

# Quantum enhanced magnetometry and resonant squeezing interaction with atoms

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Travis Horrom, Gleb Romanov, and Irina Novikova

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PQE, January 10, 2013

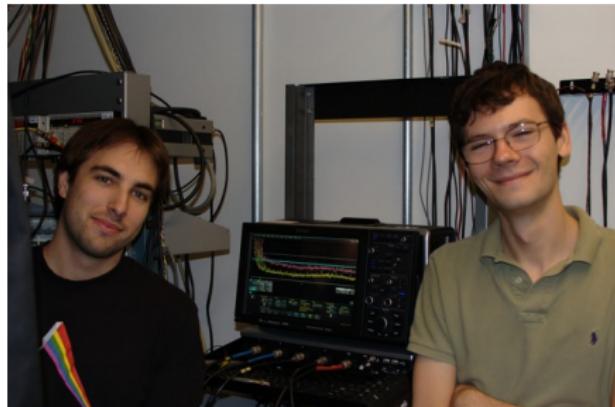
# People

Irina Novikova, W&M

Robinjeet Singh, LSU

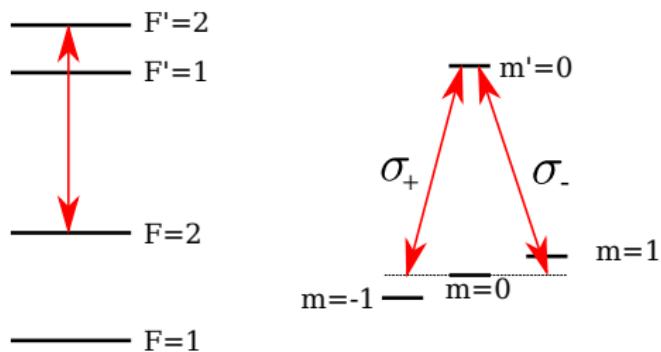


Travis Horrom and Gleb Romanov, W&M

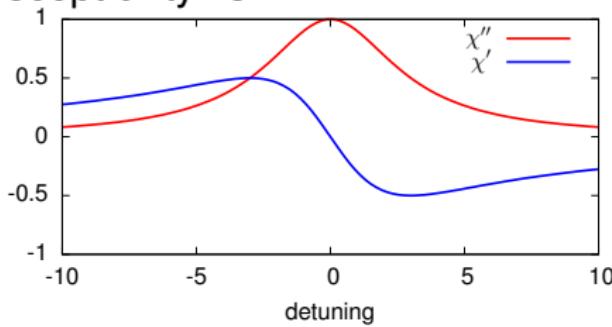


# Optical magnetometer based on Faraday effect

$^{87}\text{Rb}$  D<sub>1</sub> line

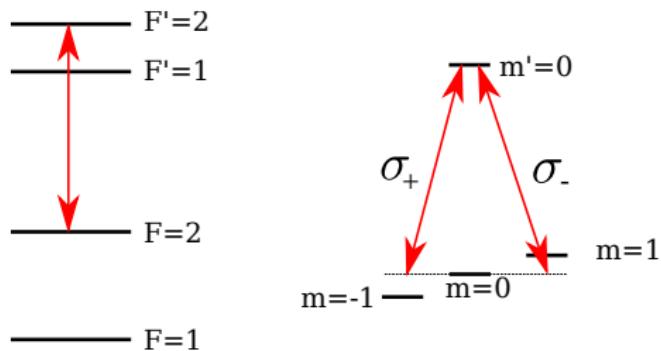


Susceptibility vs B

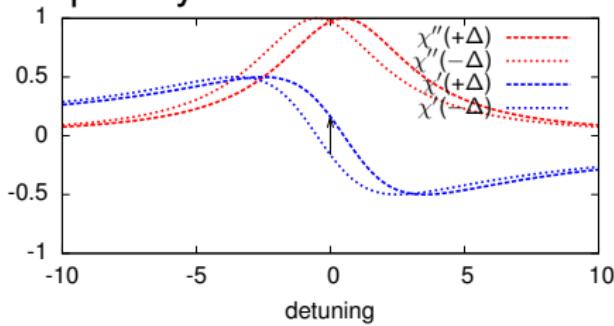


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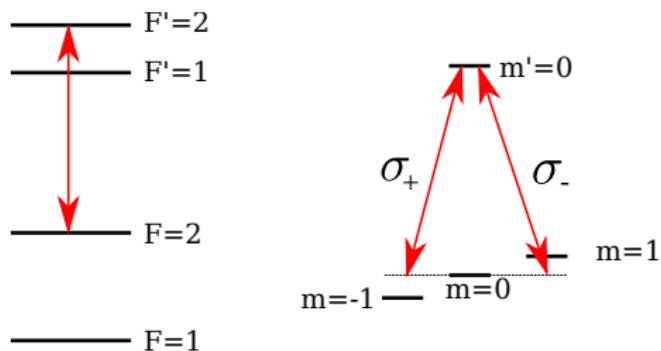


Susceptibility vs B

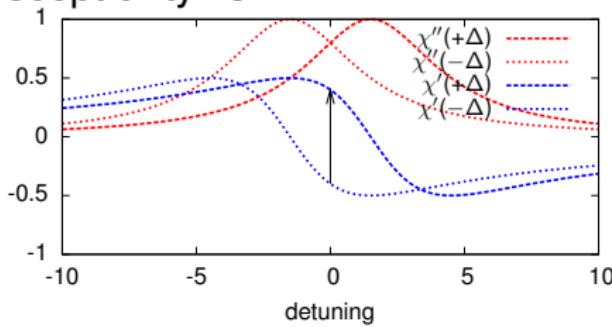


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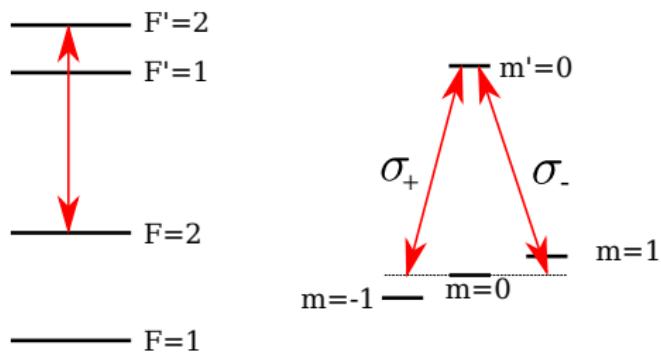


Susceptibility vs B

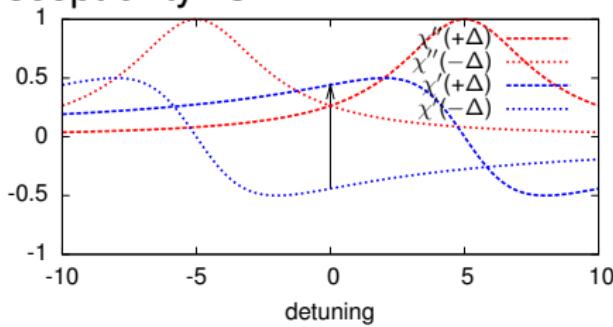


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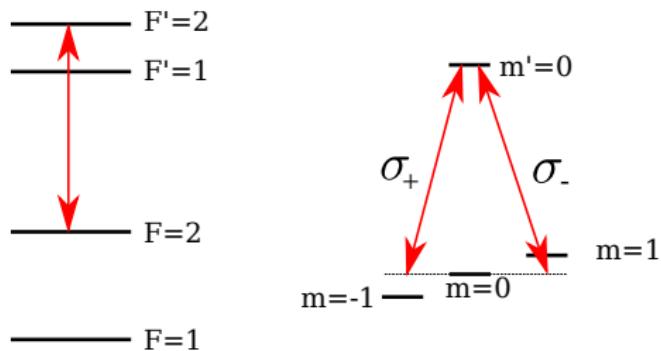


Susceptibility vs B

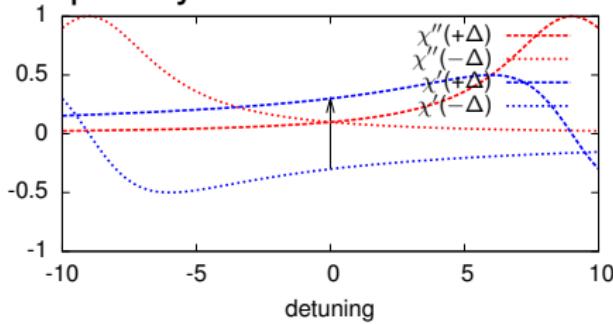


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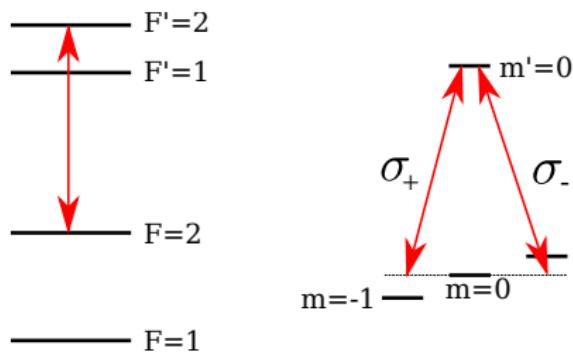


Susceptibility vs B

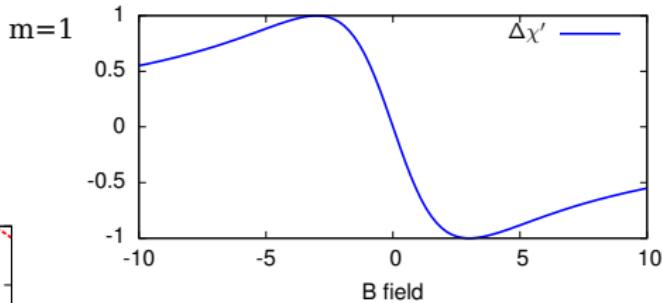


# Optical magnetometer based on Faraday effect

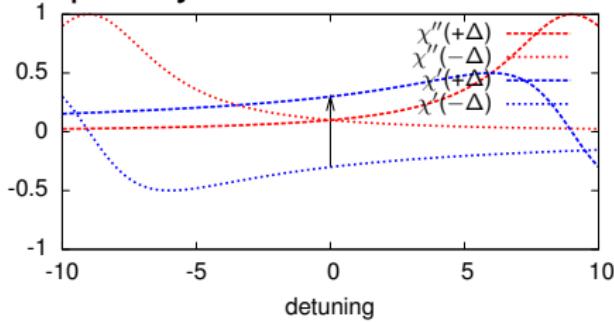
$^{87}\text{Rb}$  D<sub>1</sub> line



Polarization rotation vs B



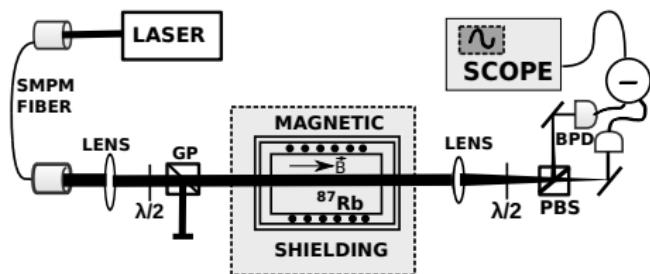
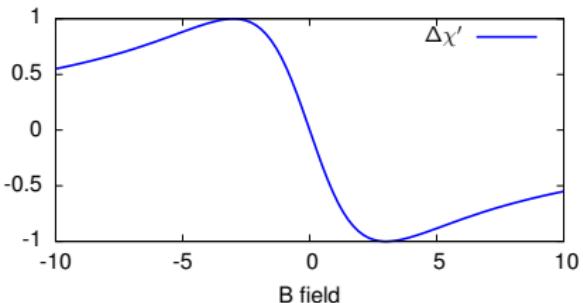
Susceptibility vs B



# Optical magnetometer and non linear Faraday effect

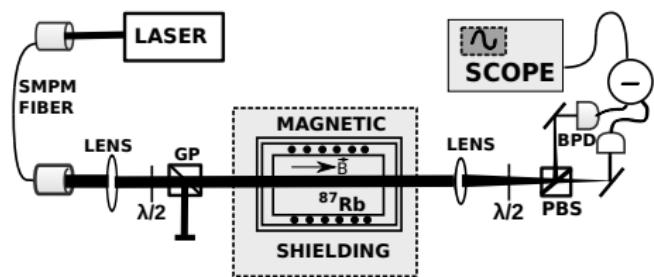
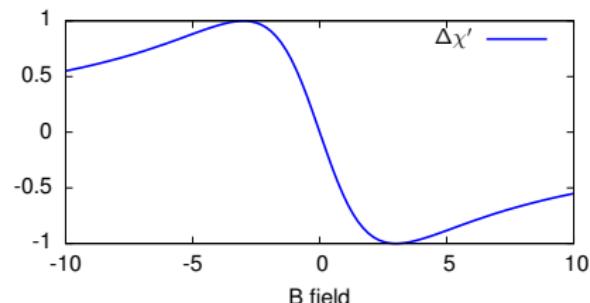
Naive model of rotation

Experiment

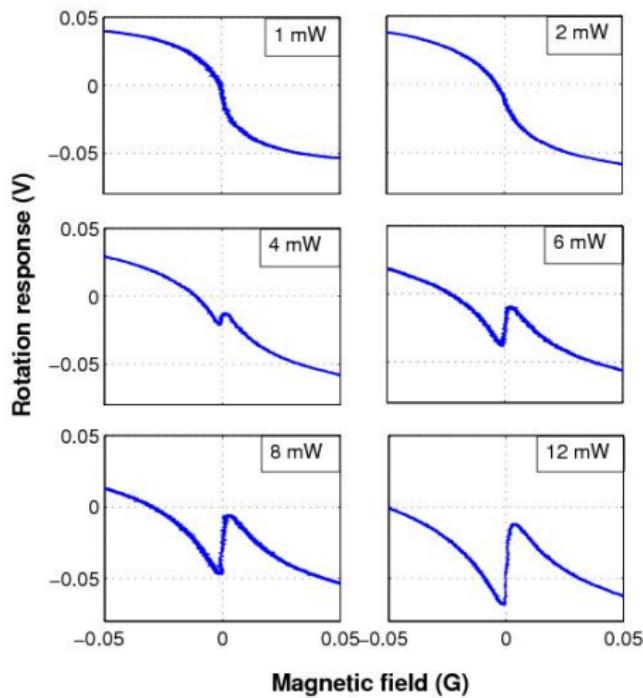


# Optical magnetometer and non linear Faraday effect

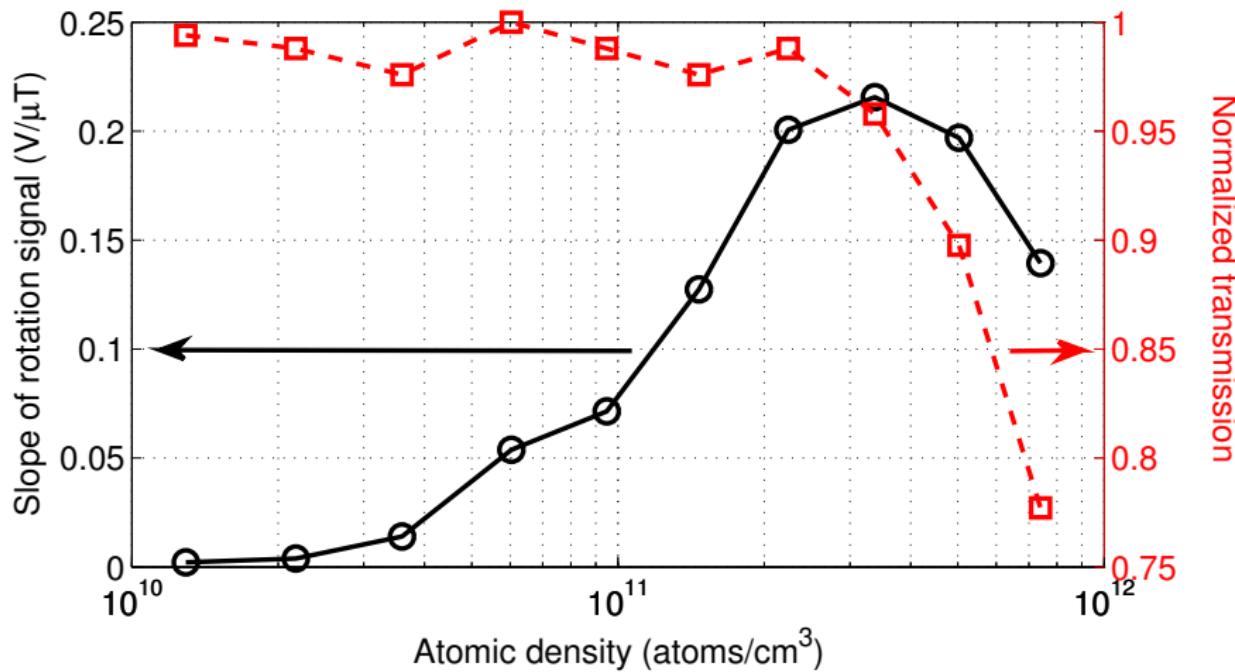
## Naive model of rotation



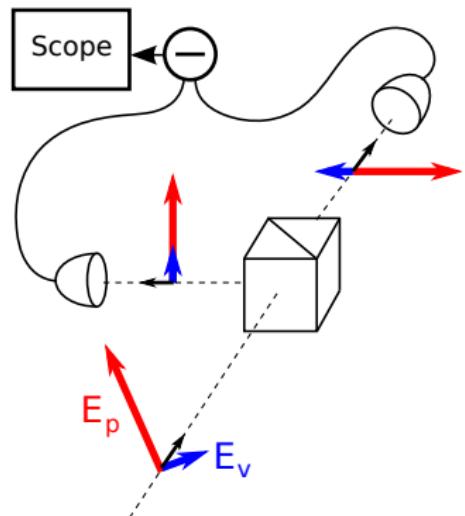
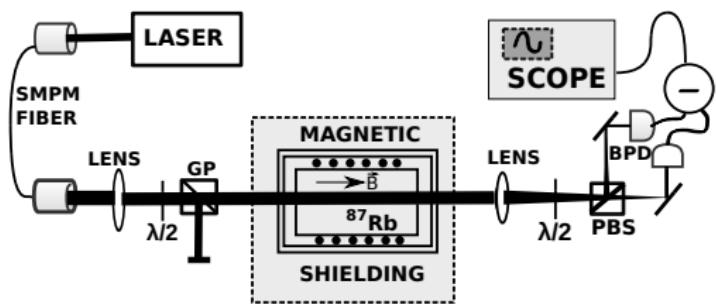
## Experiment



# Magnetometer response vs atomic density



# Shot noise limit of the magnetometer



$$S = |E_p + E_v|^2 - |E_p - E_v|^2$$

$$S = 4E_p E_v$$

$$\langle \Delta S \rangle \sim E_p \langle \Delta E_v \rangle$$

# Heisenberg uncertainty principle and its optics equivalent



## Heisenberg uncertainty principle

$$\Delta p \Delta x \geq \hbar/2$$

The more precisely the POSITION is determined, the less precisely the MOMENTUM is known, and vice versa

## Optics equivalent

$$\Delta\phi \Delta N \geq 1$$

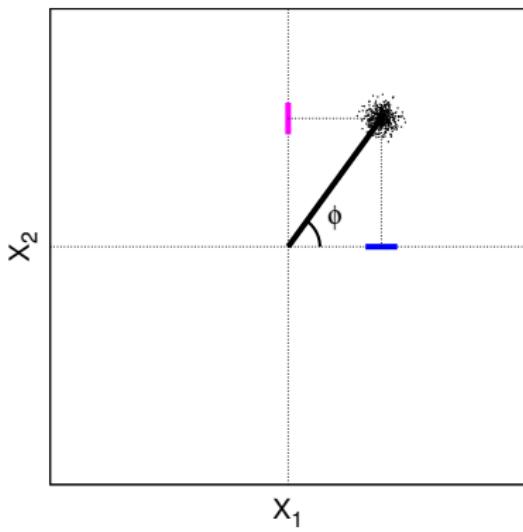
The more precisely the PHASE is determined, the less precisely the AMPLITUDE is known, and vice versa

## Optics equivalent strict definition

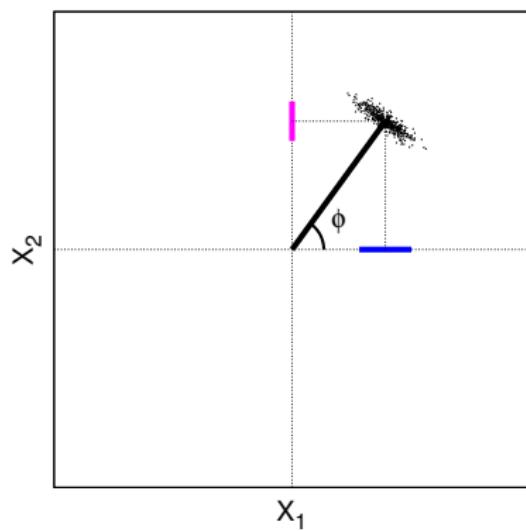
$$\Delta X_1 \Delta X_2 \geq 1/4$$

# Minimum uncertainty (coherent) states

Coherent state



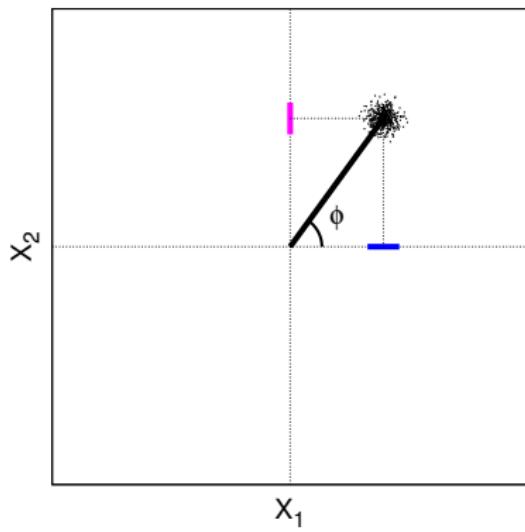
Squeezed state



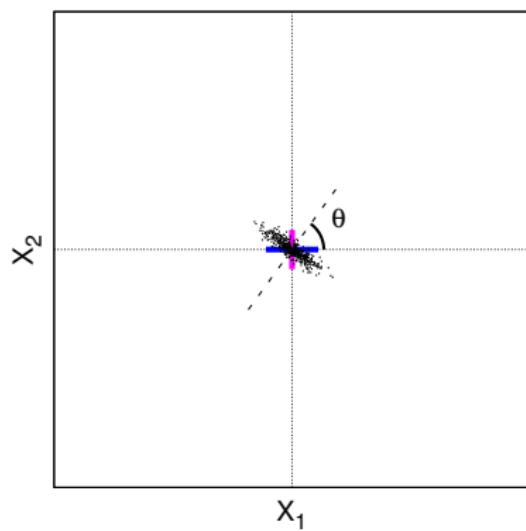
$$\Delta \textcolor{blue}{X}_1 \Delta \textcolor{magenta}{X}_2 \geq 1/4$$

# Minimum uncertainty (coherent) states

Coherent state

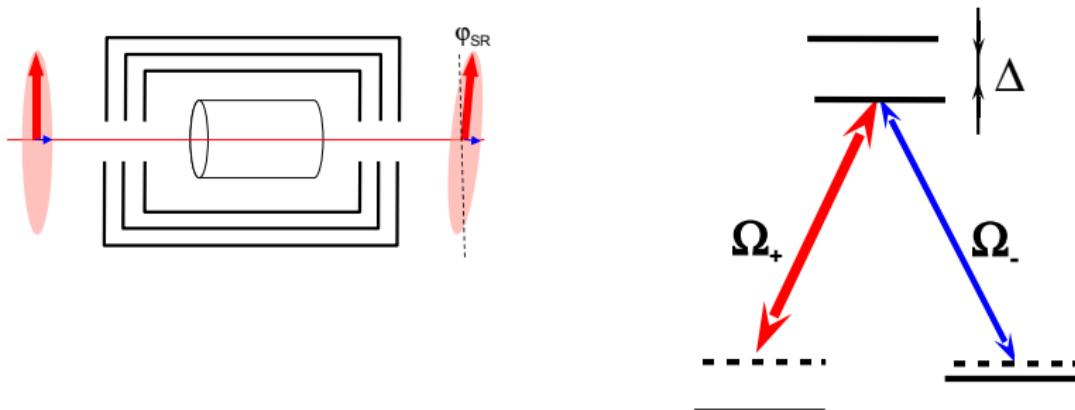


Squeezed state



$$\Delta \textcolor{blue}{X}_1 \Delta \textcolor{magenta}{X}_2 \geq 1/4$$

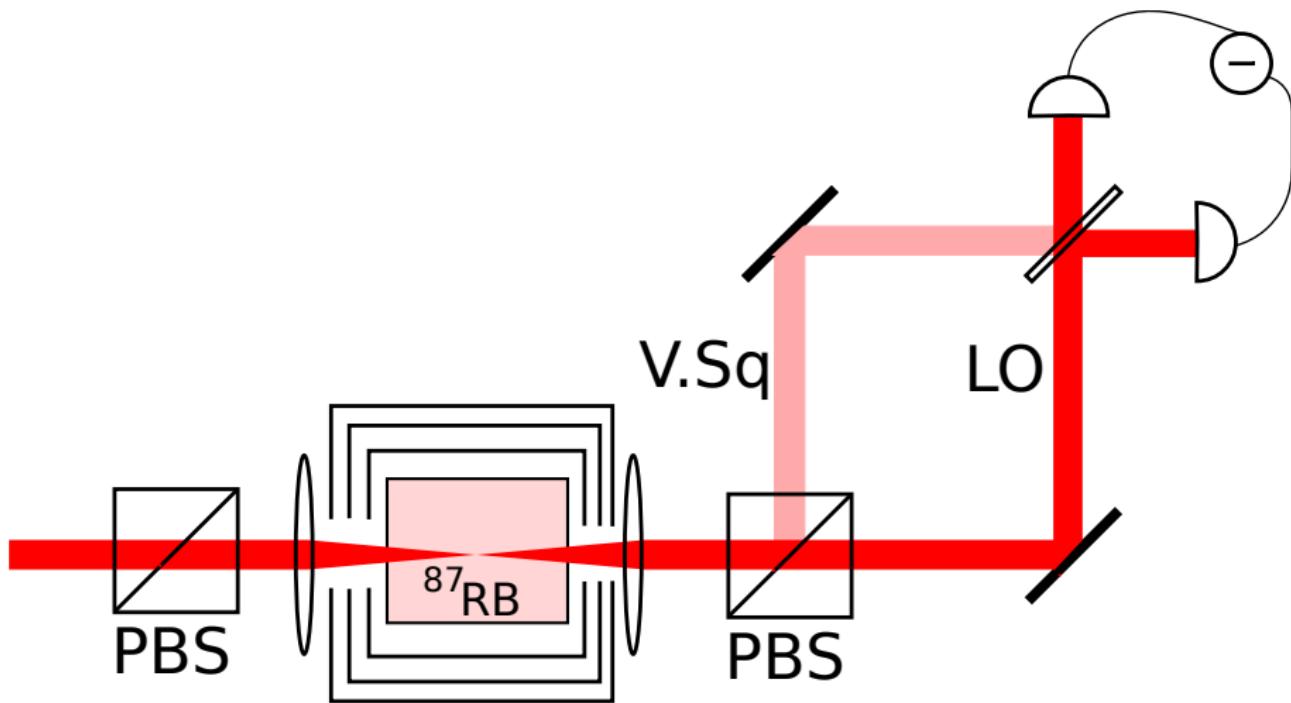
# Self-rotation of elliptical polarization in atomic medium



$$a_{out} = a_{in} + \frac{igL}{2}(a_{in}^\dagger - a_{in})$$

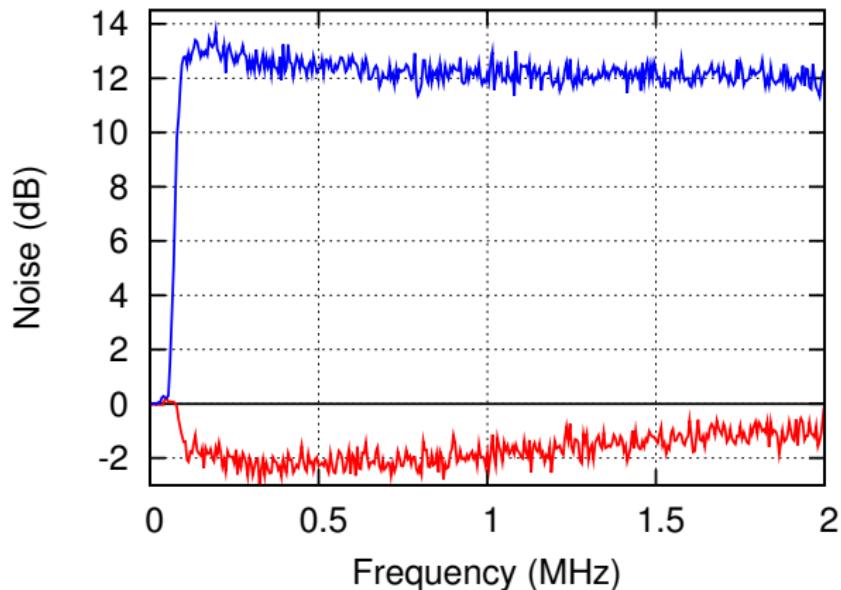
- **theory :** A.B. Matsko et al., PRA 66, 043815 (2002)
- **experiment:** J. Ries, B. Brezger, and A. I. Lvovsky, Experimental vacuum squeezing in rubidium vapor via self-rotation, PRA 68, 025801 (2003).

# Setup



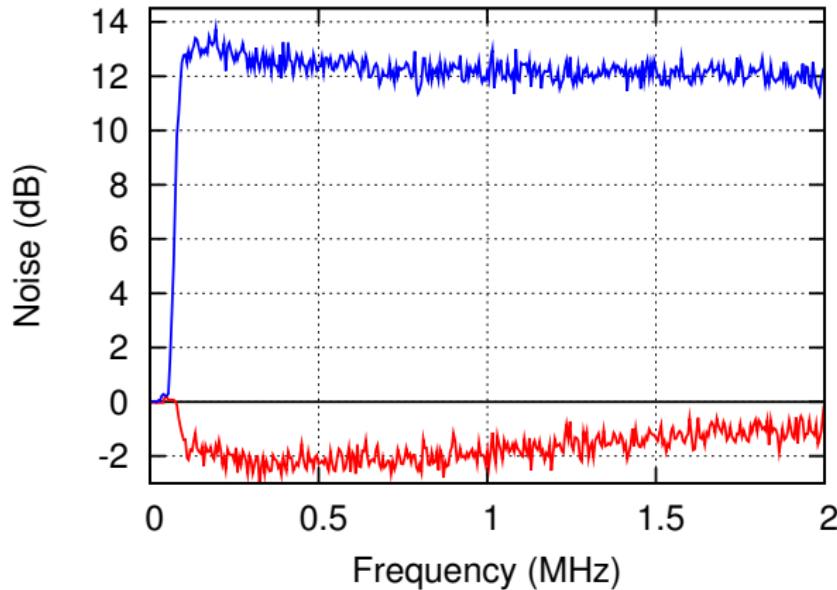
# Maximally squeezed spectrum with $^{87}\text{Rb}$

W&M team.  $^{87}\text{Rb}$   $F_g = 2 \rightarrow F_e = 2$ , laser power 7 mW, T=65° C



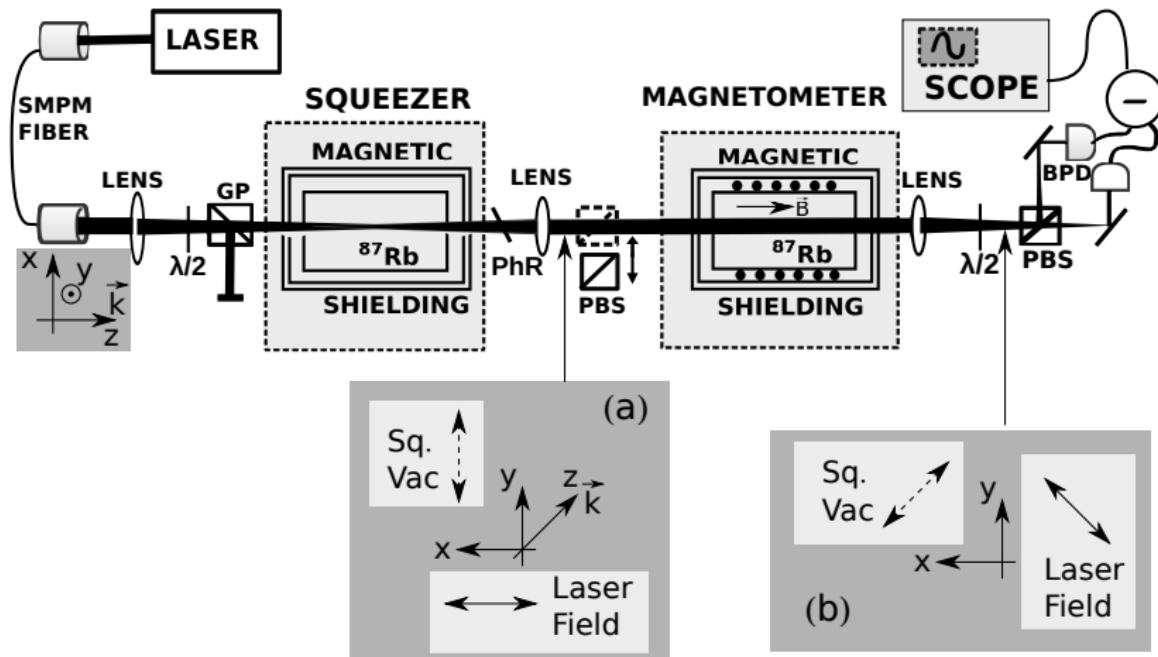
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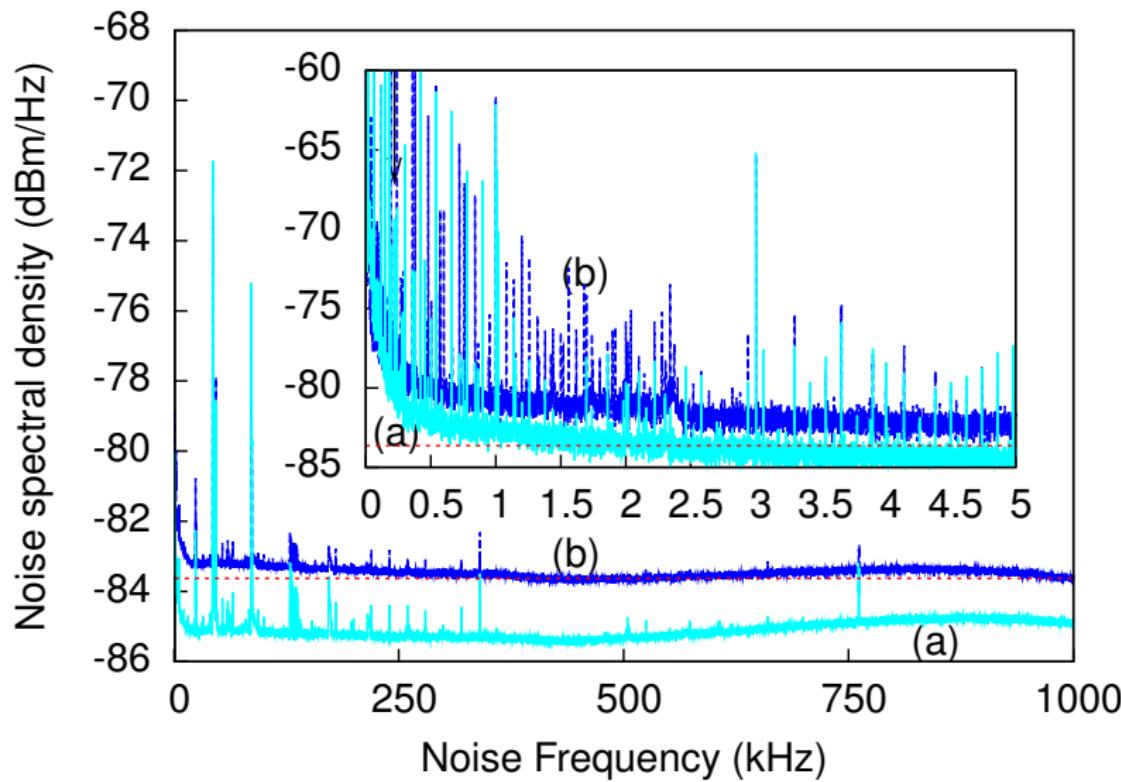
Lezama et.al report 3 dB squeezing in similar setup  
Phys. Rev. A 84, 033851 (2011)

# Squeezed enhanced magnetometer setup

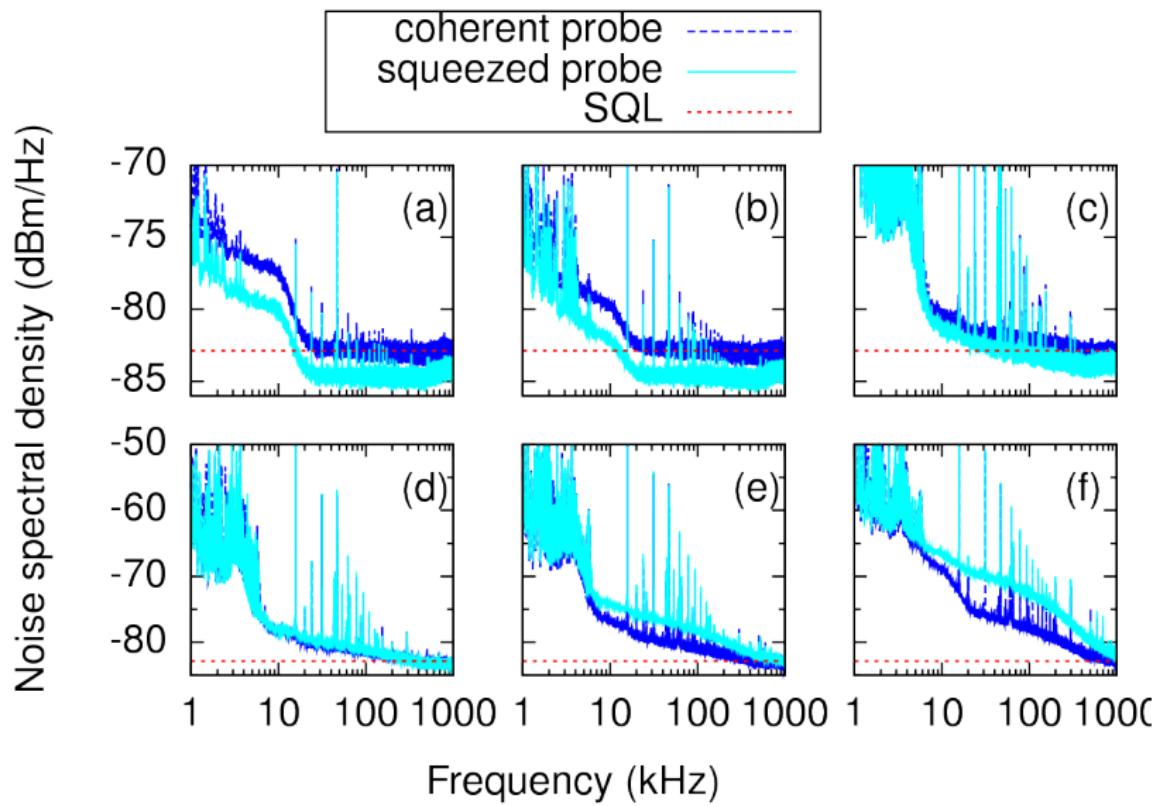


Note: Squeezed enhanced magnetometer was first demonstrated by Wolfgramm *et. al* Phys. Rev. Lett, **105**, 053601, 2010.

# Magnetometer noise floor improvements

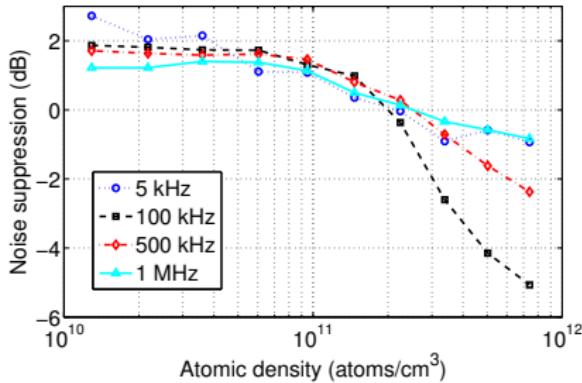


# Magnetometer noise spectra

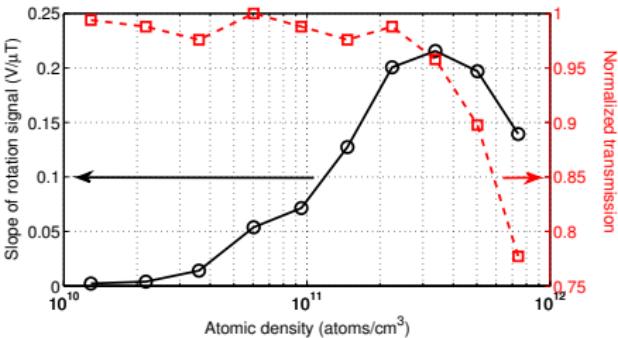


# Noise suppression and response vs atomic density

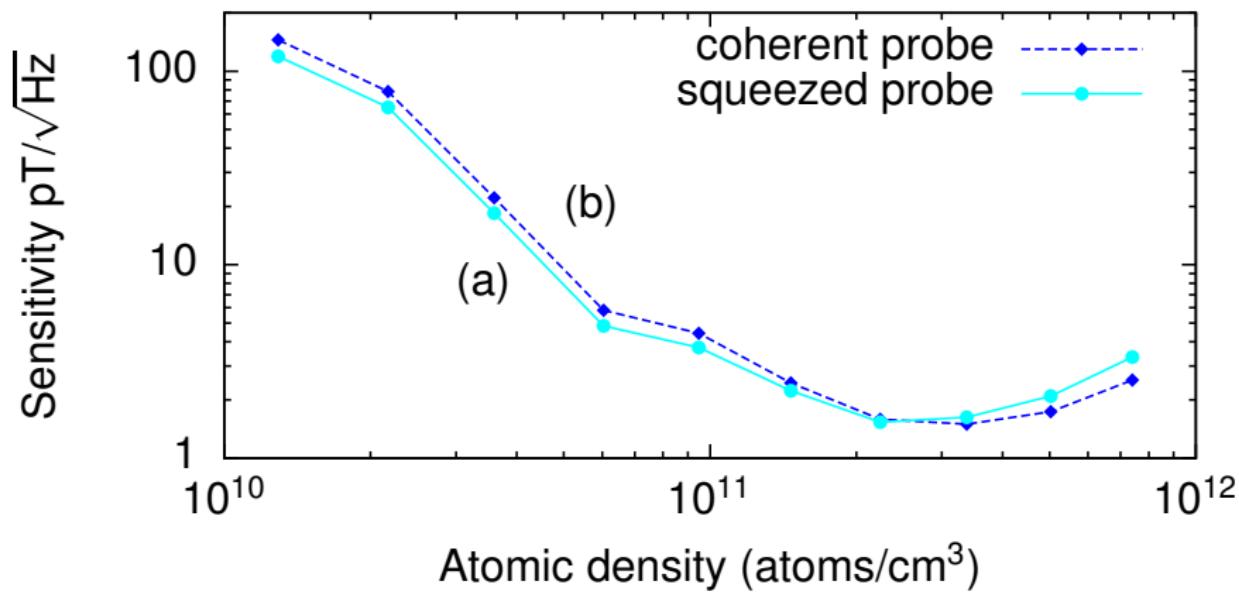
Noise suppression



Response

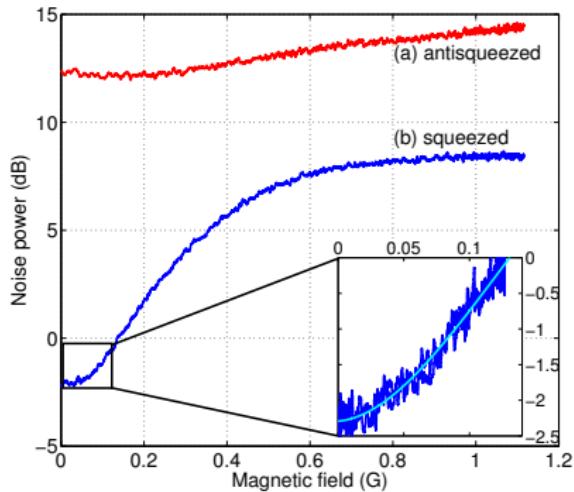
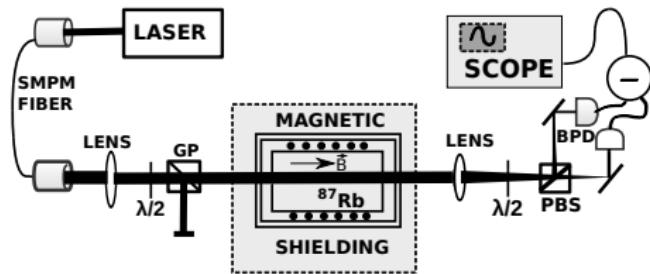


# Magnetometer sensitivity vs atomic density



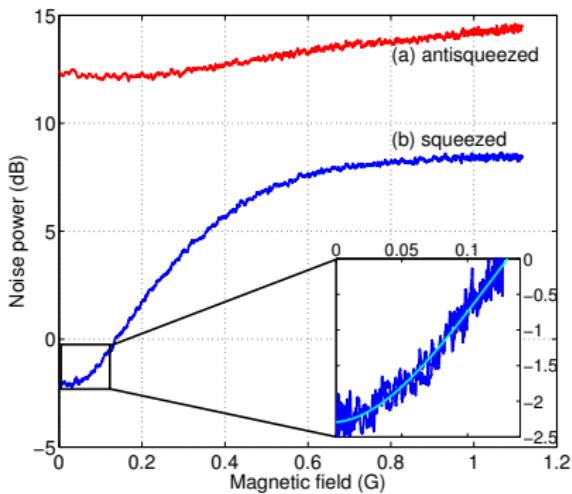
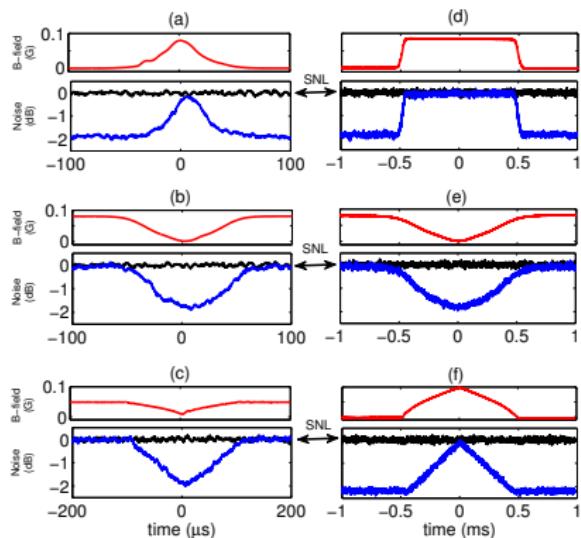
# Squeezing vs magnetic field

Spectrum analyzer settings: Central frequency = 1 MHz, VBW = 3 MHz, RBW = 100 kHz



# Squeezing vs magnetic field

Spectrum analyzer settings: Central frequency = 1 MHz, VBW = 3 MHz, RBW = 100 kHz



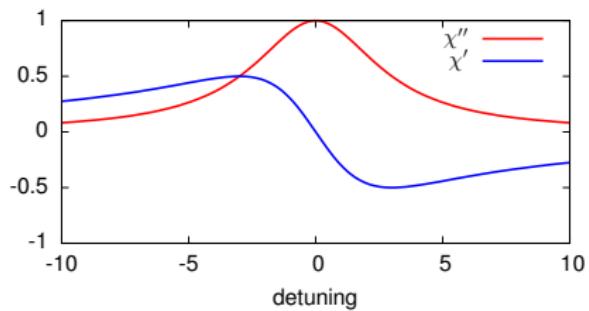
# Group velocity measurements motivation

- M. S. Shahriar, et al. “Ultrahigh enhancement in absolute and relative rotation sensing using fast and slow light”, Phys. Rev. A 75(5), 053807, 2007.
- Yakir Aharonov, et al. “Quantum Limitations on Superluminal Propagation”, Phys. Rev. Lett. 81, 2190 (1998)

# Light group velocity

$$\text{Group velocity } v_g = \frac{c}{\omega \frac{\partial n}{\partial \omega}}$$

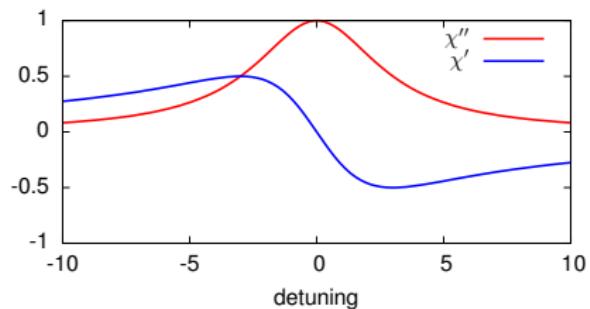
## Susceptibility



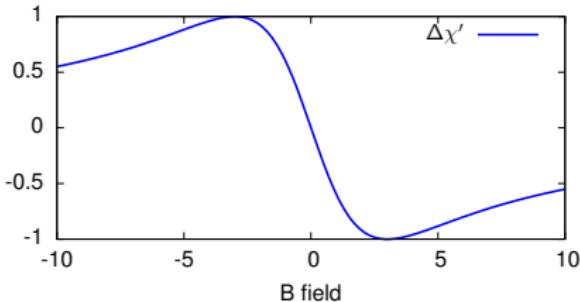
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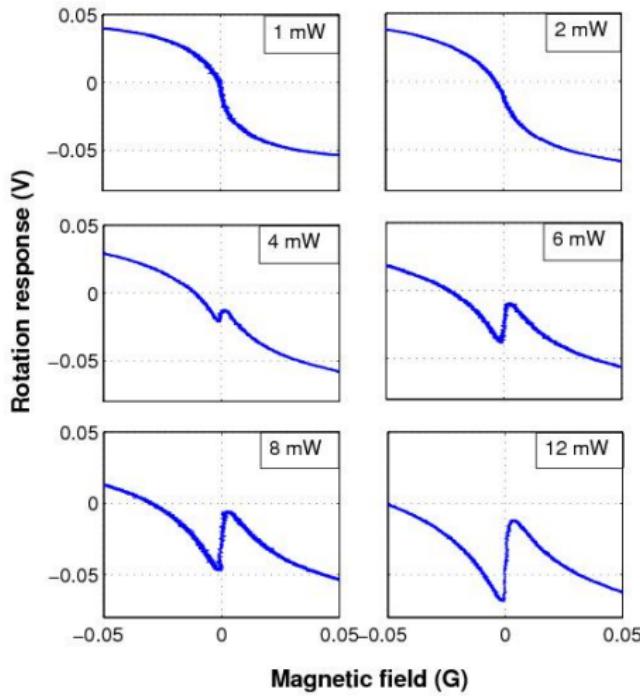
Rotation vs B field



# Light group velocity

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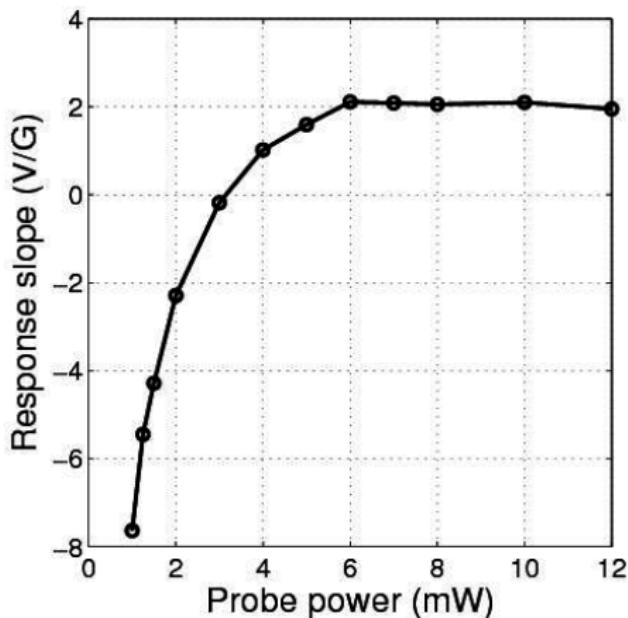
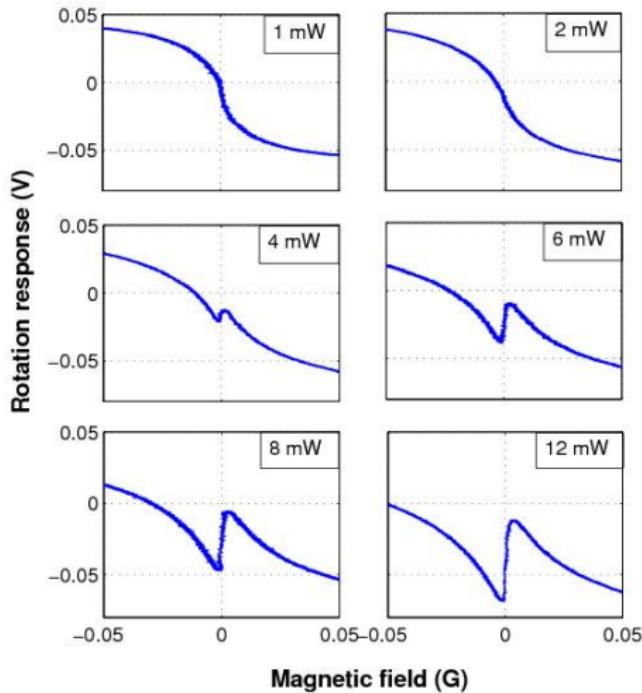
$$\text{Delay } \tau = \frac{L}{v_g} \sim \frac{\partial n}{\partial \omega} \sim \frac{\partial R}{\partial B}$$



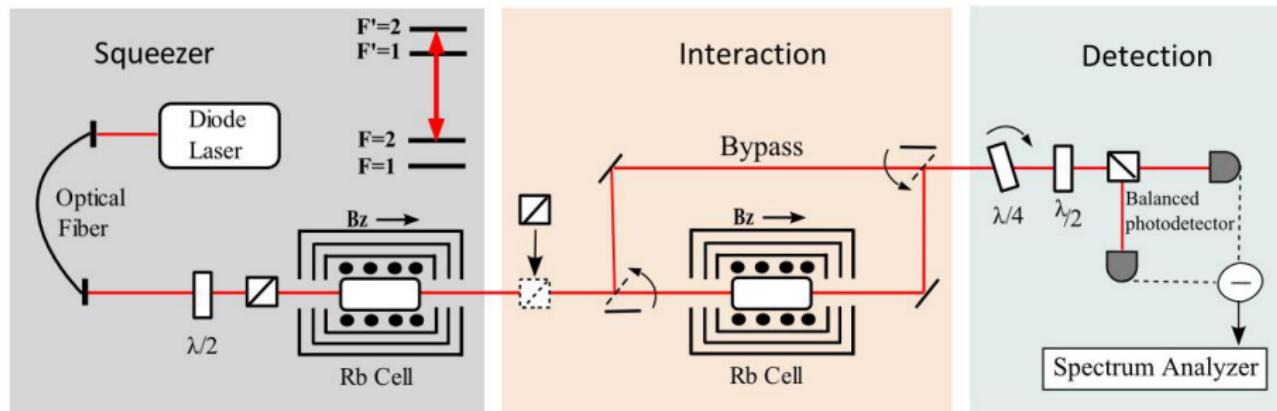
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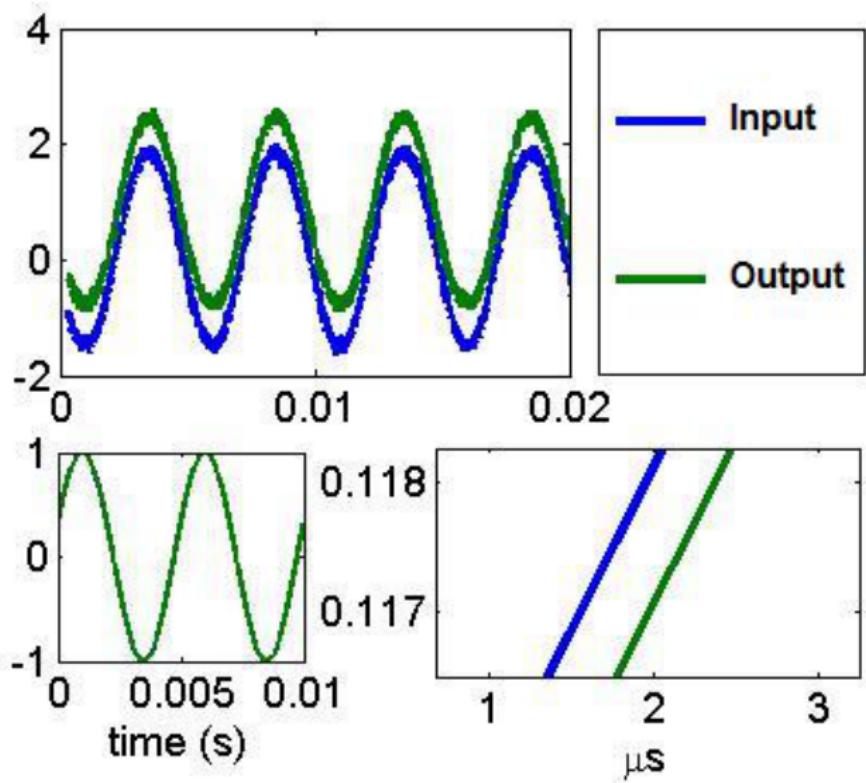
$$\text{Delay } \tau = \frac{L}{v_g} \sim \frac{\partial n}{\partial \omega} \sim \frac{\partial R}{\partial B}$$



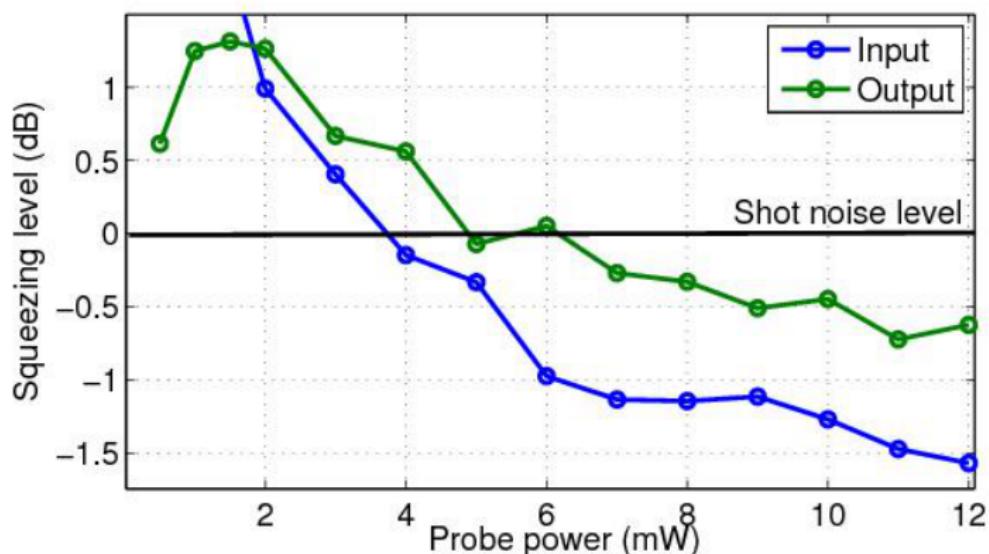
# Time advancement setup



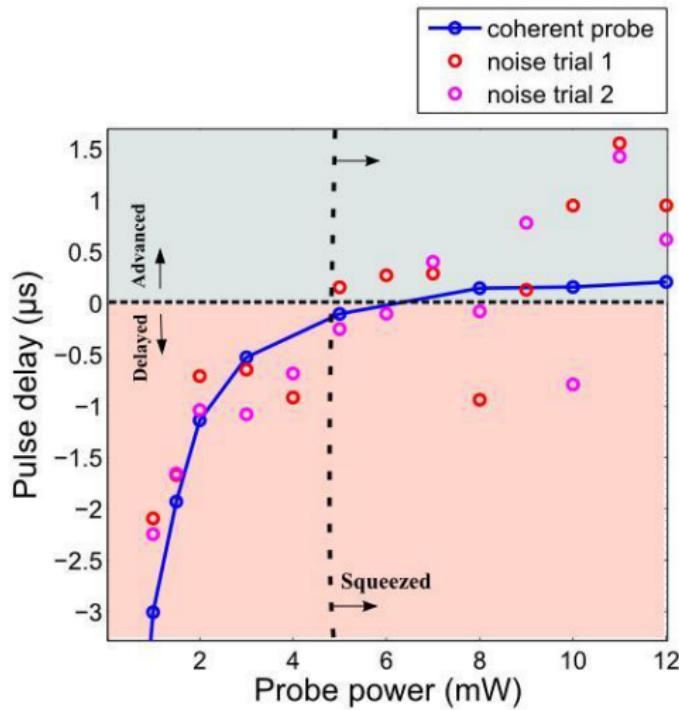
# Squeezing modulation and time advancement



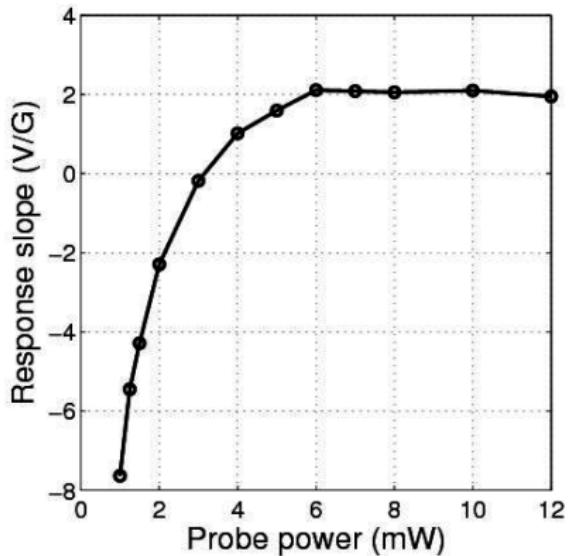
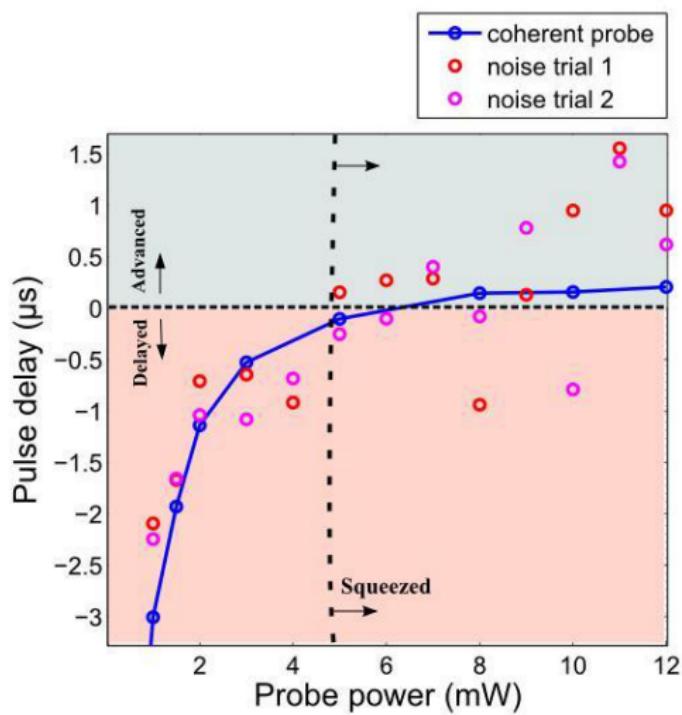
# Squeezing after advancement cell



# Advancement vs power



# Advancement vs power



# Summary

- We demonstrate fully atomic squeezed enhanced magnetometer
- Magnetometer noise floor lowered in the range from several kHz to several MHz
- Demonstrated sensitivity as low as  $1 \text{ pT}/\sqrt{\text{Hz}}$  in our particular setup
- First demonstration of superluminal squeezing propagation with  $v_g = c/2000$  or time advancement of  $0.5 \mu\text{s}$

For more details:

- T. Horrom, et al. "Quantum Enhanced Magnetometer with Low Frequency Squeezing", **PRA**, 86, 023803, (2012).