

# Quantum noise imaging using atom-based squeezed light sources

Status update on 2022 progress AFOSR FA9550-19-1-0066

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1



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Savannah Cuozzo



Irina Novikova



Hwang Lee



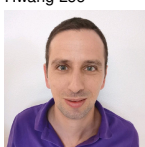
Jon Dowling (1955-2020)



Charris Gabaldon



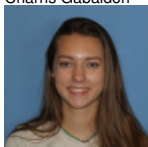
Ziqi Niu



Lior Cohen



Pratik Barge



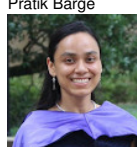
Caitlyn Marat



Nikunj Kumar Prajapati



Narayan Bhusal

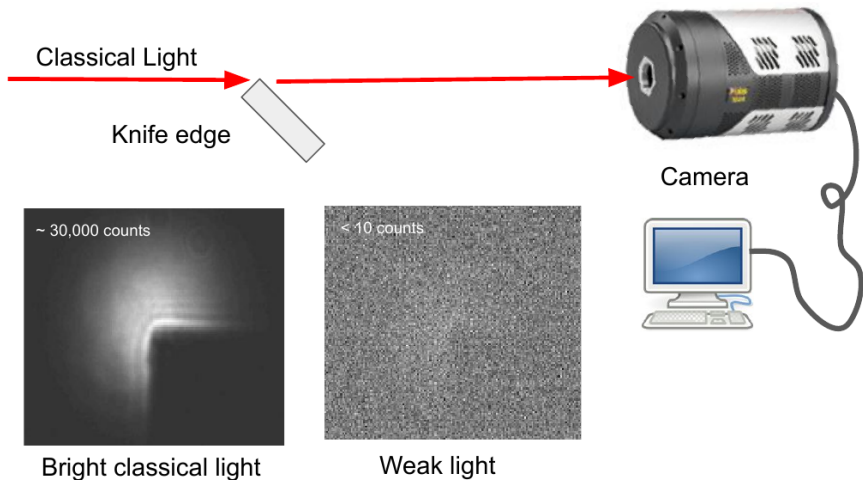


Elisha Metekole

# Outline

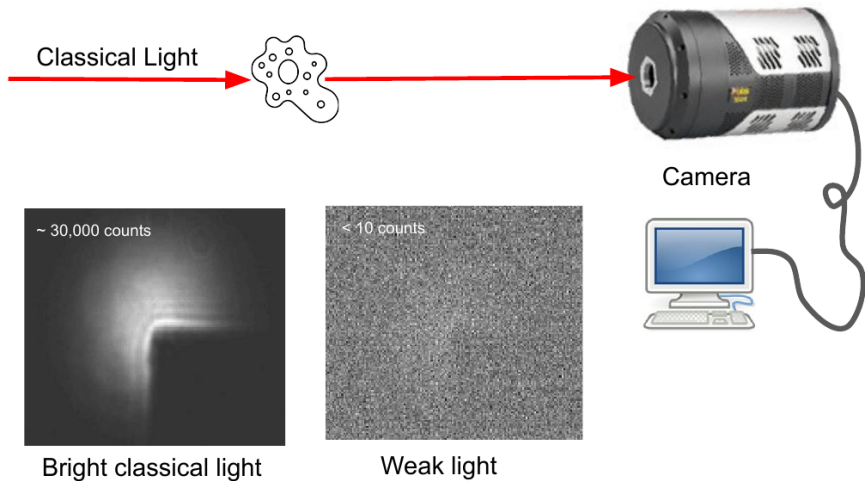
- 1 Shadow imaging with squeezed light
- 2 Squeezing mode search via optimization
- 3 Shadow imaging with thermal light
- 4 Imaging without camera: single pixel imaging
  - Classical detour: single pixel homodyning
  - Quantum quadrature single pixel homodyning

# From bright to low light imaging



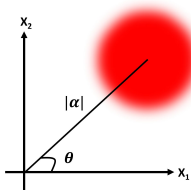


# From bright to low light imaging

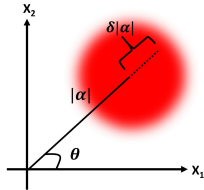


# Let's look at quantum picture

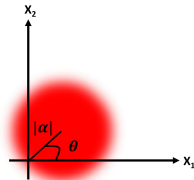
Bright state in



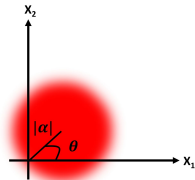
Bright state out



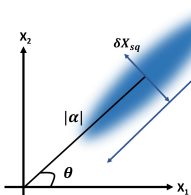
Low-light state in



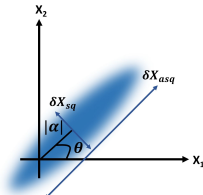
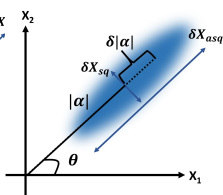
Low-light out



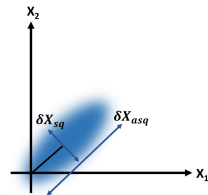
$$\alpha_{out}^2 = \alpha_{in}^2 T$$



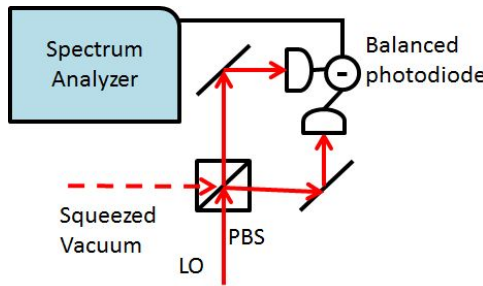
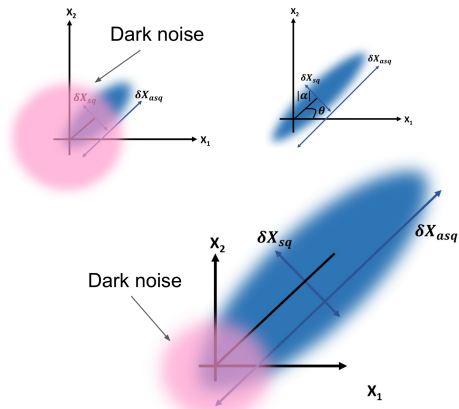
$$V = 1 + (\delta X_{sq/asq}^2 - 1) |\mathcal{O}|^2 T$$



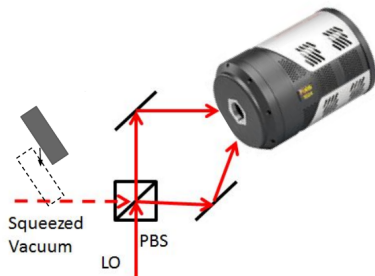
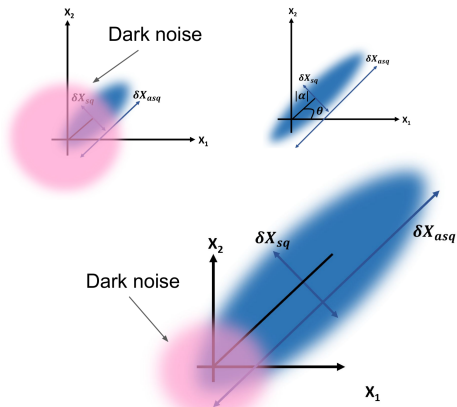
$$\mathcal{O} = \int_A u_{LO}^*(x, y) u_{in}(x, y) dA$$



# Detector dark noise



# Detector dark noise



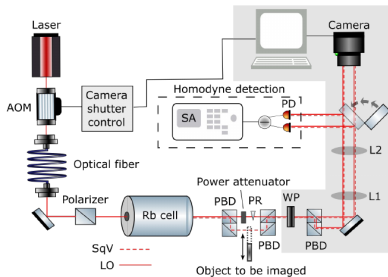
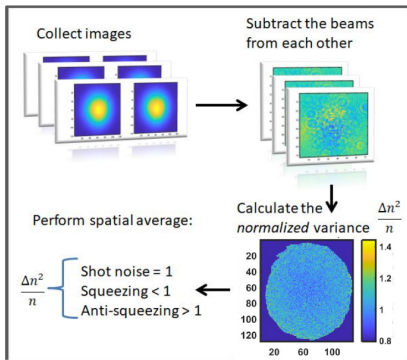
Elisha Metekole

“Quantum-Limited Squeezed Light Detection with a Camera”, Phys. Rev. Lett. **125**, 113602

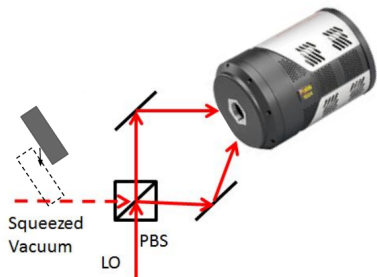
# Imaging quantum noise



Savannah Couzzo



# Imaging quantum noise with binning



$$V = 1 + (\delta X_{sq/asq}^2 - 1) |\mathcal{O}|^2 T$$

- Single pixel analysis = shot noise limited



Binning = 1

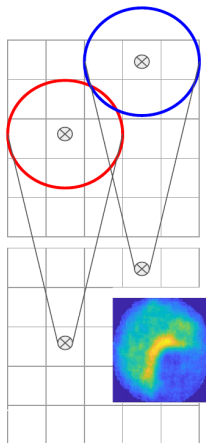


Binning = 4

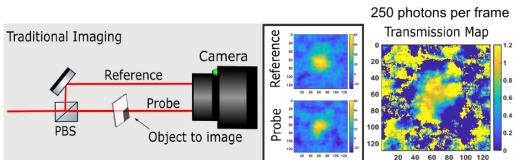
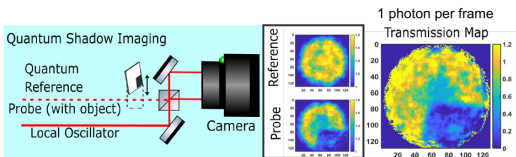


Binning = 16

- Binning pixels reveals non-classical statistics

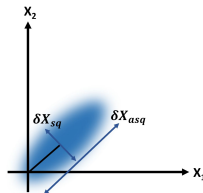


# Shadow imaging



$$V_{pr} = 1 + (\delta X_{ref}^2 - 1)|\mathcal{O}|^2 T$$

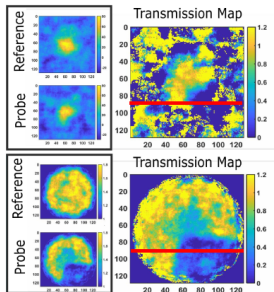
$$T = \frac{V_{pr} - 1}{V_{ref} - 1}$$



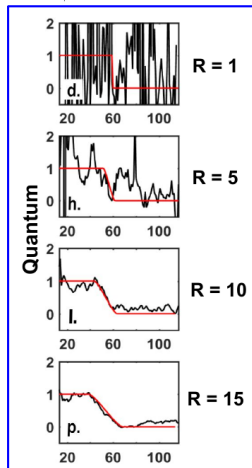
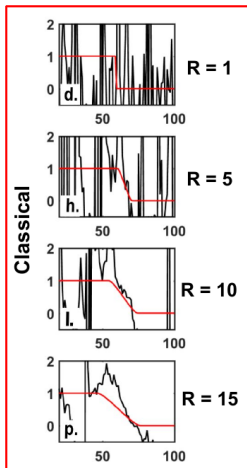
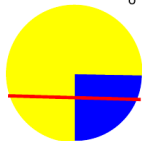
$$T = \frac{|\alpha_{pr}|^2}{|\alpha_{ref}|^2} = \frac{N_{pr}}{N_{ref}}$$

# Similarity Parameter

## Transmission Map Cross-section



Ideal case:  $T_o$



$$S = \frac{\sum T_{exp} T_o}{\sqrt{\sum T_{exp}^2 \sum T_o^2}}$$

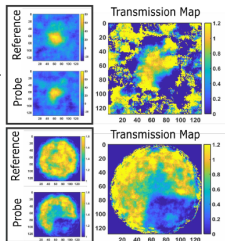
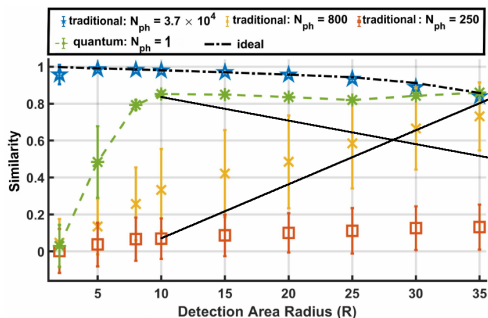


# Similarity Parameter

$$S = \frac{\sum T_{exp} T_o}{\sqrt{\sum T_{exp}^2 \sum T_o^2}}$$



Savannah Couzzo



“Low-Light Shadow Imaging Using Quadrature-Noise Detection with a Camera”, **Advanced Quantum Technologies**, 2100147, (2022)

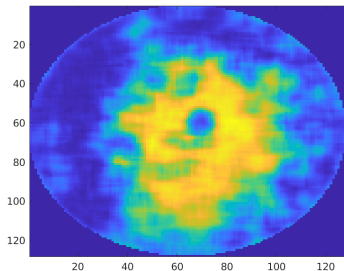
# What is the spatial output of the squeezer?



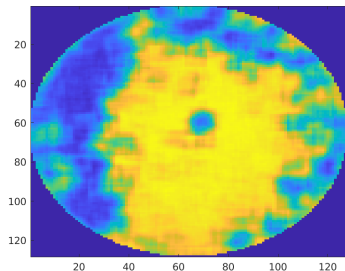
Caitlyn Marat

Find/optimize  
 $U_{sq}(x, y) \rightarrow \max \text{ Variance.}$   
Wait about 20 CPU hours.

Allow to toggle on 20%

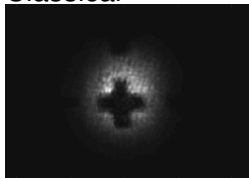


Allow to toggle on 50%

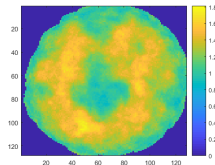


# Comparing different imaging

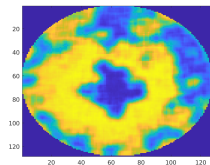
Classical



Quantum Binning



Quant. Optimization

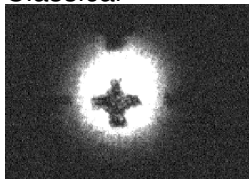


$$u_{sq}(x, y) \rightarrow \max V$$

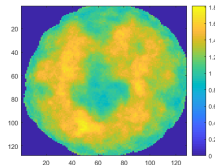
800 photons in total was used for quantum noise quadrature reconstruction

# Comparing different imaging

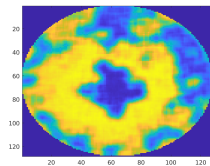
Classical



Quantum Binning



Quant. Optimization



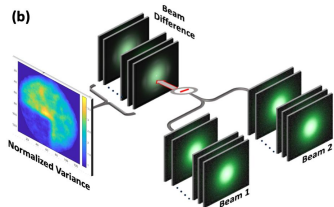
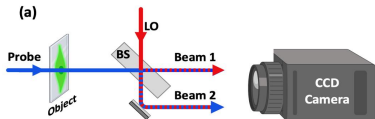
$$u_{sq}(x, y) \rightarrow \max V$$

800 photons in total was used for quantum noise quadrature reconstruction

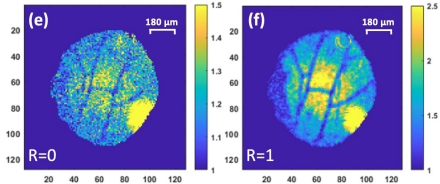
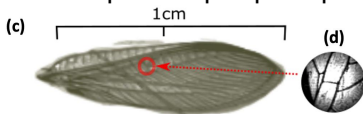
# Imaging with thermal light



Ziqi Niu



0.1 photon per pixel per exposure

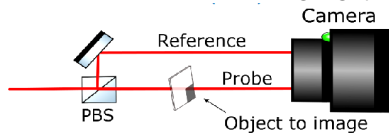


# Quadrature Shadow Imaging: theoretical framework



Pratik Barge

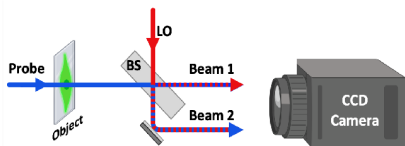
## Classical differential imaging (CDI)



Measures intensity (photon number) directly

$$SNR_{CDI} = \frac{(1-t)\bar{n}}{\sqrt{(1+t)\bar{n} + (\Delta N_d)^2}}$$

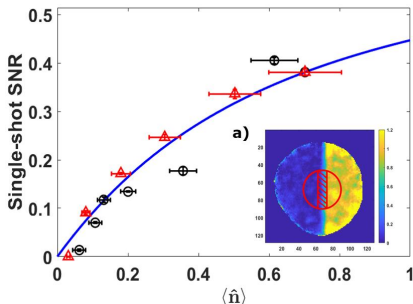
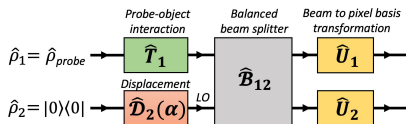
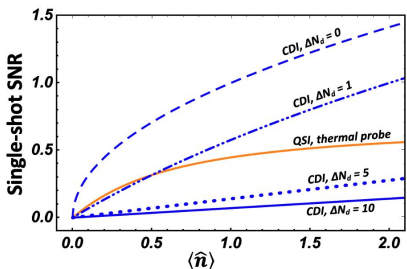
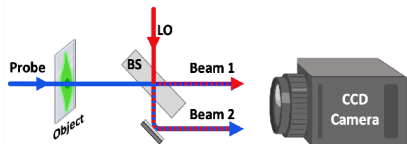
## Quadrature Shadow Imaging (QSI)



Measures variances in photon number

$$SNR_{QSI} = \frac{2(1-t)\bar{n}}{\sqrt{4 + 8(1+t)\bar{n} + 8(1+t^2)\bar{n}^2}}$$

# Classical (CDI) vs quantum (QSI)



“Weak thermal state quadrature-noise shadow imaging”, Pratik J. Barge, Ziqi Niu, Savannah L. Cuozzo, Eugeny E. Mikhailov, Irina Novikova, Hwang Lee, and Lior Cohen, **Optics Express** Vol. 30, Issue 16, pp. 29401-29408 (2022)

<https://doi.org/10.1364/OE.455646>

# Classical single pixel imaging

## Single-pixel imaging 12 years on: a review

GRAHAM M. GIBSON,<sup>1,2</sup> STEVEN D. JOHNSON,<sup>1,3</sup> AND MILES J. PADGETT<sup>1,4</sup>

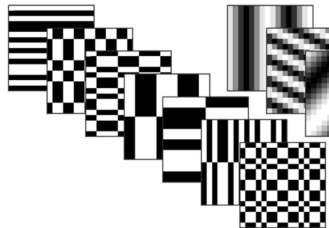
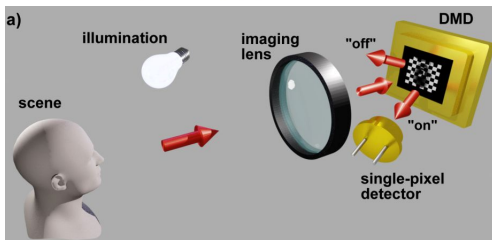
<sup>1</sup>School of Physics and Astronomy, University of Glasgow, Glasgow G12 8QQ, UK

<sup>2</sup>graham.gibson@glasgow.ac.uk

<sup>3</sup>steven.johnson@glasgow.ac.uk

<sup>4</sup>miles.padgett@glasgow.ac.uk

<https://www.gla.ac.uk/schools/physics/ourresearch/groups/optics/>

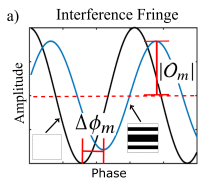
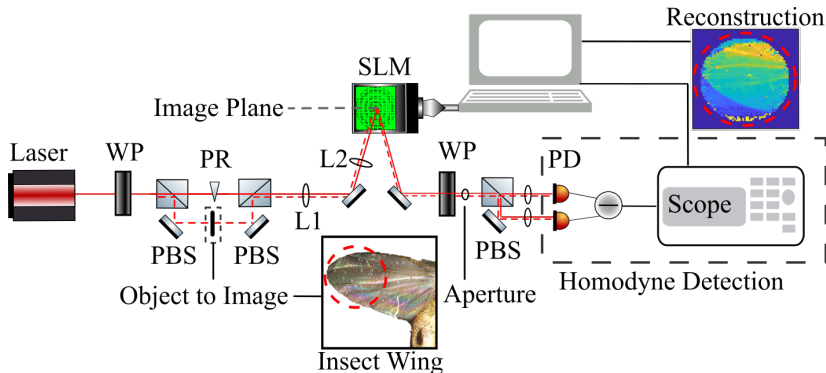


Reconstructed object

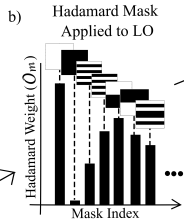
$$Ob(x, y) = \frac{1}{M} S_m P_m(x, y)$$



# Classical single pixel homodynying



$$O_m = |O_m| e^{i\Delta\phi_m}$$

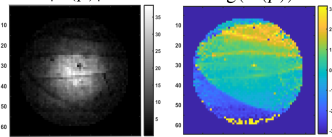


c) Reconstruct Image by Summing  $H_m$

$$S(p) = \frac{1}{M} \sum_{m=1}^M |O_m| e^{i\Delta\phi_m} H_m(p)$$

$|S(p)|$

$\arg(S(p))$



# Homodyning = full wavefront reconstruction



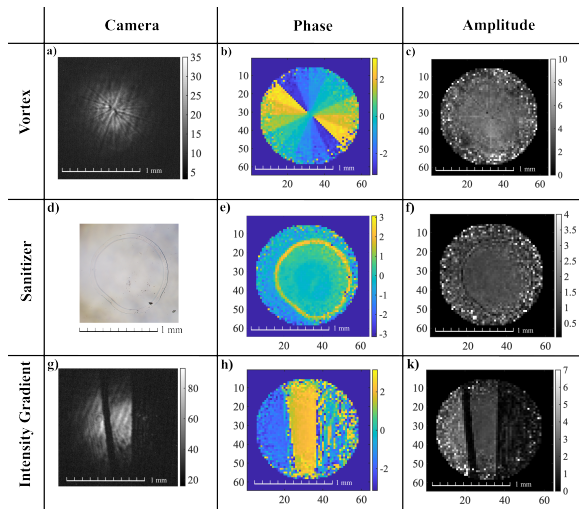
Charris Gabaldon

Wavefront product

$$u_{LO}^*(p)u_{in}(p)$$

Transmission:

- amplitude
- phase

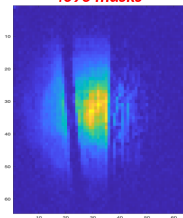


“Wave-Front Reconstruction via Single-Pixel Homodyne Imaging”

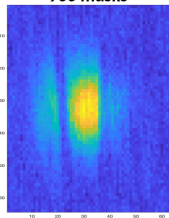
<https://arxiv.org/abs/2208.02718>

# Compressive sampling modeling

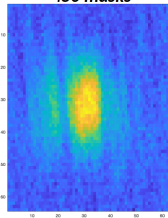
**Original Image:**  
**4096 masks**



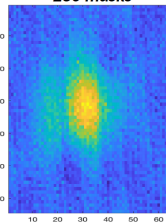
**Reconstruction:**  
**900 masks**



**Reconstruction:**  
**450 masks**

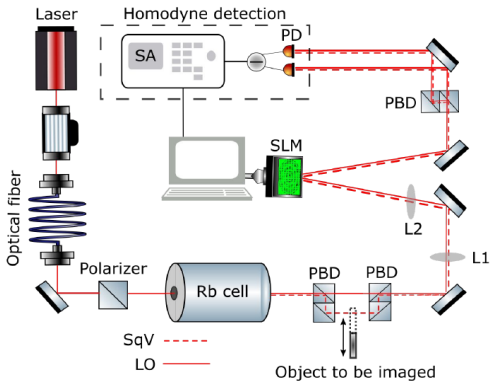


**Reconstruction:**  
**280 masks**

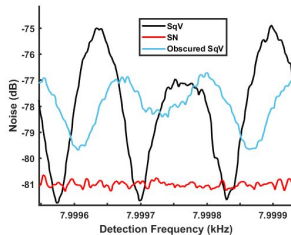
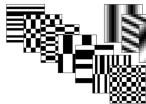


- Drastic reduction in acquisition time
- Increase in post processing complexity

# Single pixel homodyning imaging with quantum noise



Savannah Couzzo

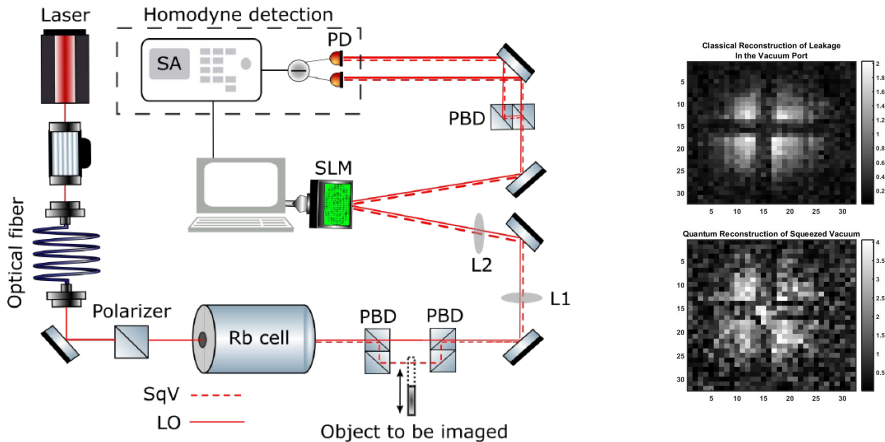


$$V_m = 1 + (\delta X_{sq/asq}^2 - 1) |O_m|^2$$

$$O_m = \int_A P_m u_{lo} u_q^* T dA$$

$$u_{lo} u_q^* T = \frac{1}{M} \sum O_m P_m(x, y)$$

# Single pixel homodyning imaging with quantum noise: wire cross

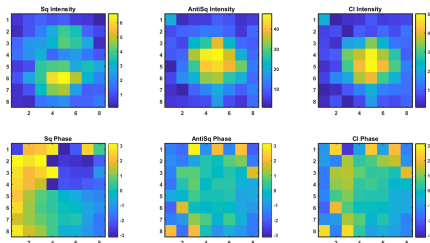
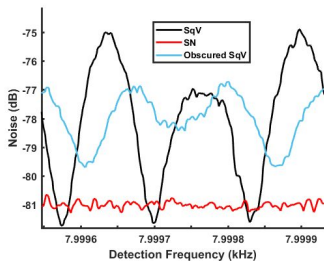


# Single pixel homodyning using different quantum quadratures: squeezer output

$$V_m = 1 + (\delta X_{sq/asq}^2 - 1) |\mathcal{O}_m|^2$$

$$\mathcal{O}_m = \int_A P_m u_{lo} u_q^* T dA$$

$$u_{lo} u_q^* T = \frac{1}{M} \sum \mathcal{O}_m P_m(x, y)$$



# Summary

## Developed methods

- Camera Quantum shadow imaging with squeezed or thermal states
- Single pixel homodyning for classical and quantum illumination

## Advantages

- Overcome detectors dark noise
- Suitable for low light illumination: covert or avoiding sample damage
- Outperforming classical detection at low light illumination contaminated by detector dark noise

## Next step

- Refining single pixel homodyning with quantum noise

