Towards fast-light gyroscope, modification of dispersion, and pulling sensitivity

Eugeniy E. Mikhailov, Matt T. Simons, Irina Novikova¹ Simon Rochester, Dmitry Budker²,



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Eugeniy E. Mikhailov (W&M)

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Sagnac effect in interferometer



$$t_{\pm} = \frac{2\pi R}{c} \left(1 \pm \frac{R\Omega}{c} \right)$$
$$\Delta t = t_{+} - t_{-} = \frac{4\pi R^{2}\Omega}{c^{2}}$$
$$\Delta \phi = 2\pi \frac{c\Delta t}{\lambda} = \frac{8\pi A\Omega}{c\lambda}$$

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Sagnac effect and cavity response



$$\Delta p = c\Delta t = \frac{4A\Omega}{c}$$
$$\Delta f = f_0 \frac{\Delta p}{p} \frac{1}{n_g} = \Delta f_{empty} \frac{1}{n_g}$$

Group index

$$n_g(f) = n + f_0 \frac{\partial n}{\partial f}$$

Cavity response enhanced if $n_q < 1$ i.e. under the fast light condition Shahriar et al., PRA 75, 053807 (2007)





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N-scheme, with forbidden transition - fast but no gain



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N-bar with four-wave mixing - fast and with gain



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N-bar with four-wave mixing - optimal parameters



N. B. Phillips, *et al.* Journal of Modern Optics, Issues 1, 60, 64-72, (2013).

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N-bar with Doppler averaging



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N-bar field competition

 $\Omega_4 = 0$

$$\Omega_4 = \Omega_2/2$$

$$\Omega_4 = \Omega_2$$



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N-bar beam propagation









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N-bar beam propagation







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N-bar scheme linearly polarized pumps - single pass



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Gyro lasing - no fast light condition



Lasing conditions

- round trip gain is 1
- round trip phase shift is 0

Simulation parameters

- N = 9.6 \times 10¹⁰ 1/cm³
- $\delta_1 = -2\pi \times 800 \text{ MHz}$
- $\delta_3 = 0 \text{ MHz}$
- $\Omega_1 = 6 \text{ mW/cm}^2$
- $\Omega_3 = 10 \text{ mW/cm}^2$
- Finesse = 18

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Gyro lasing - fast light condition, single frequency



Lasing conditions

- round trip gain is 1
- round trip phase shift is 0

Simulation parameters

- N = $4.8 \times 10^{10} \ 1/cm^3$
- $\delta_1 = 0 \text{ MHz}$
- $\delta_3 = 0 \text{ MHz}$
- $\Omega_1 = 48.2 \text{ mW/cm}^2$
- $\Omega_3 = 192.9 \text{ mW/cm}^2$
- Finesse = 60

 $\Delta f = 150 \Delta f_{empty.cavity}$

Gyro lasing - fast light condition, multiple frequencies



Lasing conditions

- round trip gain is 1
- round trip phase shift is 0

Simulation parameters

• N = $4.8 \times 10^{10} \ 1/cm^3$

•
$$\delta_1 = 0 \text{ MHz}$$

- $\delta_3 = 0 \text{ MHz}$
- $\Omega_1 = 50.6 \text{ mW/cm}^2$, 5% higher
- $\Omega_3 = 192.9 \text{ mW/cm}^2$
- Finesse = 60

Multiple lazing points might be problematic in the experiment

First gyro setup and its performance



 Ω_2 tuned around $F = 1 \rightarrow F' = 1, 2$

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First gyro setup and its performance



E. Mikhailov, et al. Optical Engineering, Issue 10, 53, 102709, (2014)

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Gyro setup and lasing beat-note



Gyro setup and lasing beat-note



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Gyro pulling - response to cavity length change



Pulling drastically improved by mainly two factors

- Higher finesse $20 \rightarrow 70$
- Higher pumping powers

Higher pulling happens at D₂ detuning where lasing tends to stop

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Irina Novikova, Matt T. Simons, Joshua Hill, Hunter Rew (WM), Dmitry Budker, Simon Rochester (Rochester Scientific).

Eugeniy E. Mikhailov (W&M)

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Summary

- We demonstrated feasibility of fast laser
- Our laser has pulling factor exceeding 1
- We are working on the laser stabilization to demonstrate rotation sensitivity





Eugeniy E. Mikhailov (W&M)