LIGO, squeezed states of light, and nonlinear light-atom interactions.



and Eugeniy E. Mikhailov



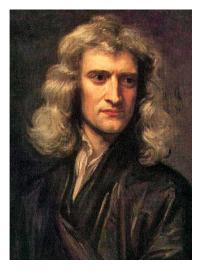
February 19, 2016



Outline

- History of gravity
 - Newton's laws
 - Einstein's laws
 - A bit of astrophysics
- 2 Detectors
 - Gravitational wave interferometer
- Operation
- Assorted LIGO pictures
 - Extra information
- Squeezing
 - LIGO noise budget
 - Squeezed states of light
 - Squeezing and interferometers
 - Polarization self-rotation squeezing
 - Setup
- 6 Magnetometry
 - Squeezing enhanced magnetometry

Newton's laws 1686





$$F_g = G \frac{m_1 m_2}{r^2}$$

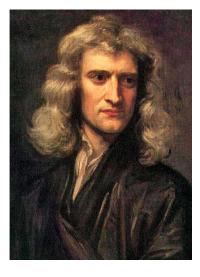
Laws of motion and law of gravitation solved problems of astronomy and terrestrial physics.

- eccentric orbits
- tides
- perturbation of moon orbit due to sun

Unified the work of Galileo, Copernicus and Kepler.

Did not explained precession of Mercury orbit

Newton's laws 1686





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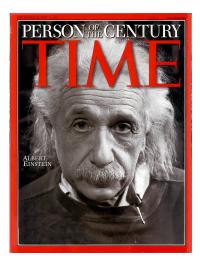
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Einstein's laws 1915

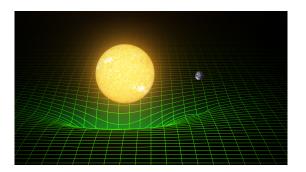


The General Theory of Relativity and theory of Gravity (1915)

- No absolute motion thus only relative motion
- Space and time are not separate thus four dimensional space-time
- Gravity is not a force acting at a distance thus warpage of space-time

General relativity

- A geometric theory connecting matter to spacetime
- Matter tells spacetime how to curve
- Spacetime tells matter how to move



important predictions

- ullet Light path bends in vicinity of massive object o confirmed in 1919
- Gravitational radiation (waves) \rightarrow confirmed indirectly in 1974

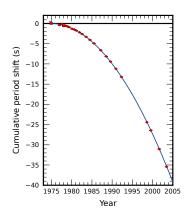
Indirect observation of gravitational wave

Emission of gravitational radiation from pulsar PSR1913+16 leads to loss of orbital energy.

- orbital period decreased by 36 sec from 1975 to 2005
- measured to 50 ms accuracy
- deviation grows quadratically with time

This can be explained by general relativistic effects: J.H. Taylor and J.M. Weisberg, Astrophysical Journal, Part 1, vol. 253, Feb. 15, 1982, p. 908-920.

Nobel prize in 1993 to Hulse and Taylor



Astrophysical sources of GW

- Coalescing compact binaries
 - objects: NS-NS, BH-NS, BH-BH
 - physics regimes: Inspiral, merger, ringdown

- Periodic sources
 - spinning neutron stars (pulsars)







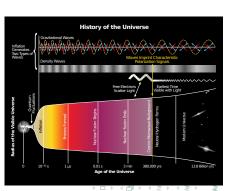


Astrophysical sources of GW (cont)

- Burst events
 - Supernovae with asymmetric collapse



- Stochastic background
 - right after Big Bang $(t = 10^{-43} \text{ sec})$
 - continuum of sources



Astrophysics with GWs vs. E&M

E&M (photons)

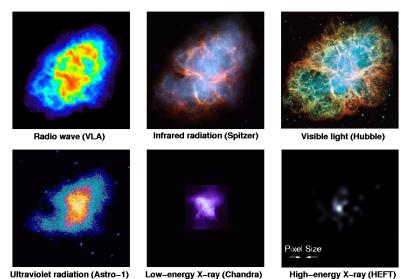
- Space as medium for field
- Accelerating charge
- Absorbed, scattered, dispersed by matter
- 10 MHz and up
- Light = not dark (but >95% of Universe is dark)

GW

- Spacetime itself ripples
- Accelerating aspherical mass
- Very small interaction; matter is transparent
- 10 kHz and down
- Radiated by dark mass distributions

New view to the universe

Crab Nebula: Remnant of an Exploded Star (Supernova)

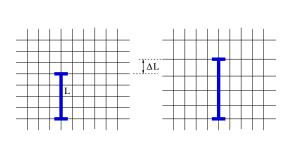


Gravitational waves (GW)

- Predicted by the General Theory of Relativity
- Generated by aspherical mass distribution
- Induce space-time ripples which propagate with speed of light

New tool for astrophysics

GW stretch and squeeze space-time thus move freely floating objects



Strain - strength of GW

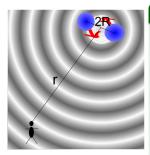
$$h = \frac{\Delta L}{L} \tag{1}$$

typical strain

$$h \sim 10^{-21}$$

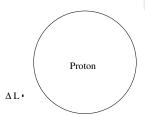
February 19, 2016

Typical strain



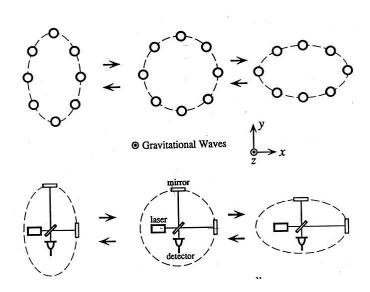
Two neutron star

with a mass of 1.4 solar masses each orbiting each other with a frequency $f=400~{\rm Hz}$ at a distance $2R=20~{\rm km}$ would generate strain $h\sim 10^{-21}$ at distance equal to $10^{23}~{\rm m}$ (distance to the Virgo cluster) For 4 km base line that would correspond to ΔL thousand times smaller than size of proton.

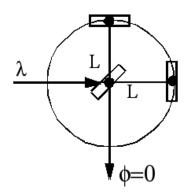


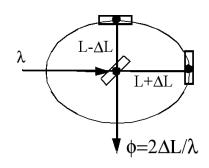
Detection of GW is difficult problem

GW acting on matter



Interferometric Measurement



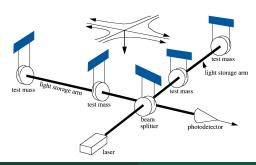


Laser Interferometer Gravitational-wave Observatory

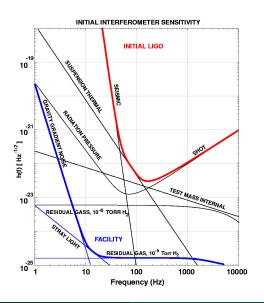




- L = 4 km
- $h \sim 2 \times 10^{-23}$
- \bullet $\Delta L \sim 10^{-20} \text{ m}$



Initial LIGO sensitivity goal and noise budget



Displacement noise

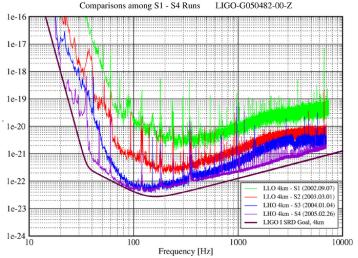
- seismic
- thermal suspension
- thermal Brownian
- radiation pressure noise

Detection noise

- electronics
- shot noise

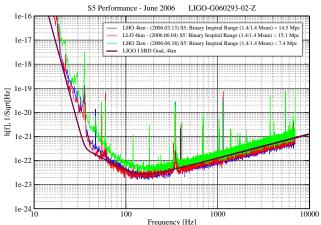
LIGO sensitivity, S1-S4 runs

Best Strain Sensitivities for the LIGO Interferometers

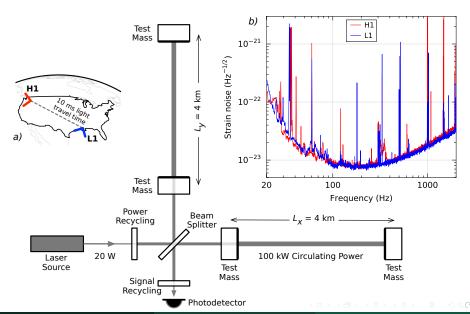


LIGO sensitivity, S5 run, June 2006

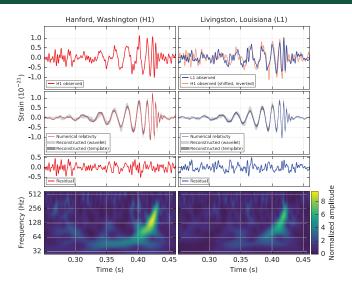
Strain Sensitivity for the LIGO Interferometers



LIGO detector summary



GW signal at 09:50:45 UTC on 14 September 2015

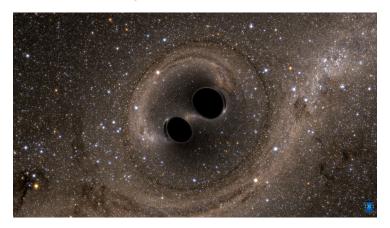


LIGO Scientific Collaboration, "Observation of Gravitational Waves from a Binary Black Hole Merger", Phys. Rev. Lett., 116, 061102 (2016).

20 / 46

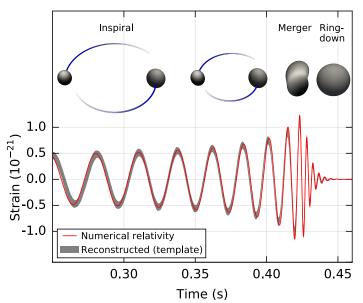
The sound of gravitational wave and simulated sky

- The Sound of Two Black Holes Colliding
- Two Black Holes Merge into One

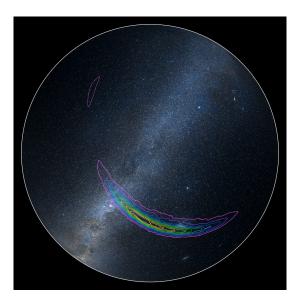


Two black holes with 29 and 36 solar masses merged about 1.3 billion years ago

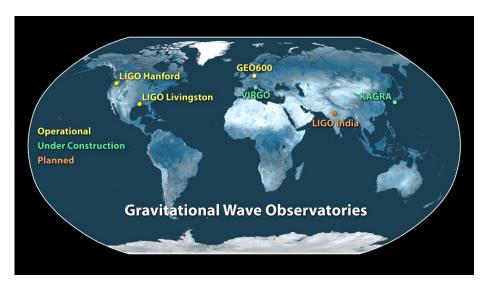
Reconstructed signal



GW source location at the southern hemisphere sky



World wide network of detectors



Seismic isolation



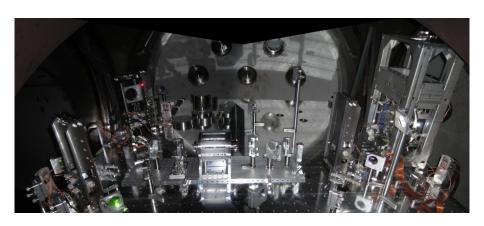
Part of large system



Work in chamber



Inside vacuum chamber



Mirror



Inner test mass



We can catch GW but ...



Additional links



www.ligo.org

Couple movies

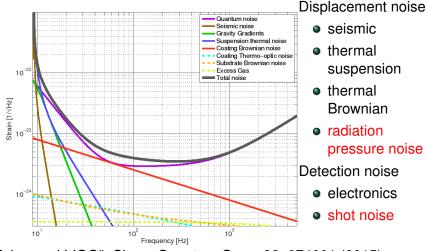
- LIGO Generations http://www.space.com/ 28409-ligo-generations-the-film-hd-video.html
- LIGO: A Passion for Understanding http://www.space.com/ 25455-ligo-documentary-film-complete-coverage. h+m1

You can help to detect a gravitational wave

www.einsteinathome.org



Advanced LIGO sensitivity goal and noise budget



"Advanced LIGO", Class. Quantum Grav., 32, 074001 (2015)

Heisenberg uncertainty principle and its optics equivalent



Heisenberg uncertainty principle

 $\Delta p \Delta x \geq \hbar/2$

The more precisely the POSITION is determined, the less precisely the MOMENTUM is known, and vice versa

Heisenberg uncertainty principle and its optics equivalent



Heisenberg uncertainty principle

 $\Delta p \Delta x \geq \hbar/2$

The more precisely the POSITION is determined, the less precisely the MOMENTUM is known, and vice versa

Optics equivalent

 $\Delta \phi \Delta N > 1$

The more precisely the PHASE is determined, the less precisely the AMPLITUDE is known, and vice versa

Heisenberg uncertainty principle and its optics equivalent



Heisenberg uncertainty principle

 $\Delta p \Delta x \geq \hbar/2$

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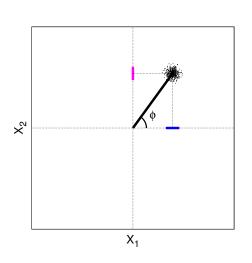
Optics equivalent

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The more precisely the PHASE is determined, the less precisely the AMPLITUDE is known, and vice versa

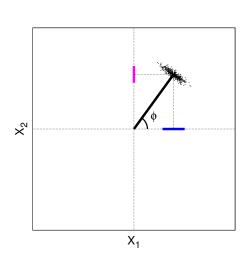
Optics equivalent strict definition

 $\Delta X_1 \Delta X_2 \geq 1/4$



Unsqueezed coherent





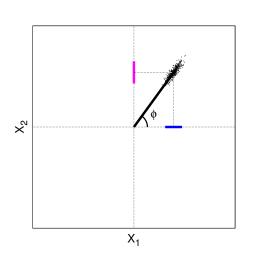
Unsqueezed coherent





Amplitude squeezed





Unsqueezed coherent



Phase

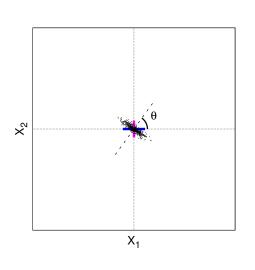
squeezed



Amplitude squeezed







Unsqueezed coherent







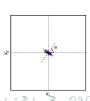




Phase squeezed

Vacuum squeezed

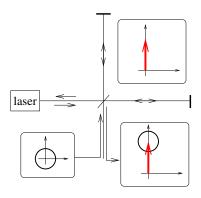




Squeezing and interferometer

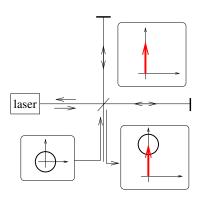
Squeezing and interferometer

Vacuum input

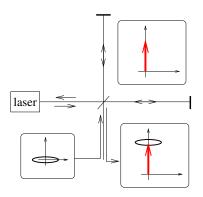


Squeezing and interferometer

Vacuum input

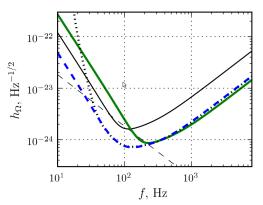


Squeezed input



Interferometer sensitivity improvement with squeezing

F. Ya. Khalili Phys. Rev. D 81, 122002 (2010) Projected advanced LIGO sensitivity

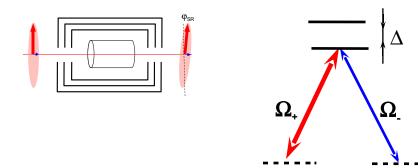


Experimental demonstration with LIGO detectors Nature Physics, **4**, 472-476, (2008) Nature Photonics **7**, 613-619 (2013)

Squeezer optical table



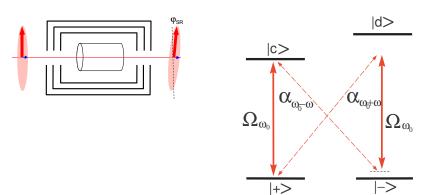
Self-rotation of elliptical polarization in atomic medium



A.B. Matsko et al., PRA 66, 043815 (2002): theoretically prediction of 4-6 dB noise suppression

$$a_{out} = a_{in} + \frac{igL}{2}(a_{in}^{\dagger} - a_{in})$$

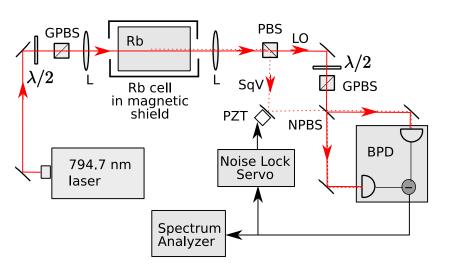
Self-rotation of elliptical polarization in atomic medium



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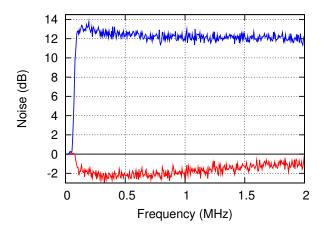
$$a_{out} = a_{in} + \frac{igL}{2}(a_{in}^{\dagger} - a_{in})$$

Setup



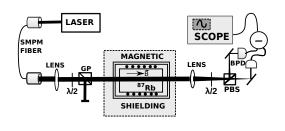
Maximally squeezed spectrum with 87Rb

W&M team. ⁸⁷Rb $F_g = 2 \rightarrow F_e = 2$, laser power 7 mW, T=65° C



Lezama et.al report 3 dB squeezing in similar setup Phys. Rev. A 84, 033851 (2011)

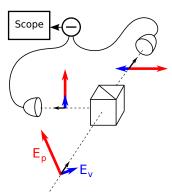
Shot noise limit of the magnetometer



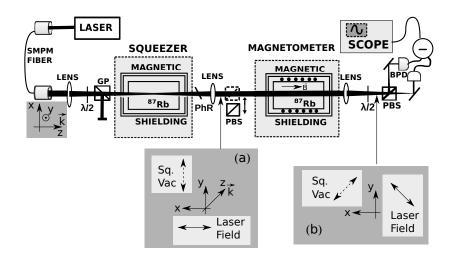
$$S = |E_{p} + E_{v}|^{2} - |E_{p} - E_{v}|^{2}$$

$$S = 4E_{p}E_{v}$$

$$< \Delta S > \sim E_{p} < \Delta E_{v} >$$

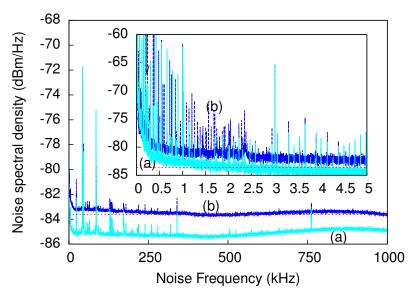


Squeezed enhanced magnetometer setup

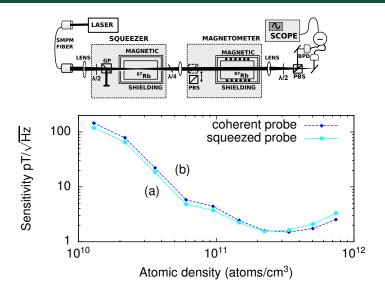


Note: Squeezed enhanced magnetometer was first demonstrated by Wolfgramm *et. al* Phys. Rev. Lett, **105**, 053601, 2010.

Magnetometer noise floor improvements



Magnetometer with squeezing enhancement



T. Horrom, et al. **PRA**, 86, 023803, (2012).

Summary

- Gravitational waves exist and they are detected
- Moreover we can learn from them and do GW astronomy
- The future is in quantum noise suppression