# Towards fast-light gyroscope, modification of dispersion, and pulling sensitivity

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## Sagnac effect in interferometer



$$
t_{\pm} = \frac{2\pi R}{c} \left( 1 \pm \frac{R\Omega}{c} \right)
$$

$$
\Delta t = t_{+} - t_{-} = \frac{4\pi R^{2}\Omega}{c^{2}}
$$

$$
\Delta \phi = 2\pi \frac{c\Delta t}{\lambda} = \frac{8\pi A\Omega}{c\lambda}
$$

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## Sagnac effect and cavity response



 $\Delta p = c\Delta t = \frac{4A\Omega}{c}$ *c*  $Δf = f<sub>0</sub> \frac{Δp}{p}$ *p* 1  $\frac{1}{n_g} = \Delta f_{empty} \frac{1}{n_g}$ *ng*

Group index

$$
n_g(f) = n + f_0 \frac{\partial n}{\partial f}
$$

Cavity response enhanced if  $n_q < 1$  i.e. under the fast light condition Shahriar et al., PRA **75**, 053807 (2007)





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## N-scheme, with forbidden transition - fast but no gain



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4 0 8 1

 $\mathbf{A} \oplus \mathbf{B}$   $\mathbf{B} \oplus \mathbf{A}$   $\oplus \mathbf{B}$ 

 $\epsilon$ 舌

## N-bar with four-wave mixing - fast and with gain



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4 0 8 1

 $\mathbf{A} \cap \mathbf{B}$   $\mathbf{B}$   $\mathbf{A} \cap \mathbf{B}$   $\mathbf{B}$ 

 $\epsilon$ 舌

# N-bar with four-wave mixing - optimal parameters



N. B. Phillips, *et al.* Journal of Modern Optics, Issues 1, 60, 64-72, (2013).

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## N-bar with Doppler averaging



### N-bar field competition

 $\Omega_4=0$ 

$$
\Omega_4=\Omega_2/2
$$

$$
\Omega_4=\Omega_2
$$

4 0 8

 $\triangleleft$ 

 $\mathcal{A}$ ∍



## N-bar beam propagation









### N-bar beam propagation







4 0 8

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# N-bar scheme linearly polarized pumps - single pass



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# Gyro lasing - no fast light condition



#### Lasing conditions

- round trip gain is 1
- round trip phase shift is 0

### Simulation parameters

- $N = 9.6 \times 10^{10}$  1/cm<sup>3</sup>
- $\delta_1 = -2\pi \times 800$  MHz
- $\delta_3 = 0$  MHz
- $\Omega_1 = 6$  mW/cm<sup>2</sup>
- $\Omega_3 = 10$  mW/cm<sup>2</sup>
- $\bullet$  Finesse = 18

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# Gyro lasing - fast light condition, single frequency



#### Lasing conditions

- round trip gain is 1
- round trip phase shift is 0

### Simulation parameters

- $N = 4.8 \times 10^{10}$  1/cm<sup>3</sup>
- $\delta_1 = 0$  MHz
- $\delta_3 = 0$  MHz
- $\Omega_1 = 48.2$  mW/cm<sup>2</sup>
- $\Omega$ <sub>3</sub> = 192.9 mW/cm<sup>2</sup>
- $\bullet$  Finesse = 60

∆*f* = 150∆*fempty*.*cavity*

<span id="page-14-0"></span> $QQ$ 

# Gyro lasing - fast light condition, multiple frequencies



#### Lasing conditions

- round trip gain is 1
- round trip phase shift is 0

#### Simulation parameters

•  $N = 4.8 \times 10^{10}$  1/cm<sup>3</sup>

$$
\bullet\ \delta_1=0\ \text{MHz}
$$

- $\delta_3 = 0$  MHz
- $\Omega_1=$  50.6 mW/cm $^2$ , 5% higher
- $\Omega_3 = 192.9$  mW/cm<sup>2</sup>
- <span id="page-15-0"></span> $\bullet$  Finesse = 60

#### Multiple lazing points might be problematic in t[he](#page-14-0) [e](#page-16-0)[x](#page-14-0)[pe](#page-15-0)[r](#page-16-0)[i](#page-12-0)[m](#page-13-0)[e](#page-15-0)[n](#page-16-0)[t](#page-12-0)

## First gyro setup and its performance



 $\Omega_2$  tuned around  $\mathcal{F}=1 \rightarrow \mathcal{F}'=1,2$ 

<span id="page-16-0"></span> $\leftarrow$   $\Box$  $\mathbf{p}_i$  $\rightarrow$   $\pm$   $\rightarrow$ 

4 D.K.

## First gyro setup and its performance



E. Mikhailov, *et al.* Optical Engineering, Issue 10, 53, 102709, (2014)

 $\Omega$ 

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## Gyro setup and lasing beat-note



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## Gyro setup and lasing beat-note



4 0 8

**D** 

# Gyro pulling - response to cavity length change



Pulling drastically improved by mainly two factors

- $\bullet$  Higher finesse 20  $\rightarrow$  70
- <span id="page-21-0"></span>• Higher pumping powers

Higher pulling happens at  $D_2$ detuning where lasing tends to stop



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# Summary

- We demonstrated feasibility of fast laser
- Our laser has pulling factor exceeding 1
- We are working on the laser stabilization to demonstrate rotation sensitivity



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