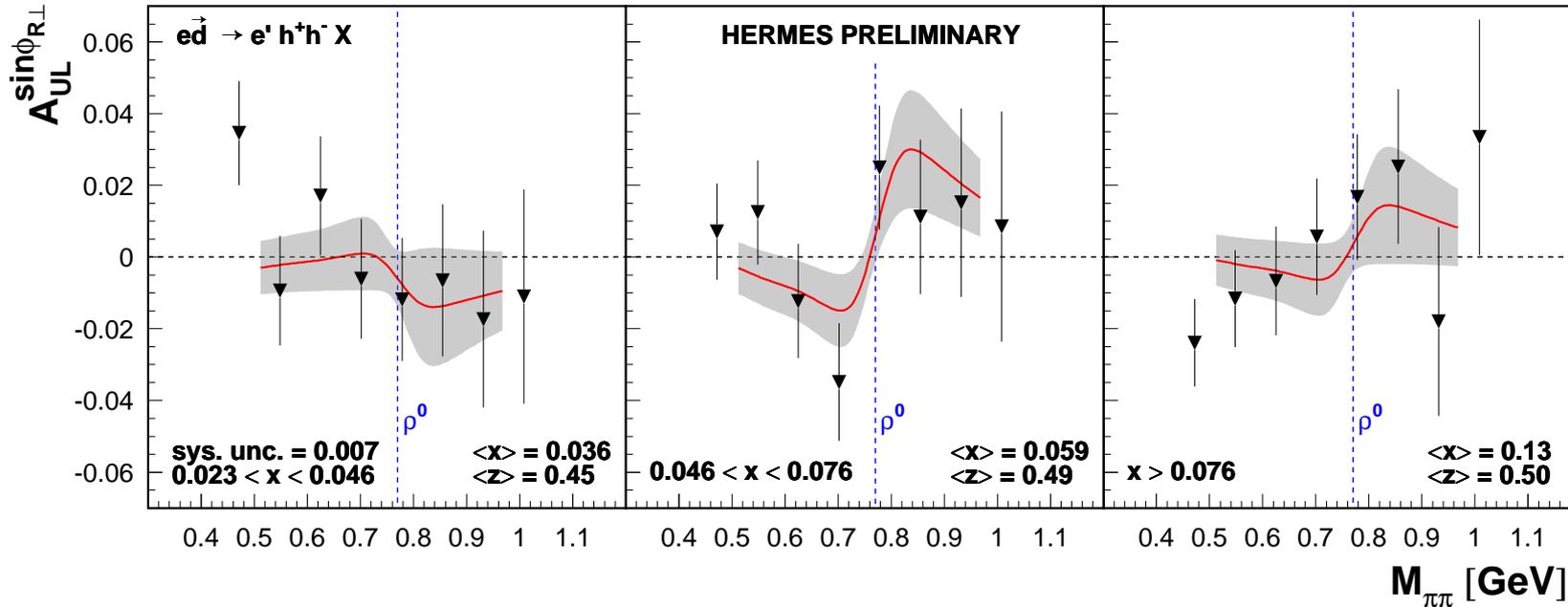
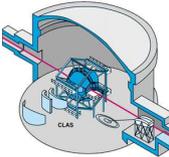
$$c_2 = -0.001 \pm 0.004$$

- hint of a sign change at the  $\rho^0$  mass

$$g(M_{\pi\pi}^2) \simeq c_1 \mathcal{P}(M_{\pi\pi}^2) + c_2$$

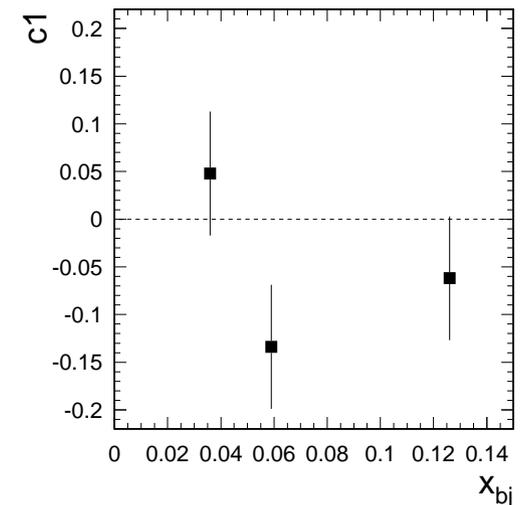


# $x$ -dependence



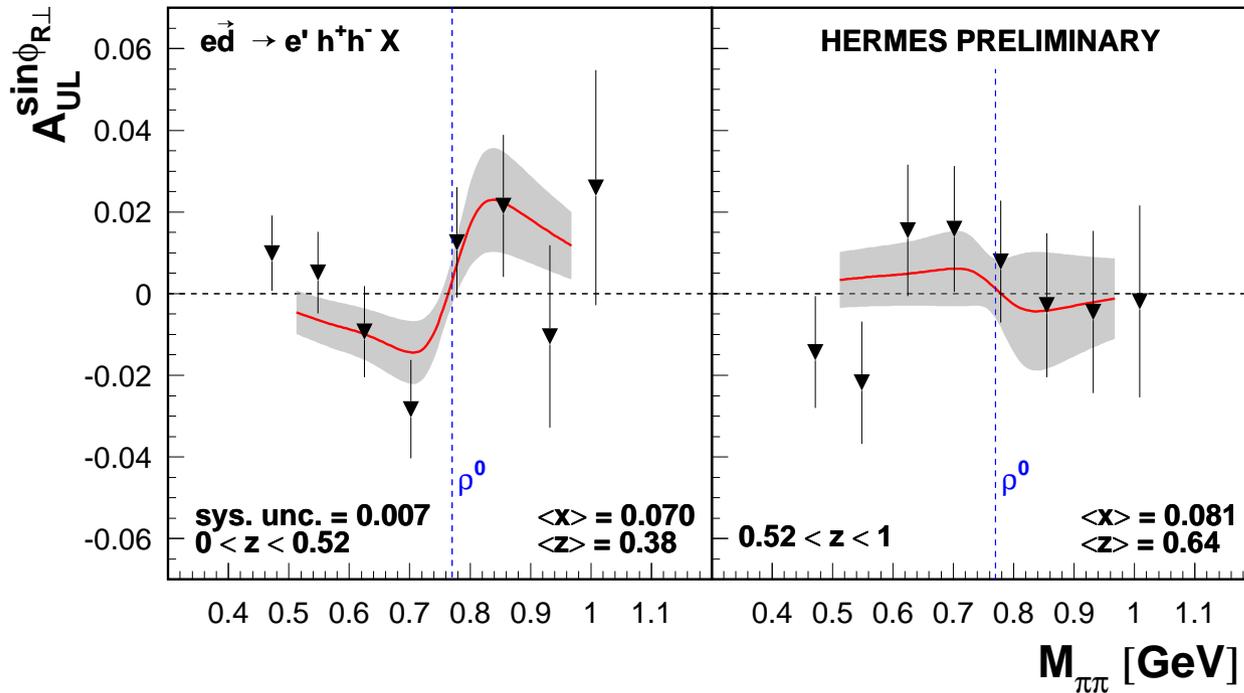
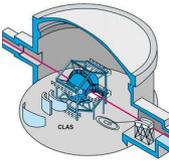
● higher  $x$ : hint of sign change at  $\rho^0$  according to Jaffe's model

●  $c_1(x) \propto h_1(x)$  ?



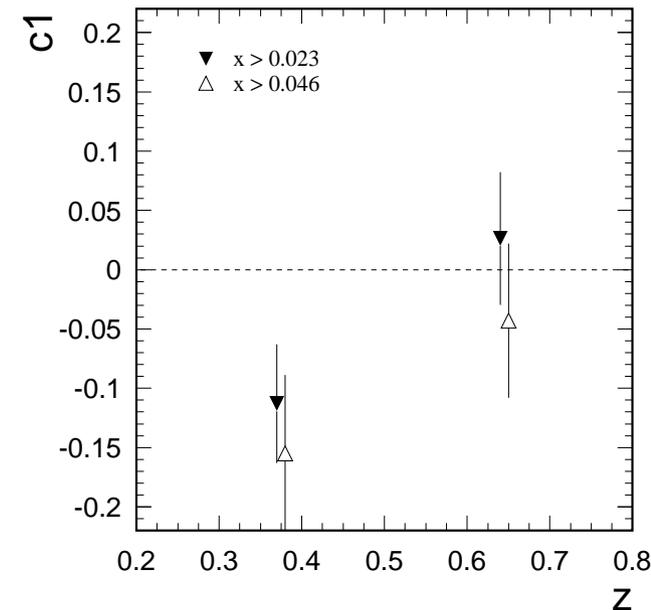


# $z$ -dependence



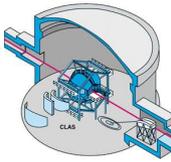
- sign change at  $\rho^0$  according to Jaffe's model for low  $z$

- $c_1(z) \propto H_1^{\triangleleft, sp}(z, M_{\pi\pi})$  ?





# Conclusions



- Initial HERMES measurements with a longitudinal target polarization show very interesting results.
- A similar analysis is underway with CLAS EG2000 data
- Since no single experiment is self-sufficient, JLab at 12 GeV can play a big role in determining  $h_1$  through 2-hadron fragmentation functions, provided there is a multi-particle detector in its future.