

# Quantum-enhanced measurements and fast squeezing with atomic vapor

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The College of William & Mary, USA



SPIE, February 03, 2014

# People

Travis Horrom and Gleb Romanov



Irina Novikova



# People

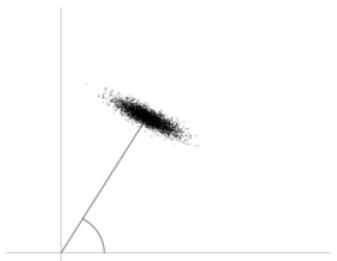
Travis Horrom and Gleb Romanov



Irina Novikova

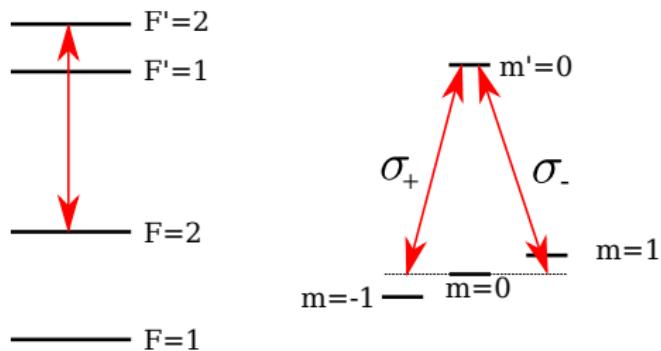


Squeezed state

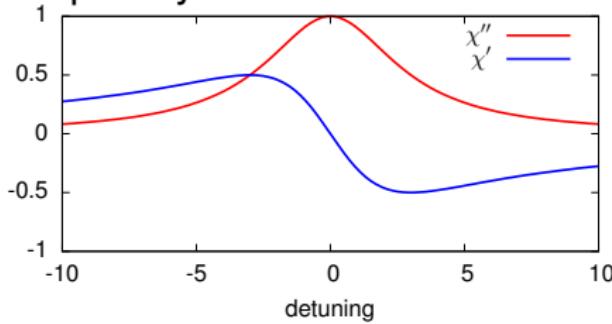


# Optical magnetometer based on Faraday effect

$^{87}\text{Rb}$  D<sub>1</sub> line

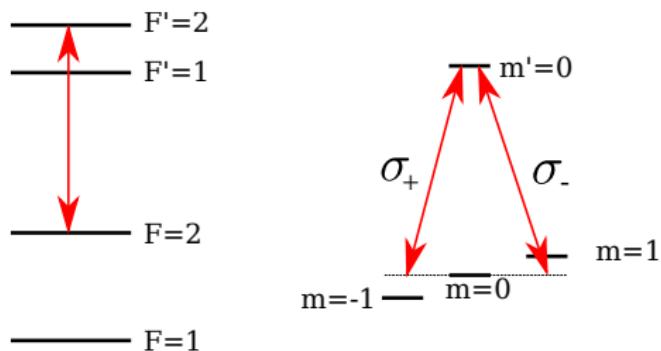


Susceptibility vs B

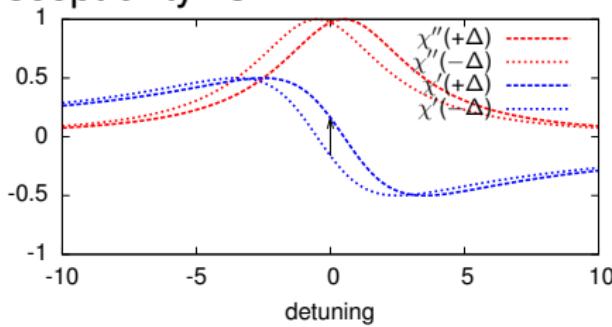


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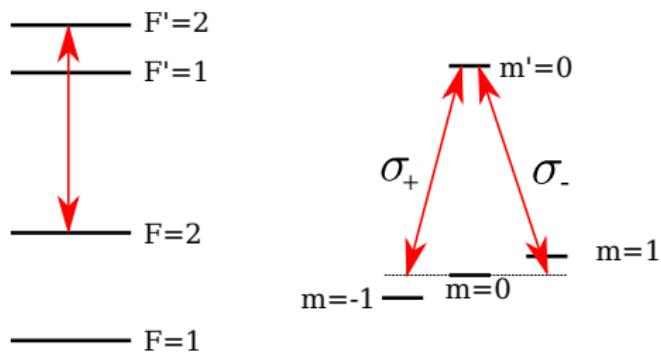


Susceptibility vs B

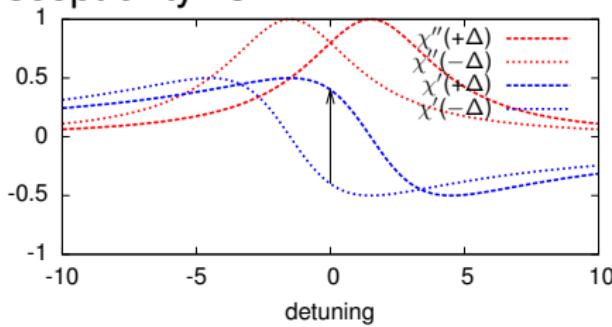


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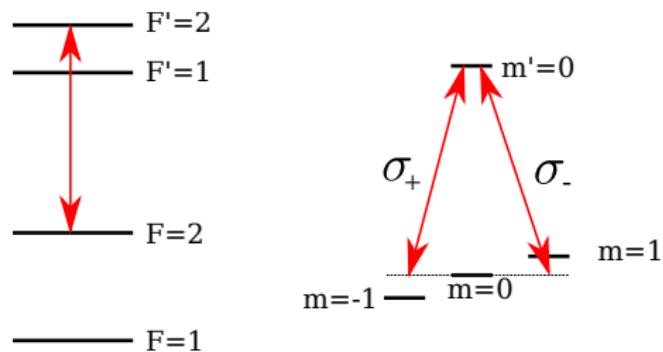


Susceptibility vs B

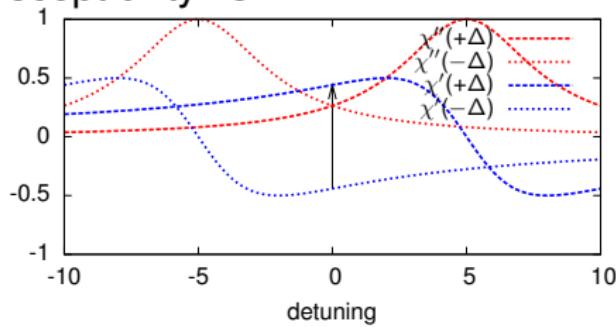


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$^{87}\text{Rb}$  D<sub>1</sub> line

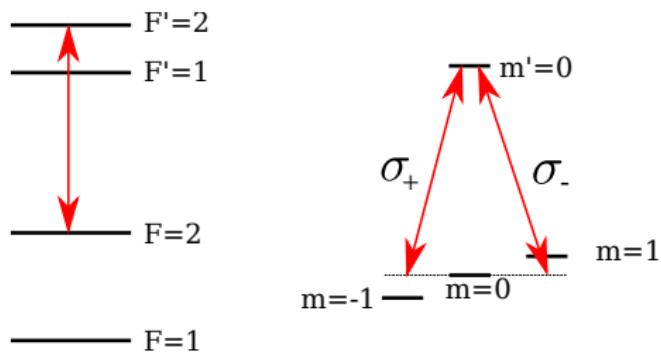


Susceptibility vs B

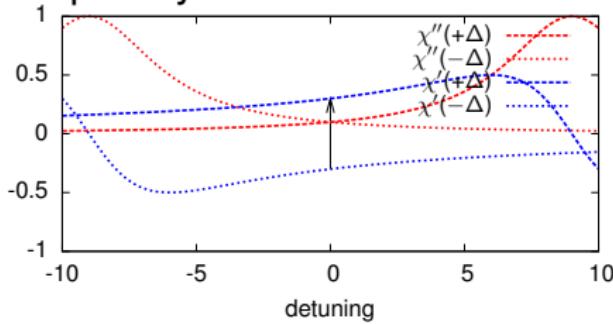


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$^{87}\text{Rb}$  D<sub>1</sub> line

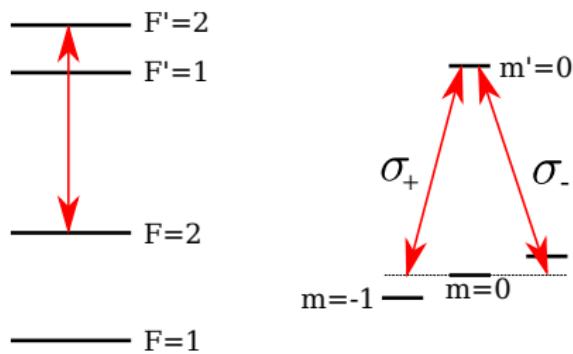


Susceptibility vs B

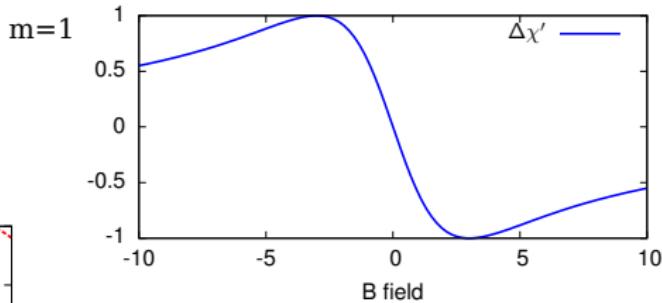


# Optical magnetometer based on Faraday effect

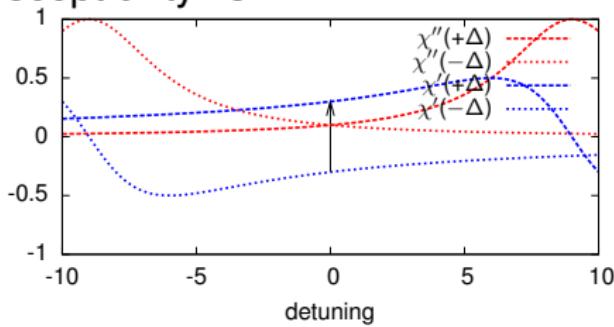
$^{87}\text{Rb}$  D<sub>1</sub> line



Polarization rotation vs B



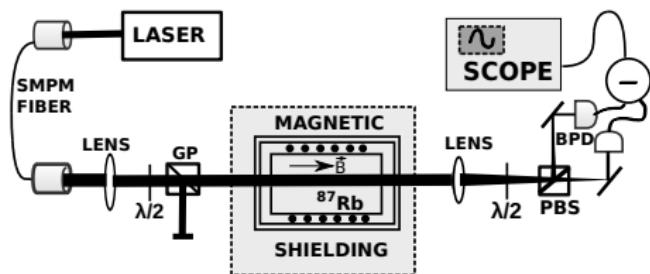
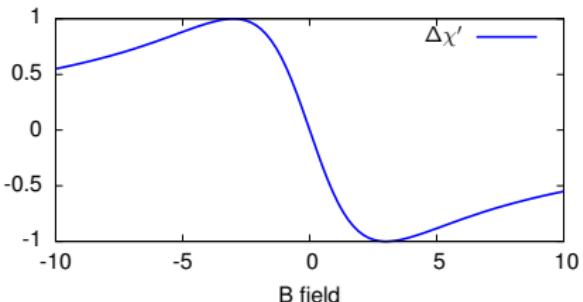
Susceptibility vs B



# Optical magnetometer and non linear Faraday effect

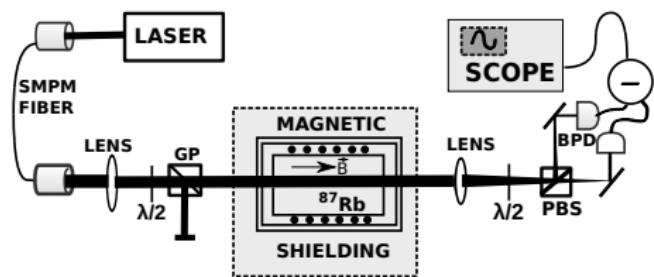
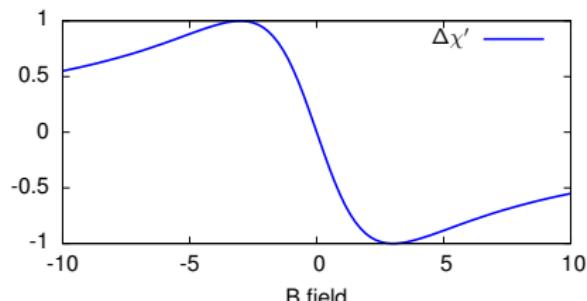
Naive model of rotation

Experiment

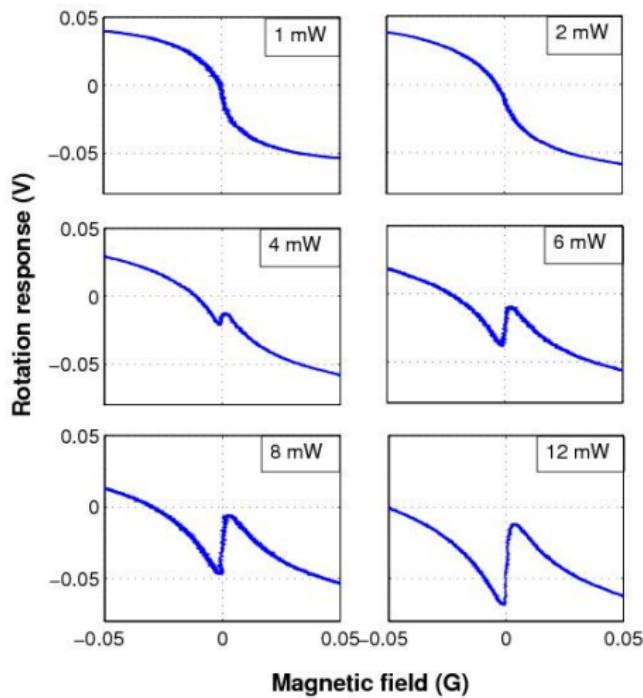


# Optical magnetometer and non linear Faraday effect

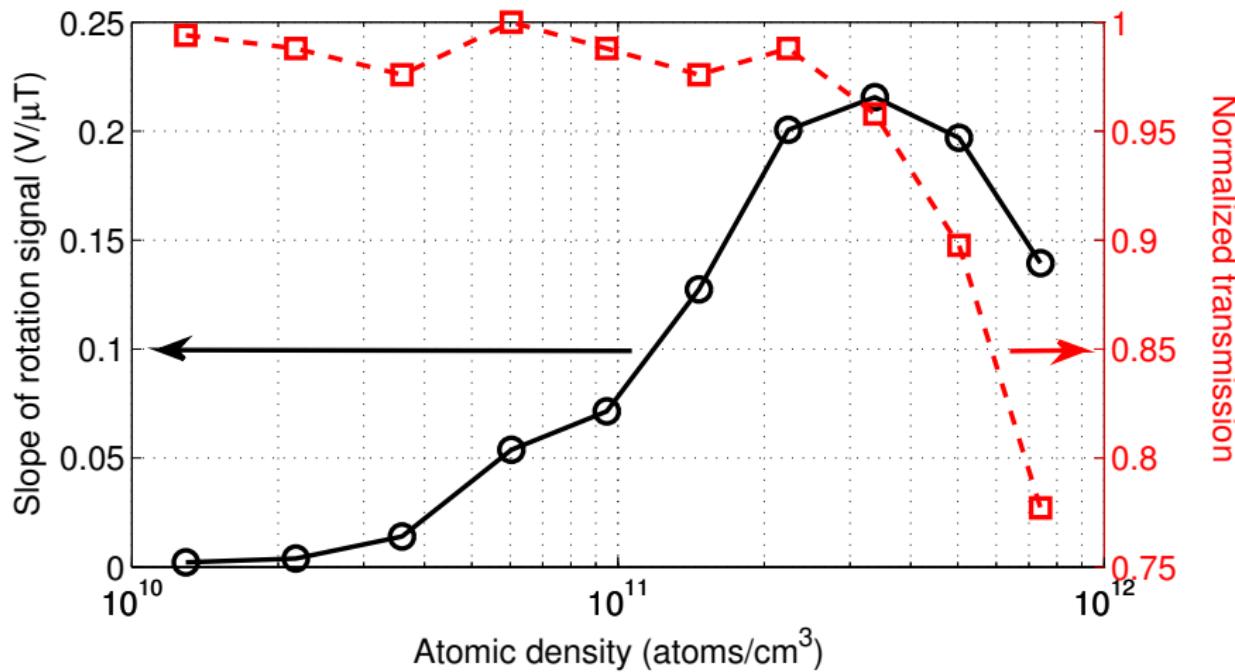
## Naive model of rotation



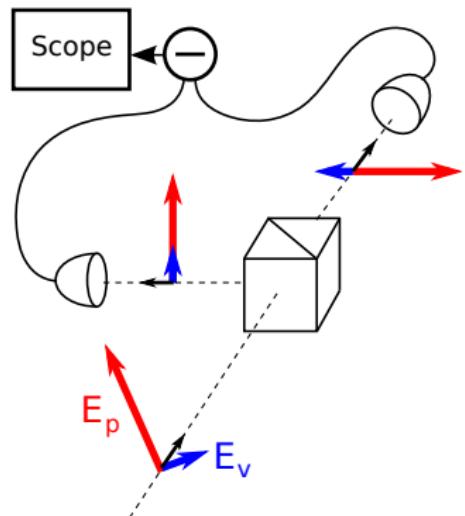
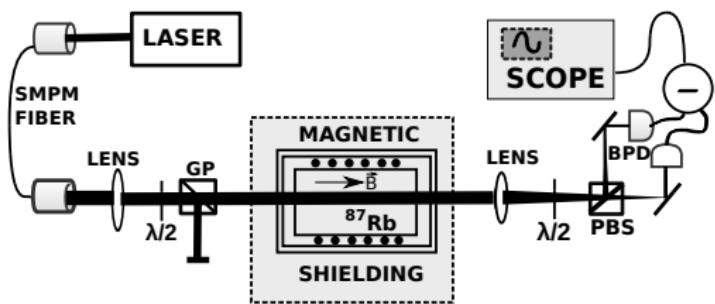
## Experiment



# Magnetometer response vs atomic density



# Shot noise limit of the magnetometer



$$S = |E_p + E_v|^2 - |E_p - E_v|^2$$

$$S = 4E_p E_v$$

$$\langle \Delta S \rangle \sim E_p \langle \Delta E_v \rangle$$

# Heisenberg uncertainty principle and its optics equivalent



## Heisenberg uncertainty principle

$$\Delta p \Delta x \geq \hbar/2$$

The more precisely the POSITION is determined, the less precisely the MOMENTUM is known, and vice versa

## Optics equivalent

$$\Delta\phi \Delta N \geq 1$$

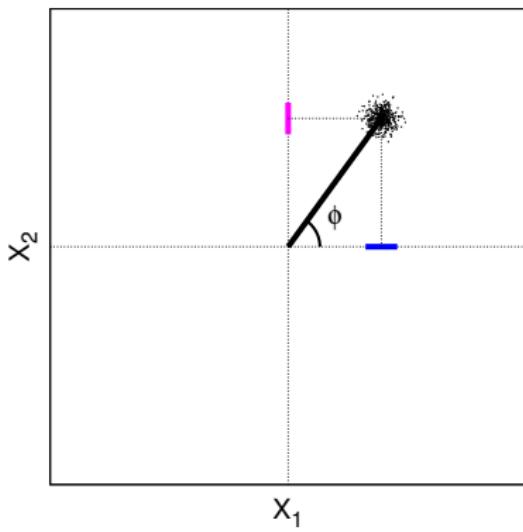
The more precisely the PHASE is determined, the less precisely the AMPLITUDE is known, and vice versa

## Optics equivalent strict definition

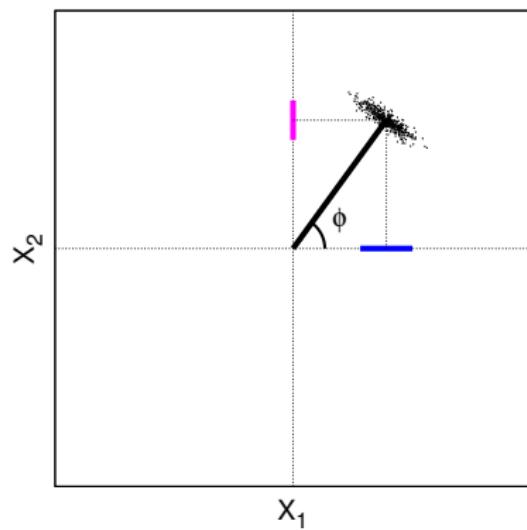
$$\Delta X_1 \Delta X_2 \geq 1/4$$

# Minimum uncertainty (coherent) states

Coherent state



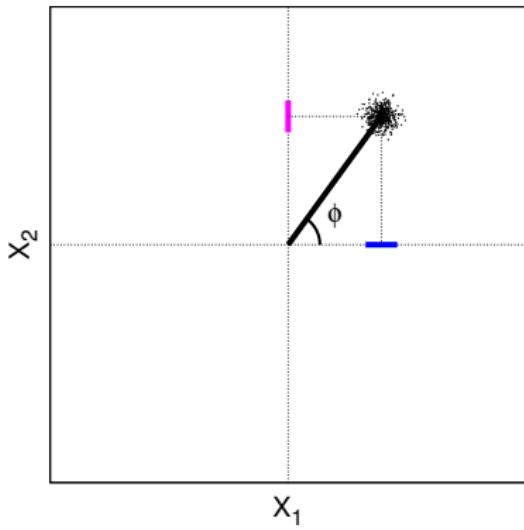
Squeezed state



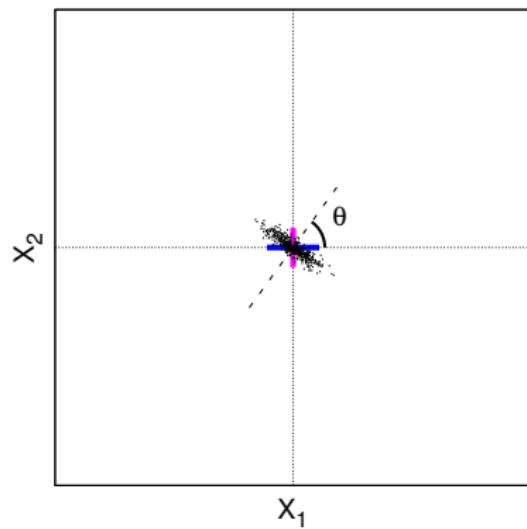
$$\Delta \textcolor{blue}{X}_1 \Delta \textcolor{magenta}{X}_2 \geq 1/4$$

# Minimum uncertainty (coherent) states

Coherent state

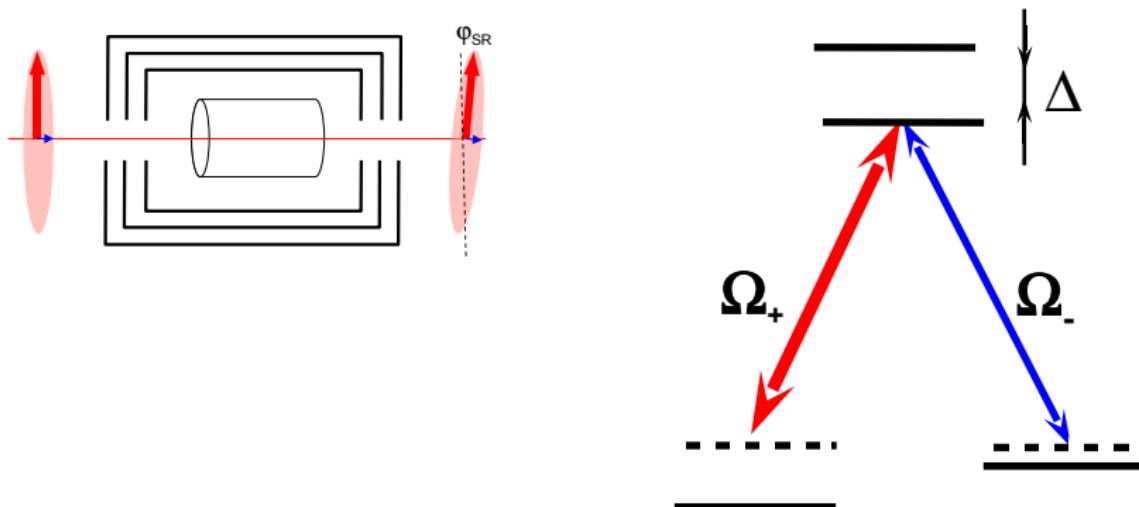


Squeezed state



$$\Delta \textcolor{blue}{x}_1 \Delta \textcolor{magenta}{x}_2 \geq 1/4$$

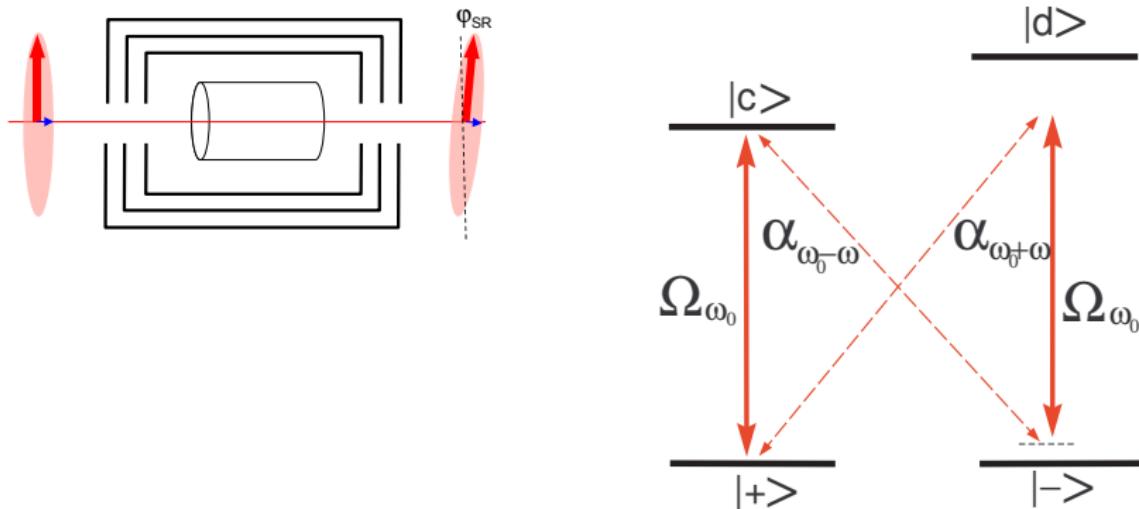
# Self-rotation of elliptical polarization in atomic medium



A.B. Matsko et al., PRA 66, 043815 (2002): theoretically prediction of 4-6 dB noise suppression

$$a_{out} = a_{in} + \frac{igL}{2}(a_{in}^\dagger - a_{in})$$

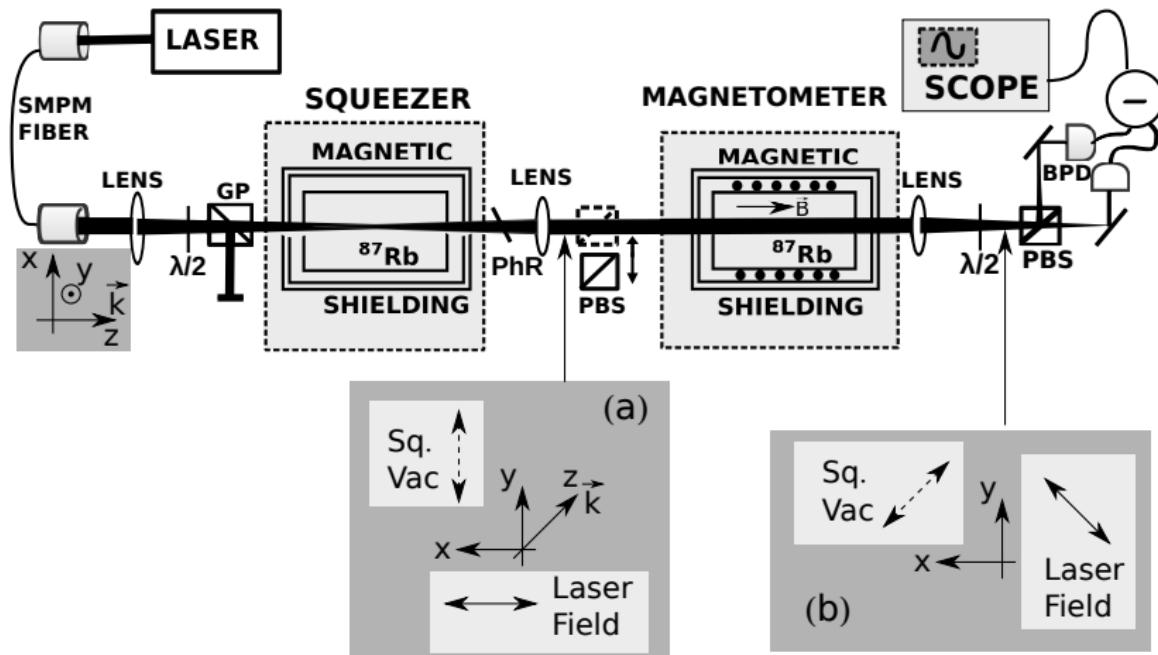
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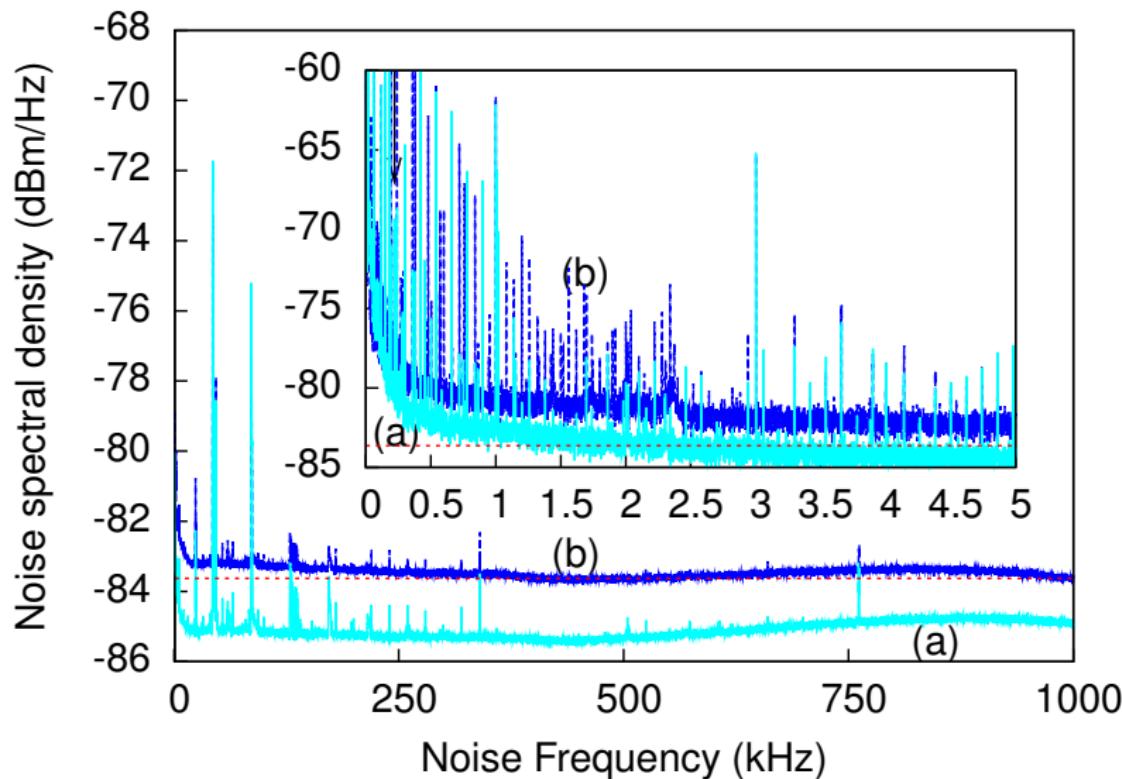
$$a_{out} = a_{in} + \frac{igL}{2}(a_{in}^\dagger - a_{in})$$

# Squeezed enhanced magnetometer setup

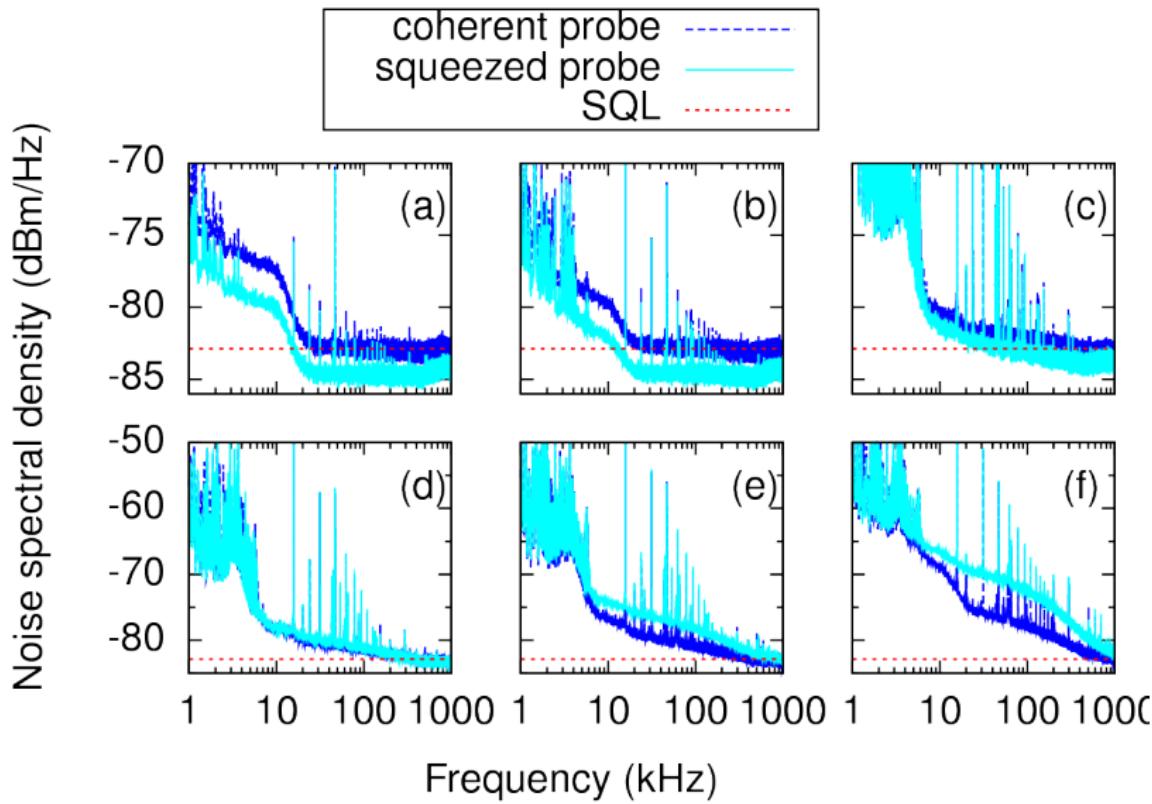


Note: Squeezed enhanced magnetometer was first demonstrated by Wolfgramm *et. al* Phys. Rev. Lett, **105**, 053601, 2010.

# Magnetometer noise floor improvements

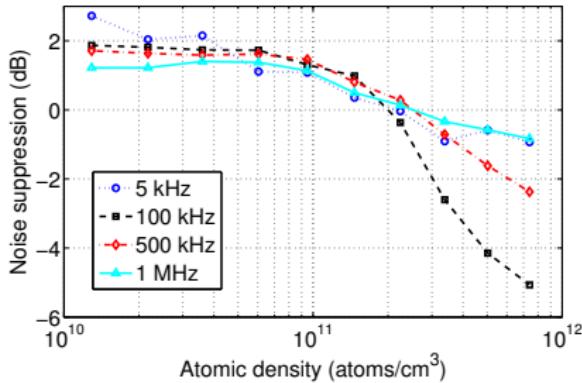


## Magnetometer noise spectra

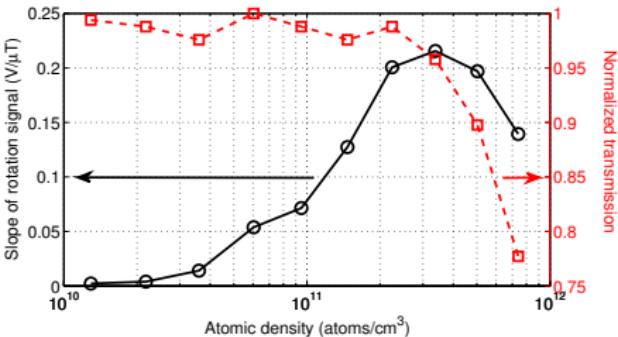


# Noise suppression and response vs atomic density

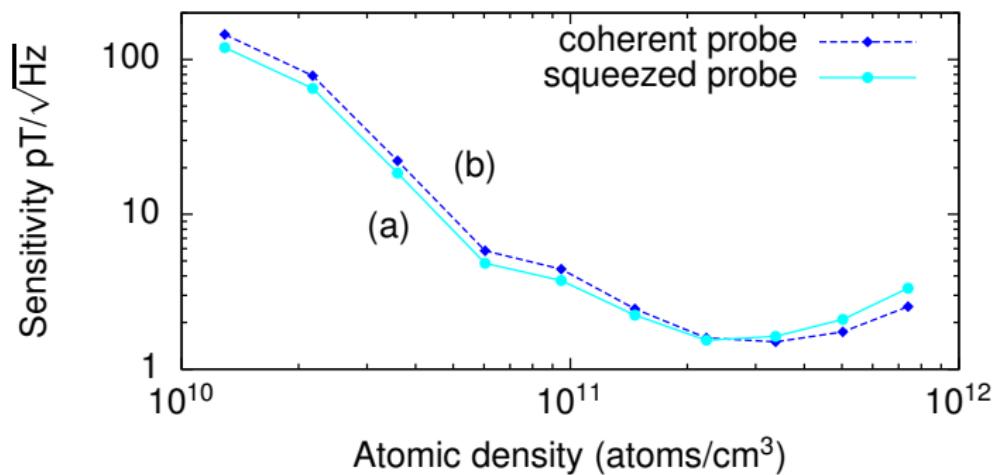
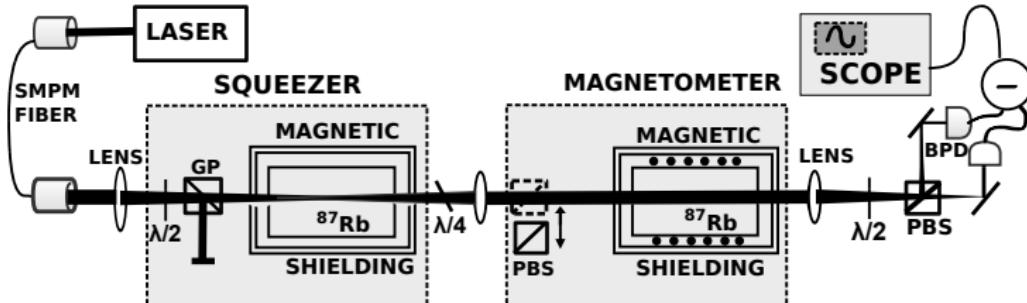
## Noise suppression



## Response



# Magnetometer with squeezing enhancement



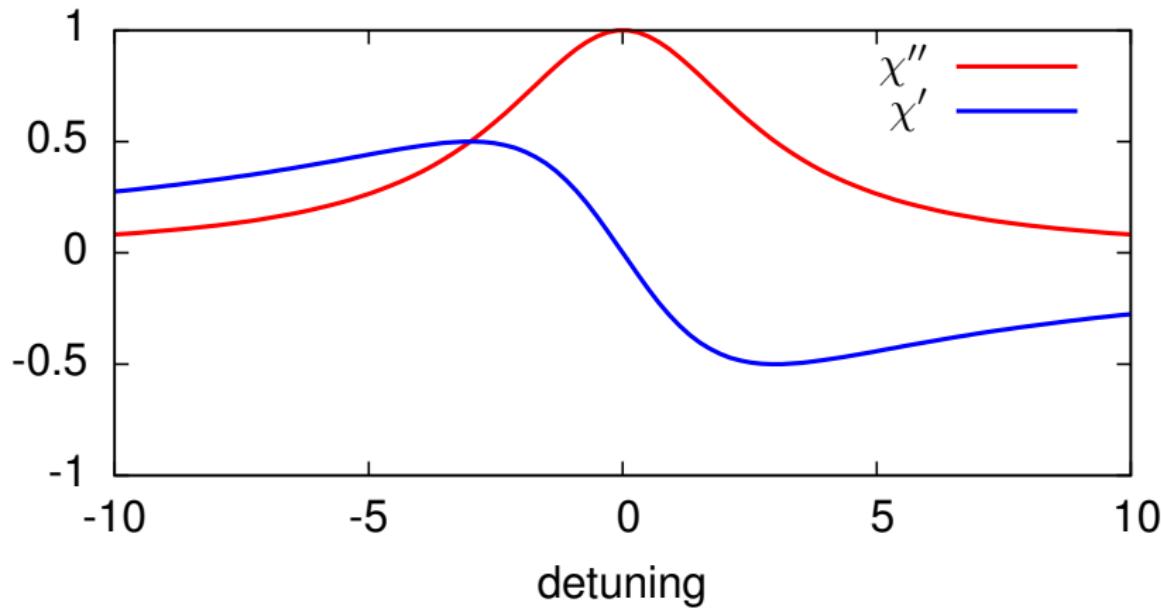
# Why superluminal squeezing?

- Quantum memories
- M. S. Shahriar, et al. “Ultrahigh enhancement in absolute and relative rotation sensing using fast and slow light”, Phys. Rev. A 75(5), 053807, 2007.
- R. W. Boyd, et al. “Noise properties of propagation through slow- and fast- light media”, Journal of Optics **12**, 104007 (2010).

# Light group velocity

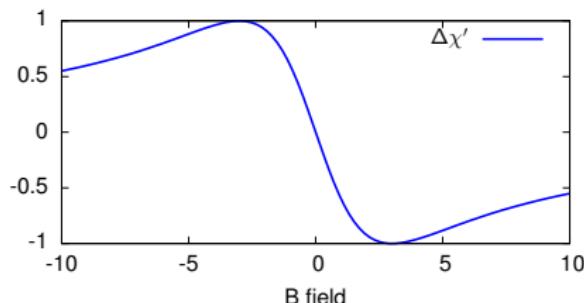
$$\text{Group velocity } v_g = \frac{c}{\omega \frac{\partial n}{\partial \omega}}$$

Susceptibility

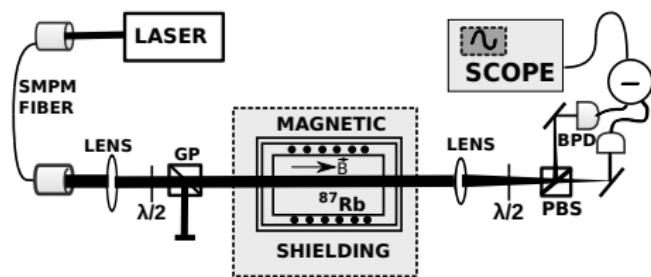
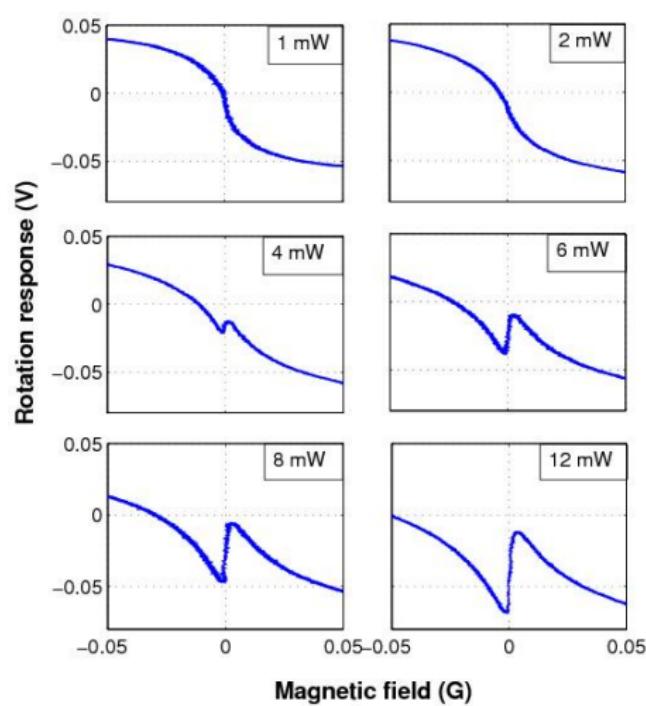


# Susceptibility and non linear Faraday effect

## Naive model of rotation



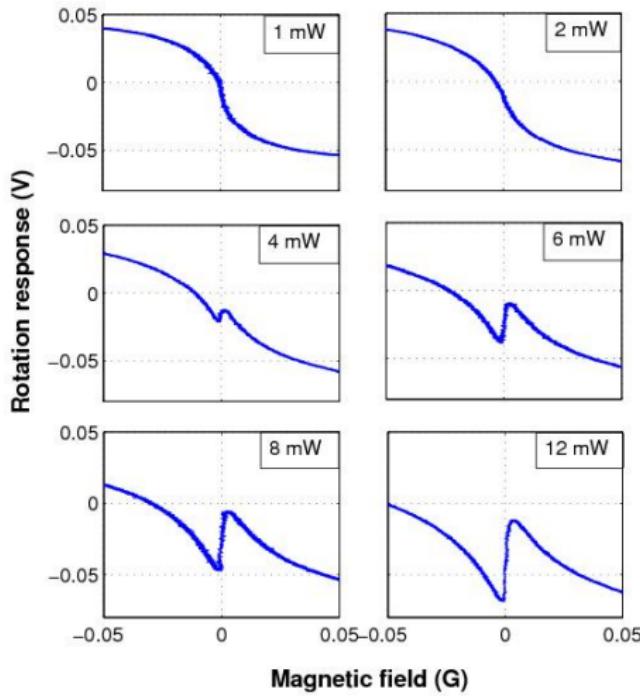
## Experiment



# Light group velocity

$$\text{Group velocity } v_g = \frac{c}{\omega \frac{\partial n}{\partial \omega}}$$

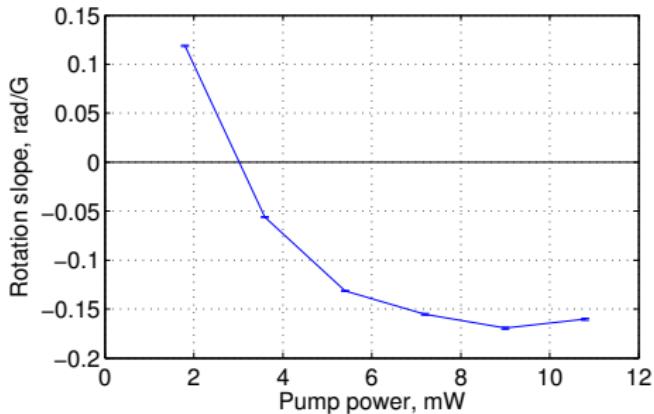
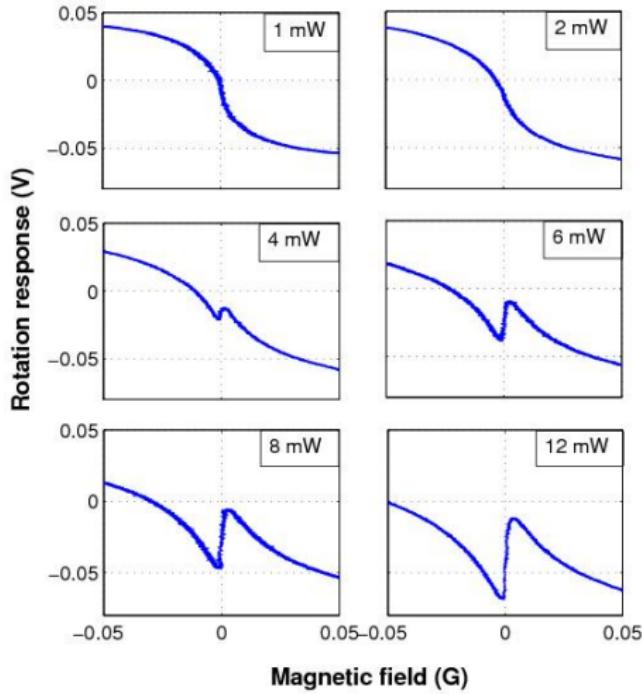
$$\text{Delay } \tau = \frac{L}{v_g} \sim \frac{\partial n}{\partial \omega} \sim \frac{\partial R}{\partial B}$$



# Light group velocity

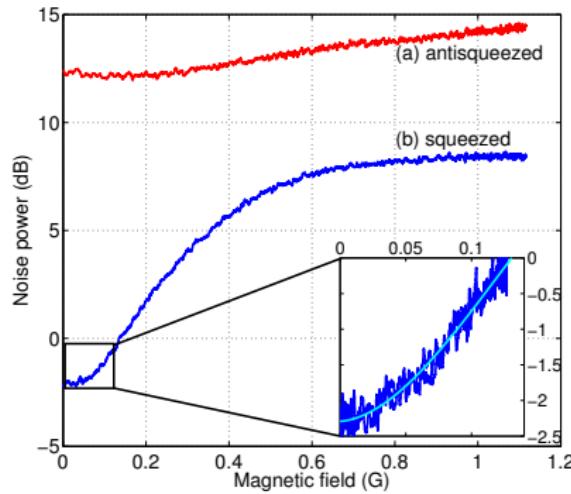
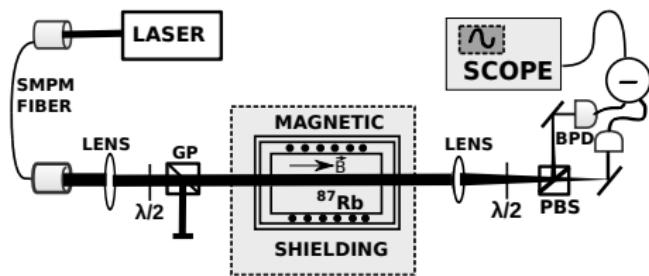
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# Squeezing vs magnetic field

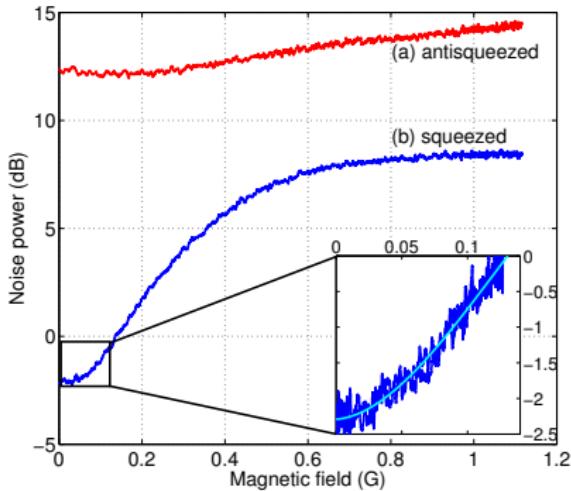
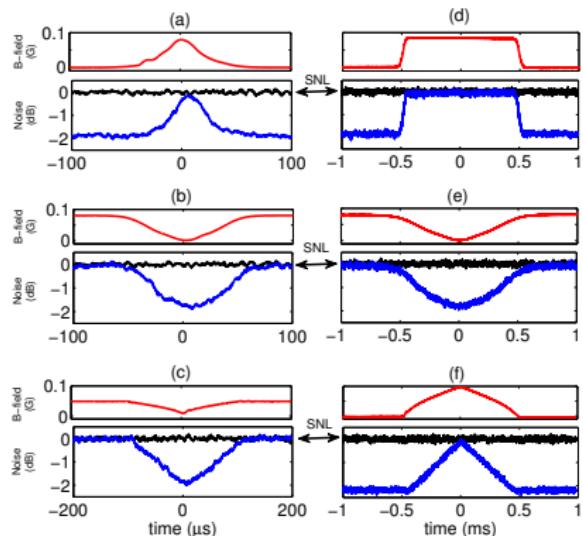
Spectrum analyzer settings: Central frequency = 1 MHz, VBW = 3 MHz, RBW = 100 kHz



Travis Horrom et al. "All-atomic source of squeezed vacuum with full pulse-shape control", Journal of Physics B: Atomic, Molecular and Optical Physics, Issue 12, 45, 124015, (2012).

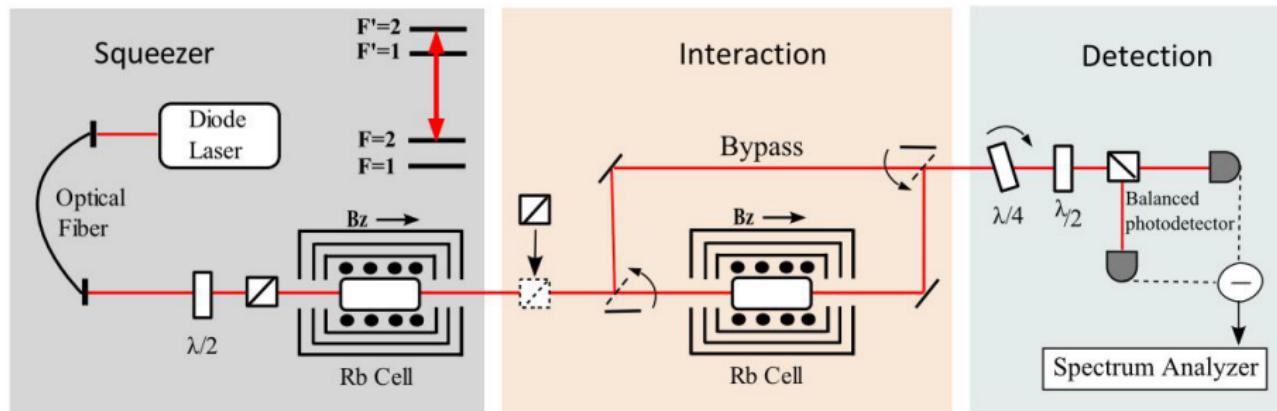
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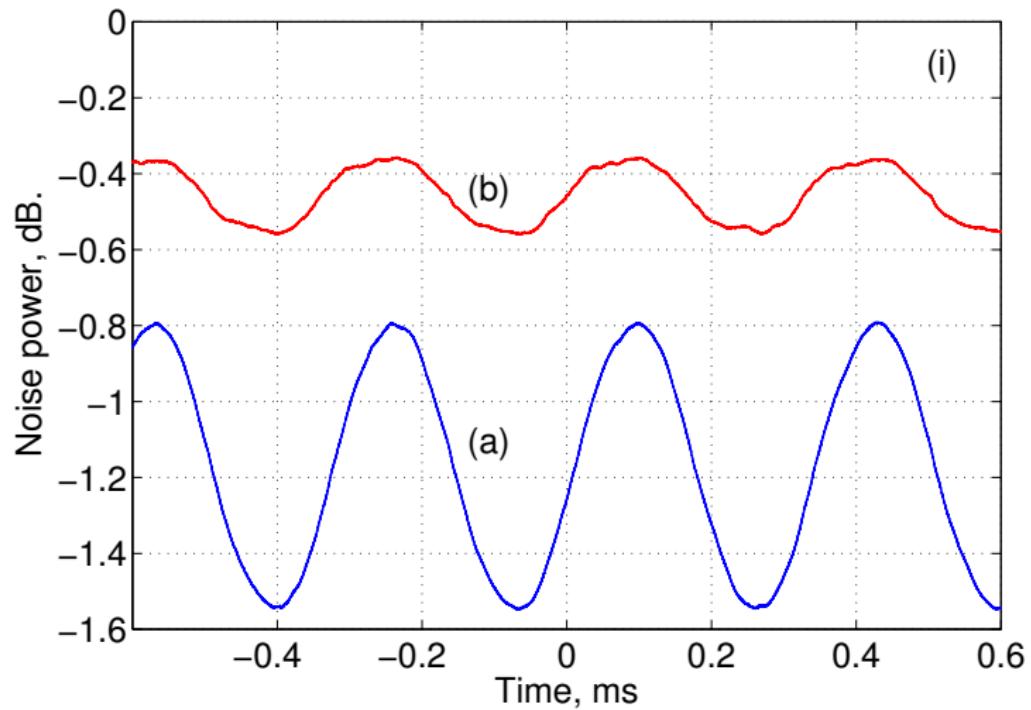


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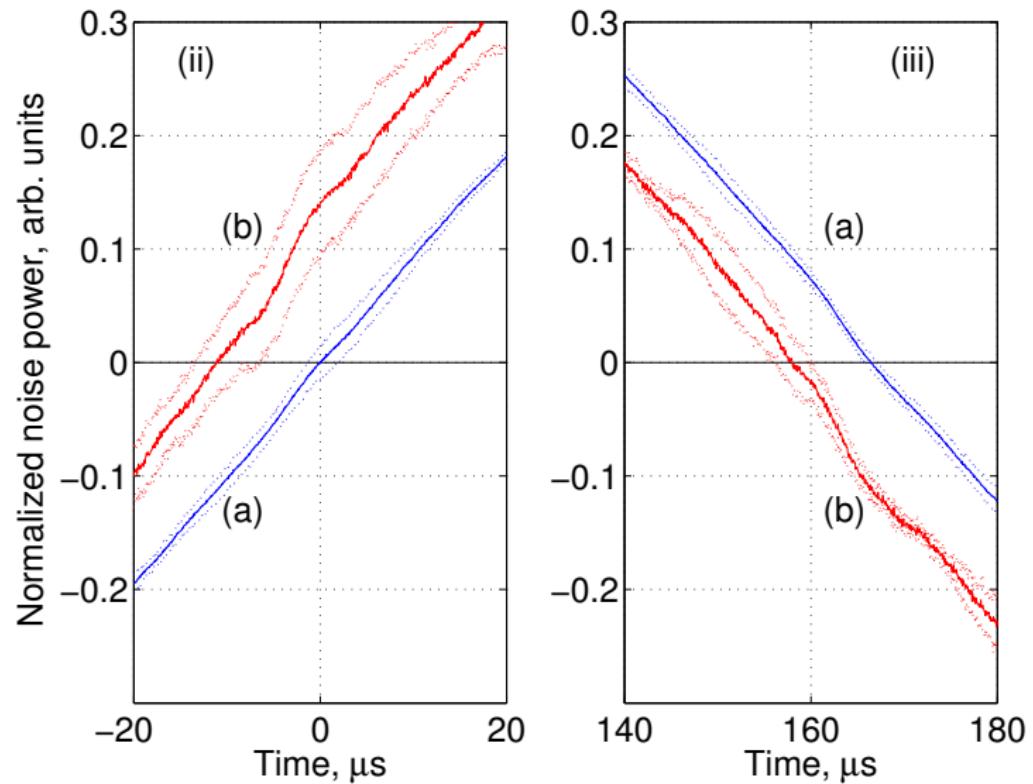
# Time advancement setup



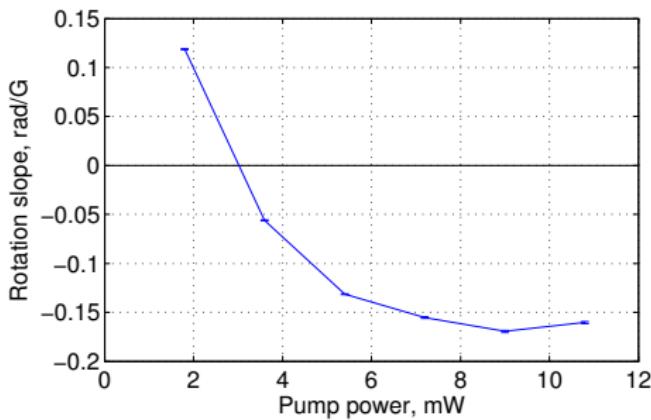
# Squeezing modulation and time advancement



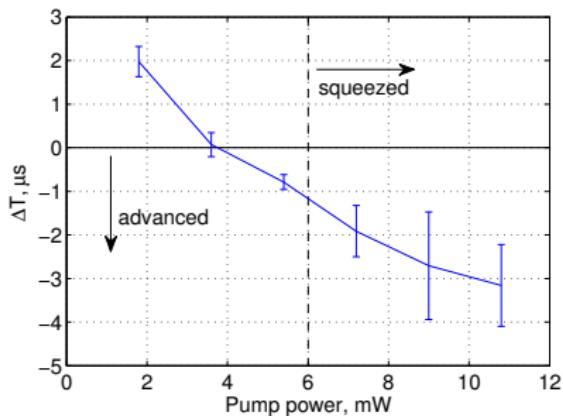
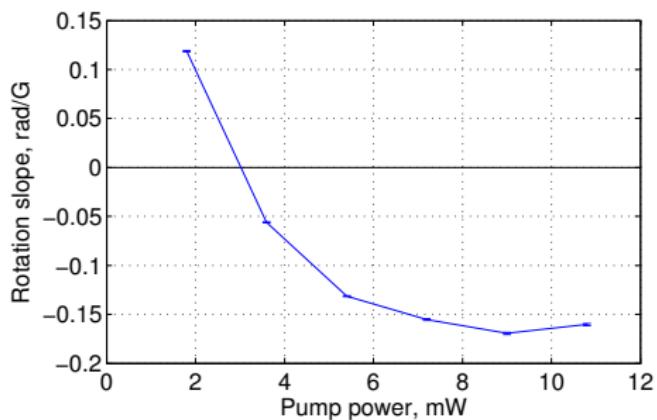
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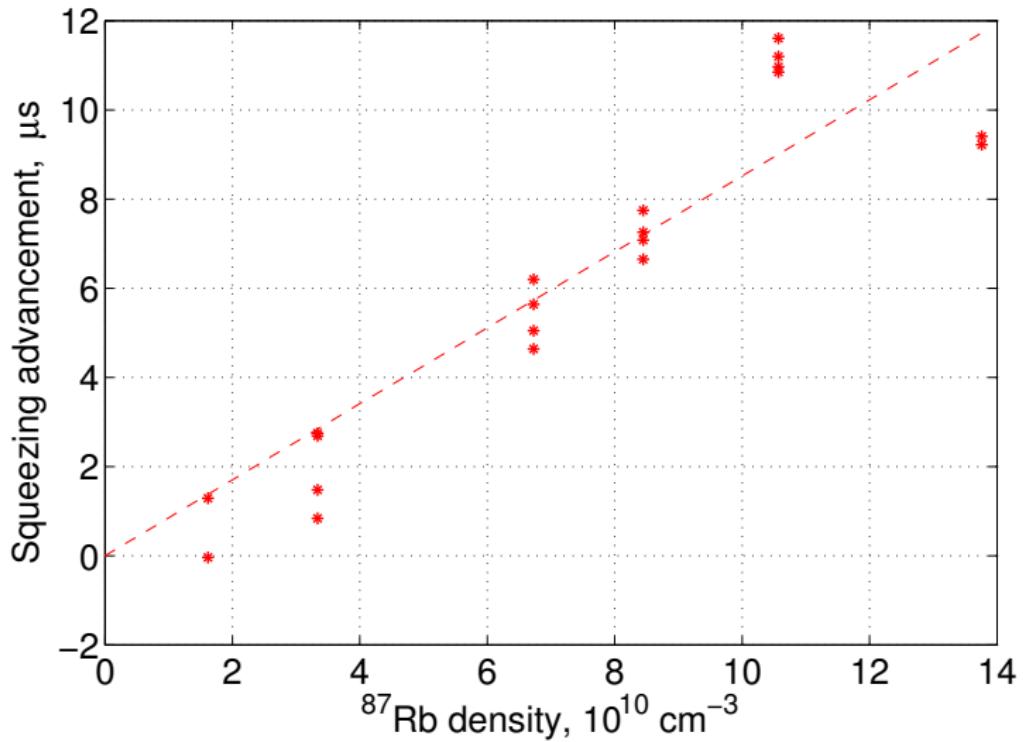
# Advancement vs power



# Advancement vs power



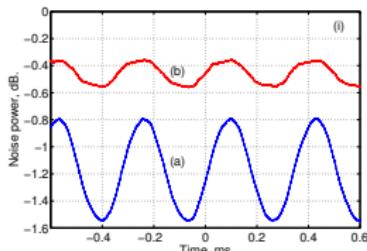
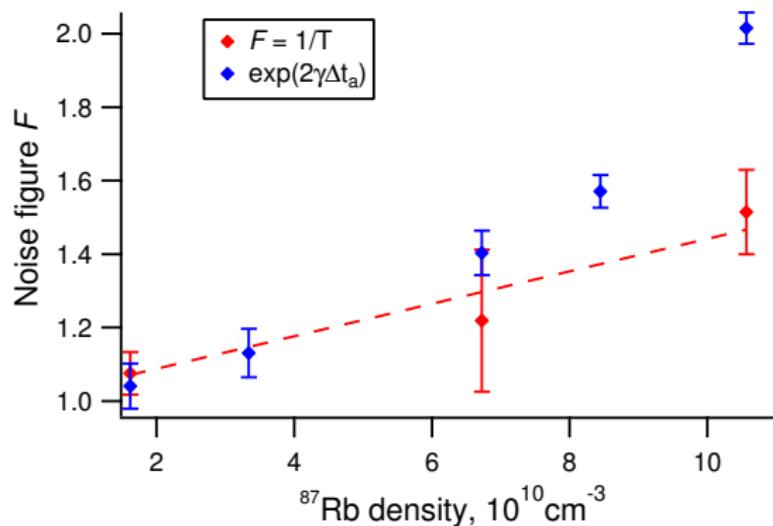
# Squeezing advancement vs atomic density



# Noise figure and advancement

R. W. Boyd, et al. "Noise properties of propagation through slow- and fast-light media", Journal of Optics **12**, 104007 (2010).

$$F = \frac{SNR_{in}}{SNR_{out}} = 1/T = e^{2\gamma\Delta t_a}$$



# Summary

- We demonstrate fully atomic squeezed enhanced magnetometer with sensitivity as low as  $1 \text{ pT}/\sqrt{\text{Hz}}$
- superluminal squeezing propagation with  $v_g \approx -7'000 \text{ m/s}$   
 $\approx -c/43'000$  or time advancement of  $11 \mu\text{s}$

For more details:

- T. Horrom, et al. "Quantum Enhanced Magnetometer with Low Frequency Squeezing", **PRA**, 86, 023803, (2012).
- G. Romanov, et al. "Propagation of a squeezed optical field in a medium with superluminal group velocity", arXiv:1310.4815, (2013). *To appear in Optics Letters*

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