

All atomic generation and manipulation of squeezed light with Rb atoms

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PQE

Heisenberg uncertainty principle and its optics equivalent



Heisenberg uncertainty principle

$$\Delta p \Delta x \geq \hbar/2$$

The more precisely the POSITION is determined, the less precisely the MOMENTUM is known, and vice versa

Heisenberg uncertainty principle and its optics equivalent



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$$\Delta \phi \Delta N \geq 1$$

The more precisely the PHASE is determined, the less precisely the AMPLITUDE is known, and vice versa

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Optics equivalent strict definition

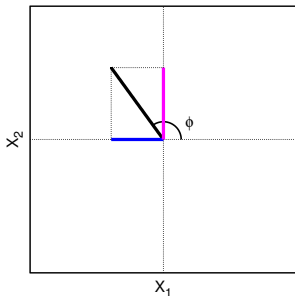
$$\Delta X_1 \Delta X_2 \geq 1/4$$

Transition from classical to quantum field

Classical analog

- Field amplitude a
- Field real part
 $X_1 = (a^* + a)/2$
- Field imaginary part
 $X_2 = i(a^* - a)/2$

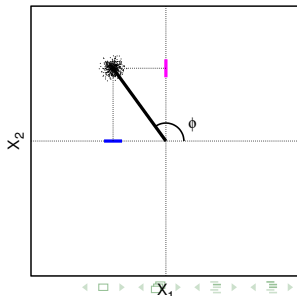
$$E(\phi) = |a|e^{-i\phi} = X_1 + iX_2$$



Quantum approach

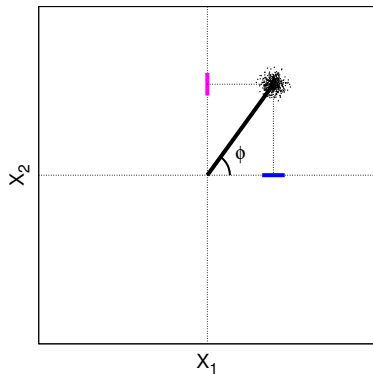
- Field operator \hat{a}
- Amplitude quadrature
 $\hat{X}_1 = (\hat{a}^\dagger + \hat{a})/2$
- Phase quadrature
 $\hat{X}_2 = i(\hat{a}^\dagger - \hat{a})/2$

$$\hat{E}(\phi) = \hat{X}_1 + i\hat{X}_2$$

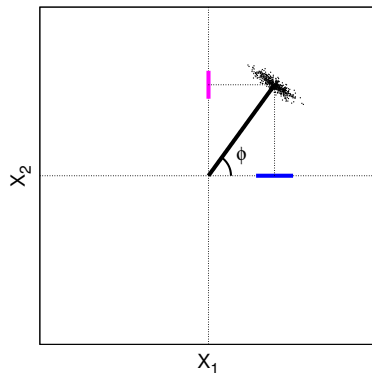


Minimum uncertainty (coherent) states

Coherent state



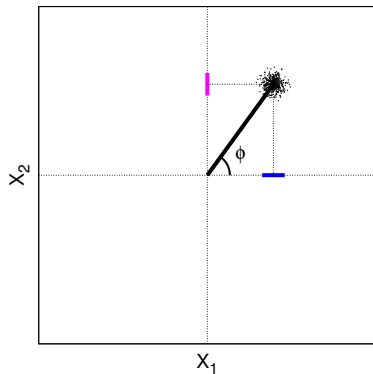
Squeezed state



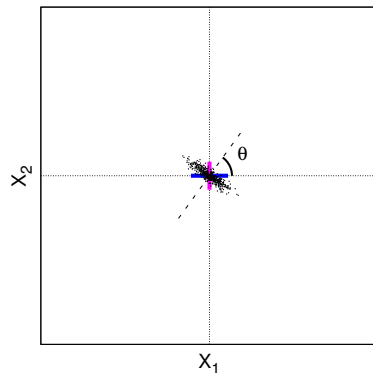
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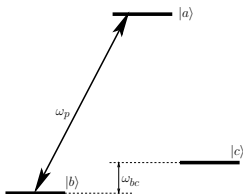
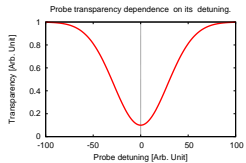


Squeezed state

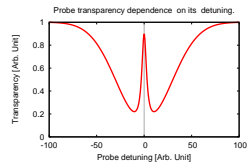
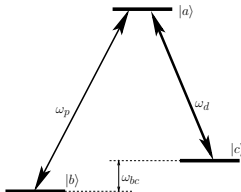
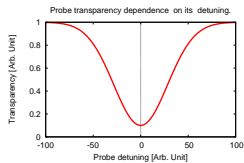


$$\Delta X_1 \Delta X_2 \geq 1/4$$

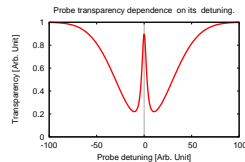
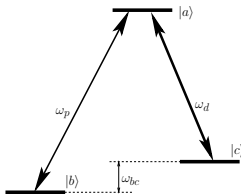
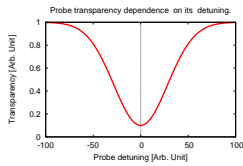
Quantum memory with atomic ensembles



Quantum memory with atomic ensembles



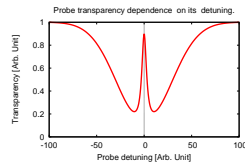
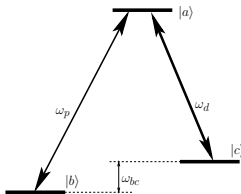
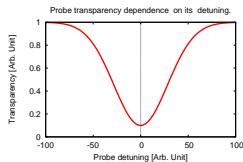
Quantum memory with atomic ensembles



Storage and retrieval

- single photon
- squeezed state (Furusawa and Lvovsky PRL **100** 2008)

Quantum memory with atomic ensembles



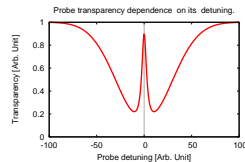
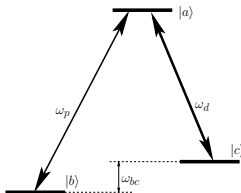
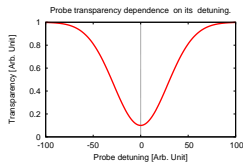
Storage and retrieval

- single photon
- squeezed state (Furusawa and Lvovsky PRL **100** 2008)

Squeezed state requirements for a quantum memory probe

- squeezing carrier at atomic wavelength (780nm, 795nm)
- squeezing within narrow resonance window at frequencies ($< 100\text{kHz}$)

Quantum memory with atomic ensembles



Storage and retrieval

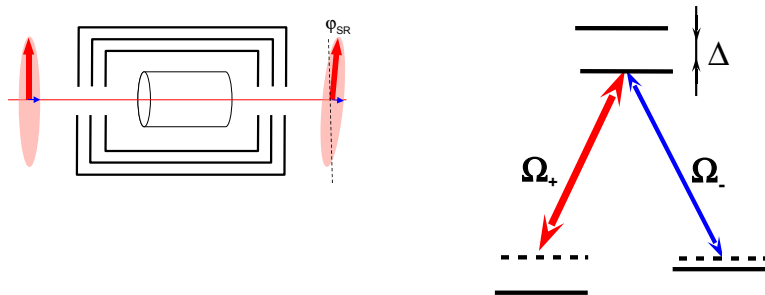
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Squeezed state requirements for a quantum memory probe

- squeezing carrier at atomic wavelength (780nm, 795nm)
- squeezing within narrow resonance window at frequencies ($< 100\text{kHz}$)

Traditional nonlinear crystal based squeezers are capable of it, but they are **extremely technically challenging** especially at short wave length.

Self-rotation of elliptical polarization in atomic medium



A.B. Matsko et al., PRA 66, 043815 (2002): theoretically prediction of 4-6 dB noise suppression

$$a_{out} = a_{in} + \frac{igL}{2}(a_{in}^{\dagger} - a_{in}) \quad (1)$$

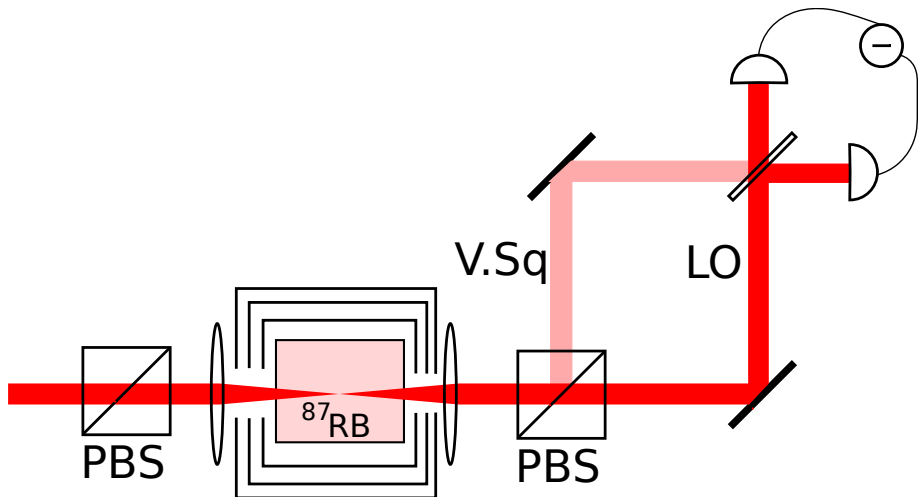
Will something so simple work?

- **Yes!** J. Ries, B. Brezger, and A. I. Lvovsky, Experimental vacuum squeezing in rubidium vapor via self-rotation, PRA **68**, 025801 (2003).
 - Observed 0.85dB of squeezing at bandwidth 5-10MHz
- **No!** M. T. L. Hsu et al., Effect of atomic noise on optical squeezing via polarization self-rotation in a thermal vapor cell, PRA **73**, 023806 (2006).
 - Observed 6dB of excess noise after the cell

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- **Possible.** Arturo Lezama et al., PRA **77**, 013806 (2008).
- **Definitely** Eugeny E. Mikhailov et al. Optics Letters, Issue 11, **33**, 1213-1215, (2008).
- **Definitely** Eugeny E. Mikhailov et al. JMO , Issues 18&19, **56**, 1985-1992, (2009).
- **Definitely** Philippe Grangier et al. Optics Express, **18**, Issue 5, pp. 4198-4205 (2010)
- **Definitely** Arturo Lezama et al., PRA **84**, 033851 (2011).
 - 3 dB of squeezing

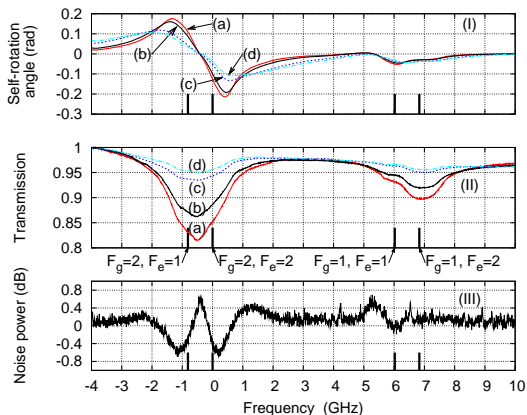
Setup



Squeezing vs laser detuning in ^{87}Rb at 795 nm

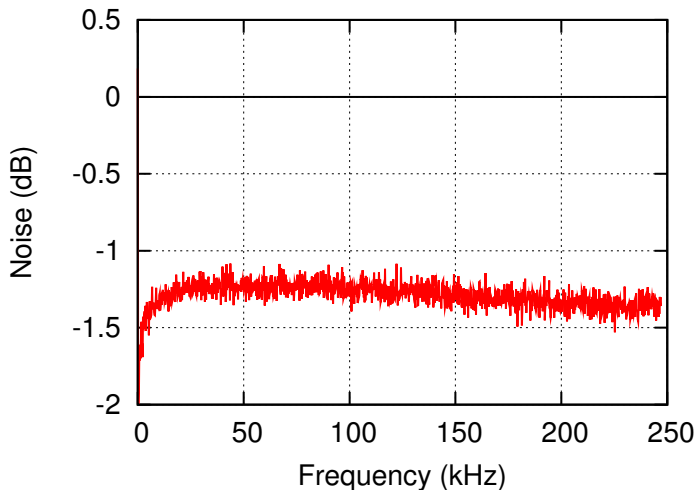
^{87}Rb cell + 2.5Torr Ne

(a) $P=1.0$ mW, (b) $P=1.5$ mW, (c) $P=4.2$ mW, (d) $P=6.6$ mW



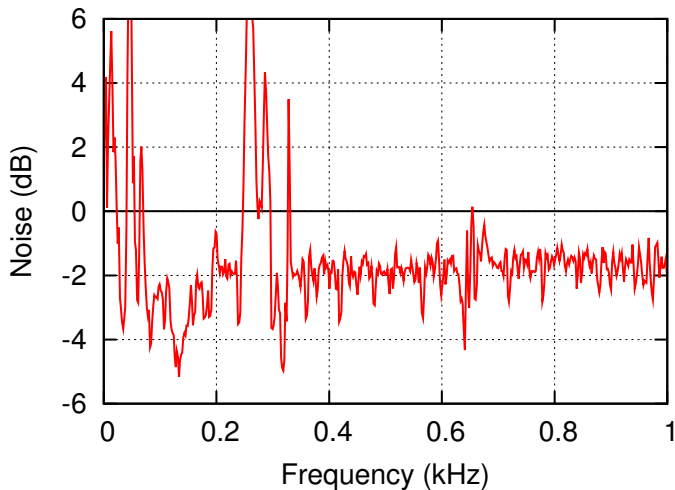
Low frequency squeezing spectrum in ^{87}Rb at 795 nm

$F_2 = 2 \rightarrow F_2 = 2$ transition ^{87}Rb cell + 2.5Torr Ne, $T=63^\circ\text{C}$ $P=5$ mW



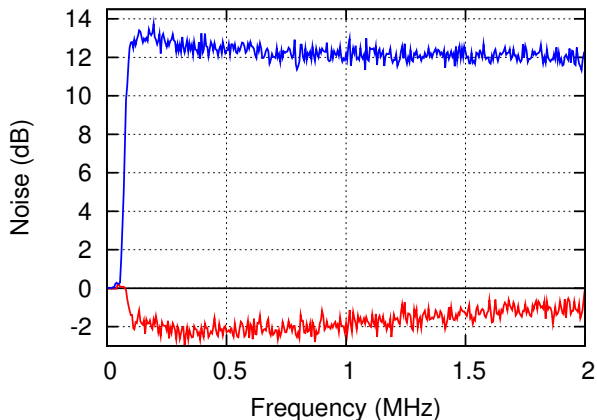
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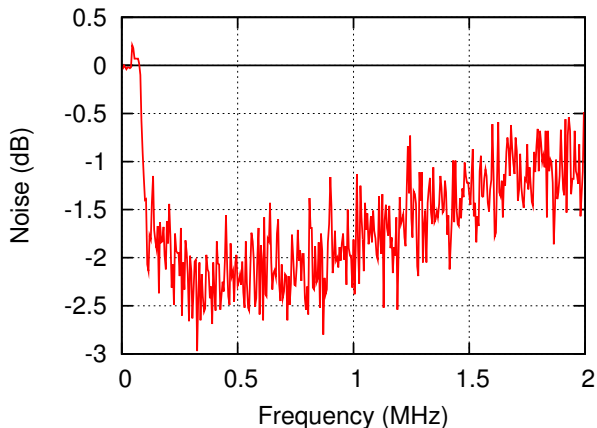
Maximally squeezed spectrum with ^{87}Rb

W&M team. ^{87}Rb $F_g = 2 \rightarrow F_e = 2$, laser power 7 mW, $T=65^\circ\text{C}$



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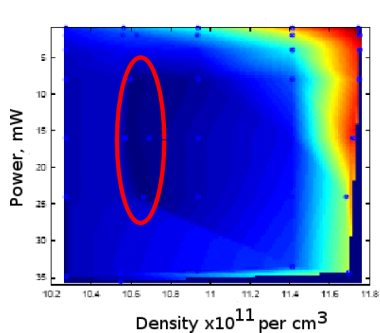
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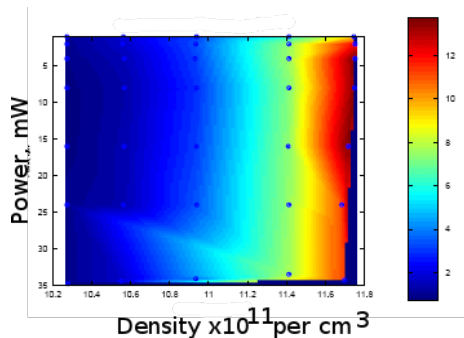
Lezama et.al report 3 dB squeezing in similar setup
Phys. Rev. A 84, 033851 (2011)

Squeezing region

Squeezing



Anti-squeezing

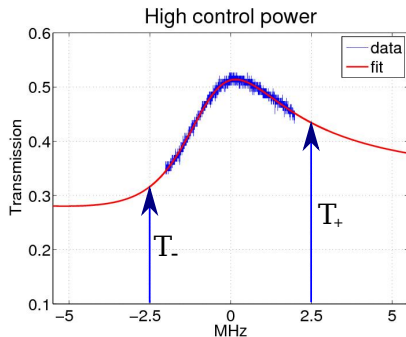
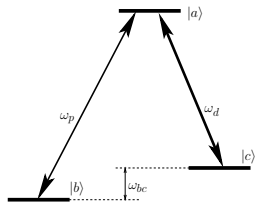


Observation of reduction of quantum noise below the shot noise limit is corrupted by the excess noise due to atomic interaction with atoms.

Squeezing and EIT filter

$$\varphi_{\pm} = \frac{1}{2} (\Theta_{+} \pm \Theta_{-})$$

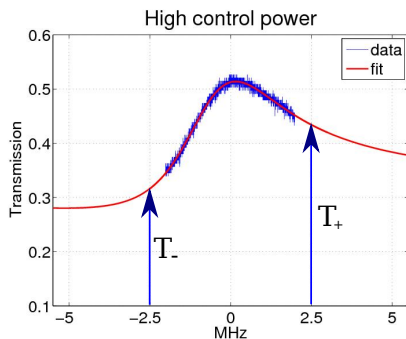
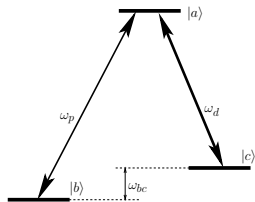
$$A_{\pm} = \frac{1}{2} (T_{+} \pm T_{-})$$



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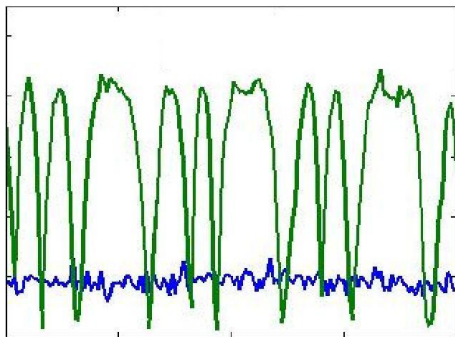
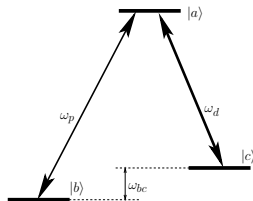
$$\begin{pmatrix} V_1^{out} \\ V_2^{out} \end{pmatrix} = \begin{pmatrix} A_+^2 & A_-^2 \\ A_-^2 & A_+^2 \end{pmatrix} \begin{pmatrix} V_1^{in} \\ V_2^{in} \end{pmatrix} + [1 - (A_+^2 + A_-^2)] \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

Eugeniy E. Mikhailov et al. Physical Review A, 73, 053810, (2006).

Squeezing and EIT filter

$$\varphi_{\pm} = \frac{1}{2} (\Theta_{+} \pm \Theta_{-})$$

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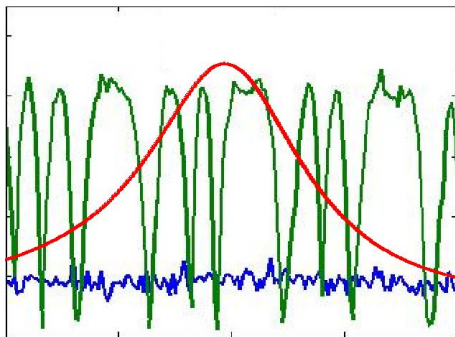
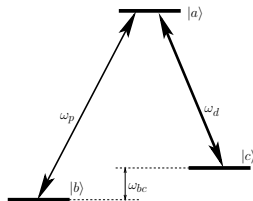
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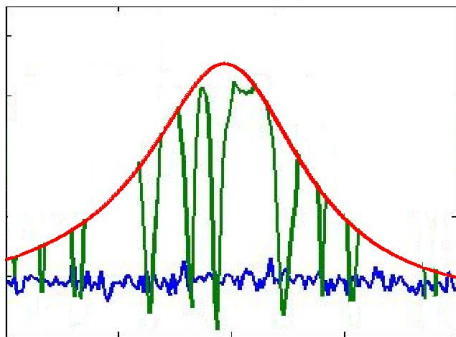
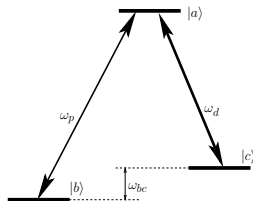
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Squeezing and EIT filter

$$\varphi_{\pm} = \frac{1}{2} (\Theta_{+} \pm \Theta_{-})$$

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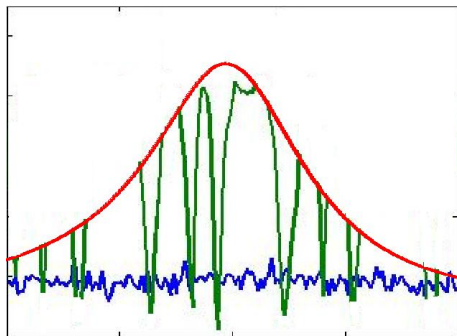
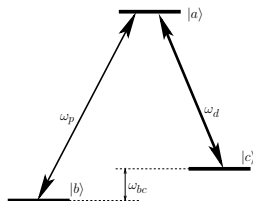
Squeezing and the simplest symmetric filter

Simple case $T_+ = T_- = T$

$$\varphi_{\pm} = 0$$

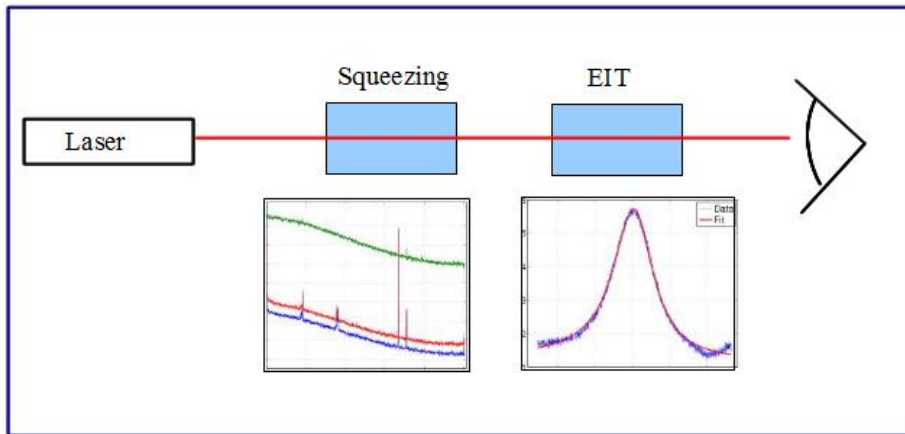
$$A_+ = T$$

$$A_- = 0$$

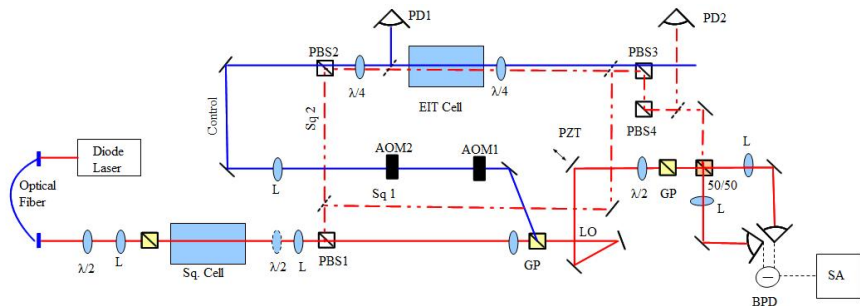


$$\begin{pmatrix} V_1^{out} \\ V_2^{out} \end{pmatrix} = \begin{pmatrix} T^2 & 0 \\ 0 & T^2 \end{pmatrix} \begin{pmatrix} V_1^{in} \\ V_2^{in} \end{pmatrix} + [1 - T^2] \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

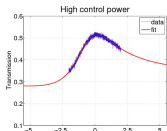
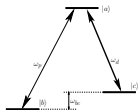
Squeezing and EIT filter setup



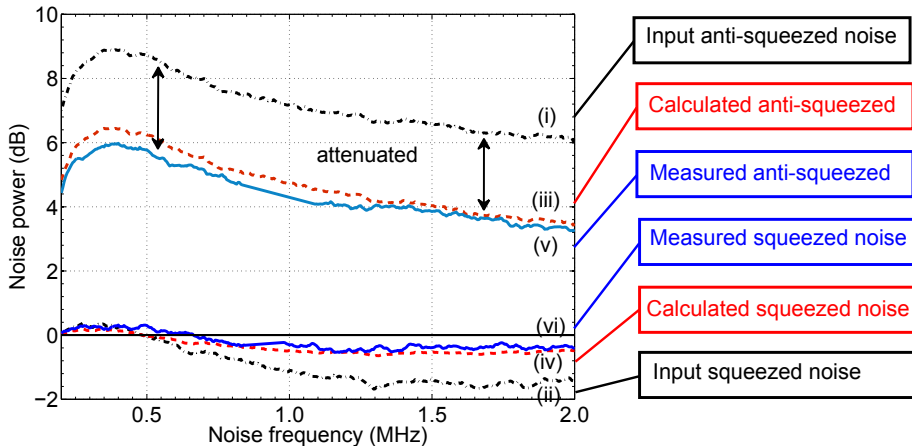
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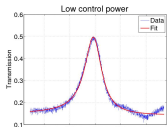
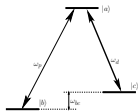
Wide EIT filter and squeezing



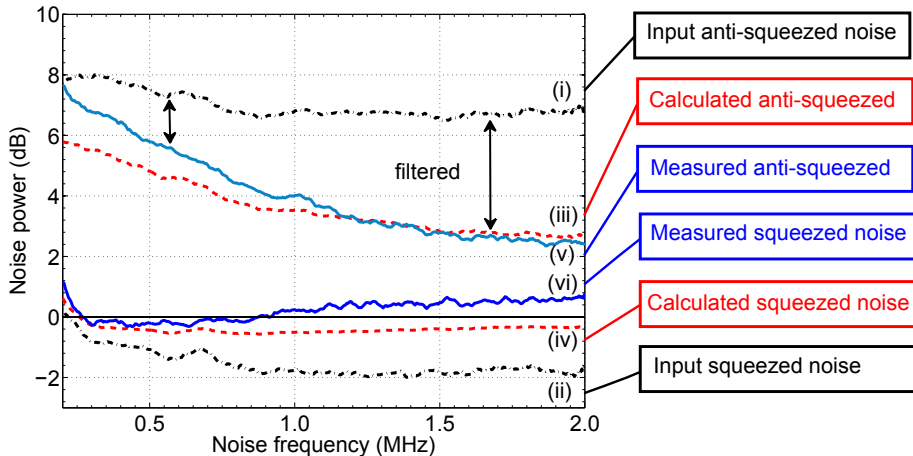
- Peak transmission = 52%
- FWHM = 4 MHz



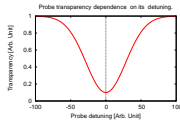
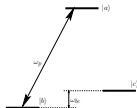
Narrow EIT filter and squeezing



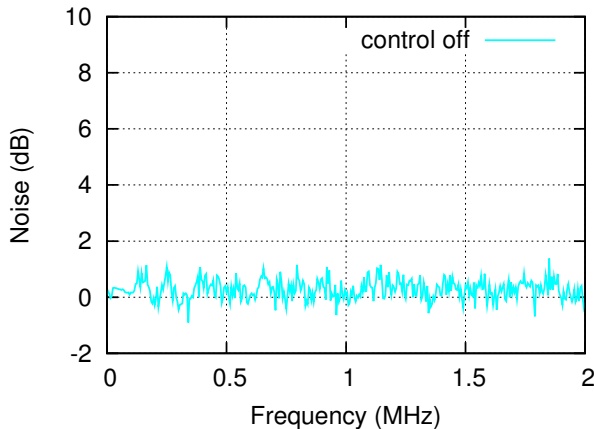
- Peak transmission = 50%
- FWHM = 2MHz



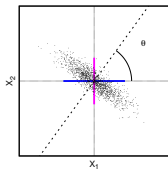
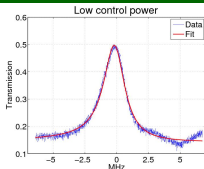
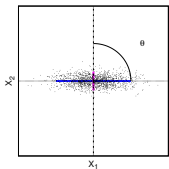
Control off no EIT and no squeezing at the output



- Peak transmission = 0%



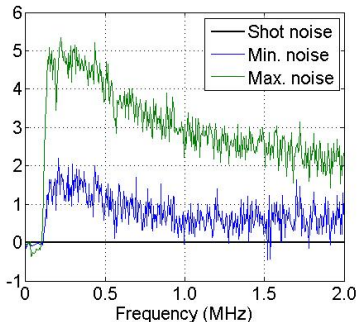
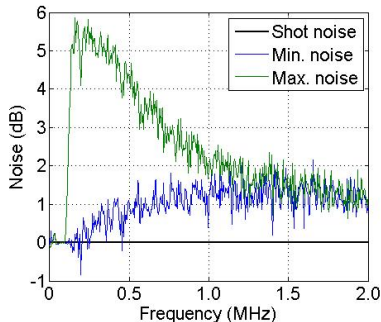
Squeezing angle rotation



$$\begin{pmatrix} V_{1out} \\ V_{2out} \end{pmatrix} = \begin{pmatrix} \cos^2 \varphi_+ & \sin^2 \varphi_+ \\ \sin^2 \varphi_+ & \cos^2 \varphi_+ \end{pmatrix} \begin{pmatrix} A_+^2 & A_-^2 \\ A_-^2 & A_+^2 \end{pmatrix} \begin{pmatrix} V_{1in} \\ V_{2in} \end{pmatrix} + [1 - (A_+^2 + A_-^2)] \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

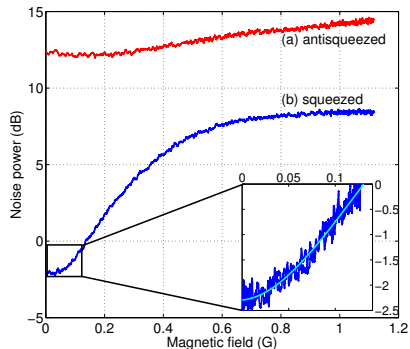
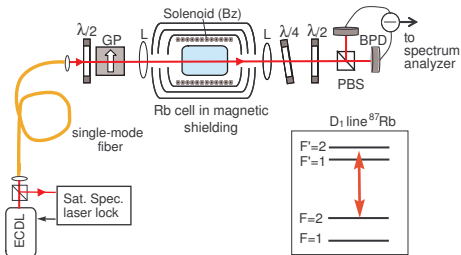
Locked at 300kHz

Locked at 1200kHz



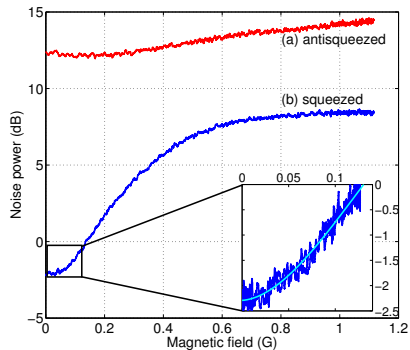
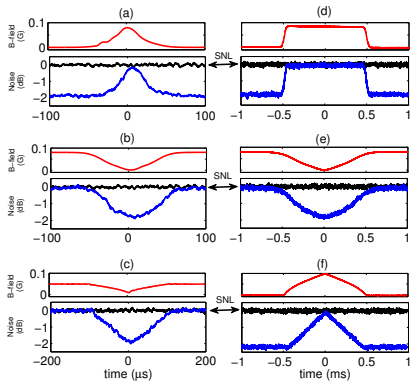
Squeezing vs magnetic field

Spectrum analyzer settings: Central freq = 1 MHz, VBW = 3 MHz, RBW = 100 kHz

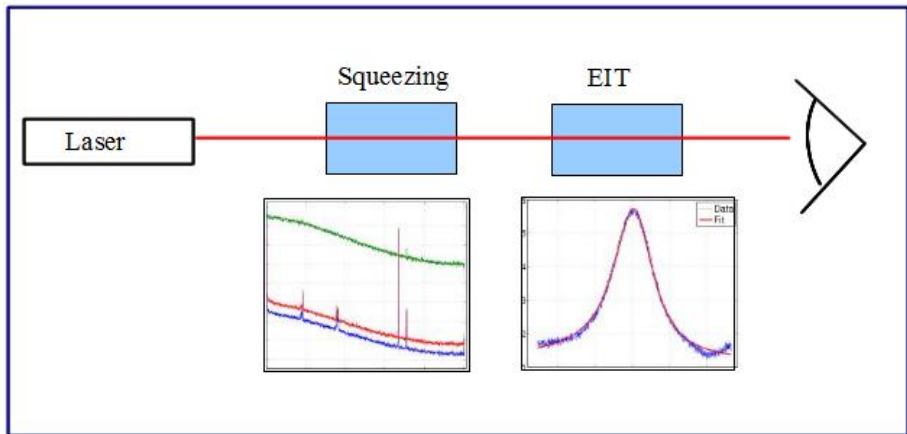


Squeezing vs magnetic field

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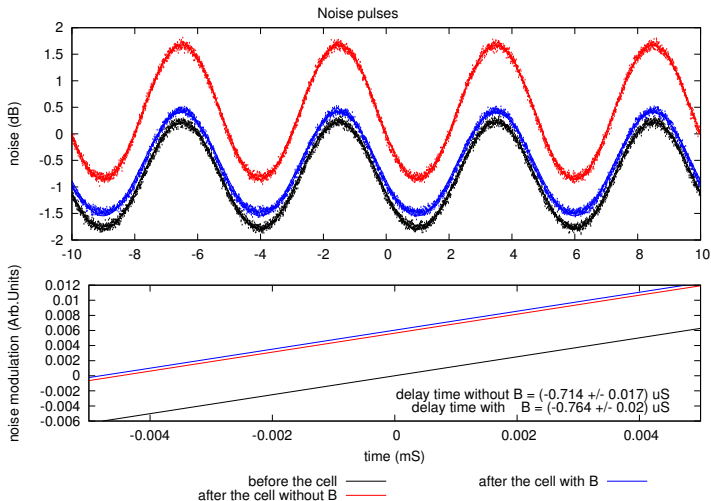


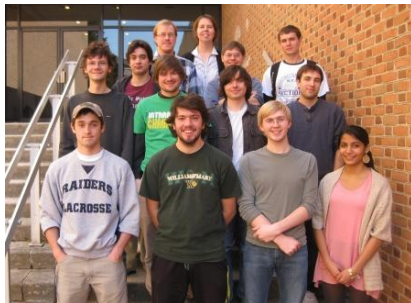
Delay/advancement measurement setup



Fast squeezed light

Spectrum analyzer settings: Central freq = 1 MHz, VBW = 3 MHz, RBW = 100 kHz





Support from



- We demonstrate fully atomic generation and manipulation of squeezing
- Squeezing is generated in the range from 100 Hz to several MHz

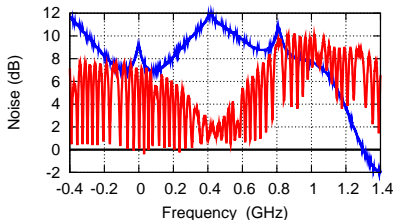
Advantages of the PSR squeezing

- Requires very little optical power (< 100 mW)
- Generated at atomic transition wavelength
- Potentially can be generated at any wavelength where the suitable transition exists
 - think blue or even ultraviolet

Noise contrast vs detuning in hot ^{87}Rb vacuum cell

$$F_g = 2 \rightarrow F_e = 1, 2$$

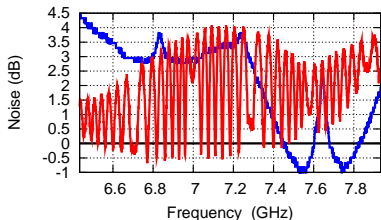
Noise vs detuning



Transmission — PSR noise

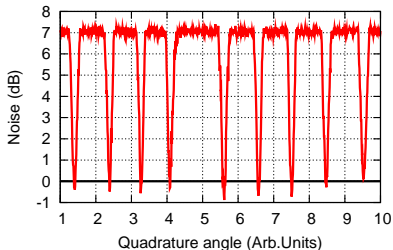
$$F_g = 1 \rightarrow F_e = 1, 2$$

Noise vs detuning

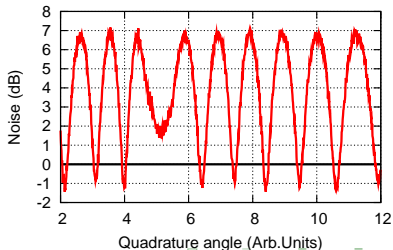


Transmission — PSR noise

Noise vs quadrature angle



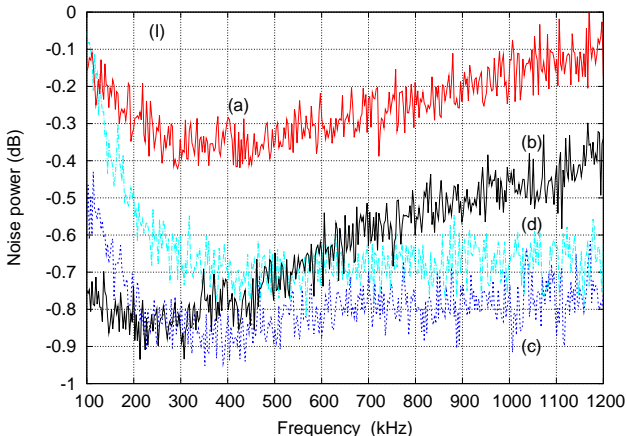
Noise vs quadrature angle



Squeezing spectrum vs pump power in ^{87}Rb

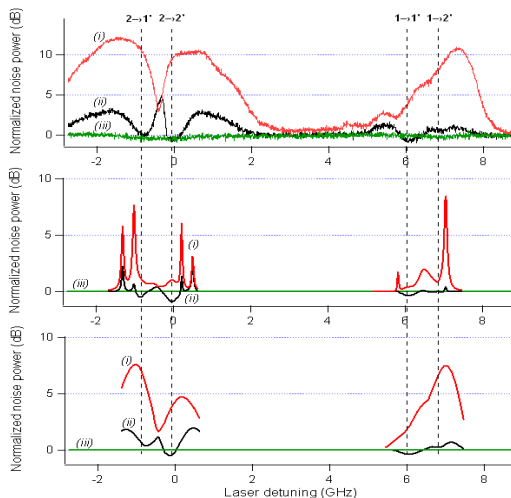
^{87}Rb cell + 2.5Torr Ne, $T=63.3^\circ\text{C}$

(a) $P=1.0$ mW, (b) $P=1.5$ mW, (c) $P=4.2$ mW, (d) $P=6.6$ mW



Squeezing theory and experiment

- ^{87}Rb cell
- no buffer gas
- density $2 \cdot 10^{11} \text{ cm}^{-3}$
- laser power 6 mW
- beam size 0.2 mm



E.E. Mikhailov, A. Lezama, T. Noel and I. Novikova,
J. Mod. Opt. **56**, 1985 (2009).