Operational amplifiers

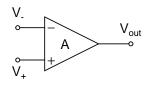
Eugeniy E. Mikhailov

The College of William & Mary



Week 9

Operational amplifiers (Op-Amp)



- $V_{out} = A(V_+ V_-)$ thus sometimes called differential amplifiers
- A is open loop gain
 - A is frequency dependent
 - $A = 10^5 \dots 10^6$ at DC
 - $A \rightarrow 0$ at high frequency (roll off) this limits operational bandwidth (typically in MHz . . . GHz range)
- input impedances are high $10^6 \dots 10^{14} \Omega$
- output impedances are low $0.1...10 \Omega$
 - however output current usually limited to 10 mA
- it is super easy to design with them

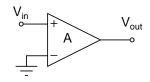


If Op-Amps are so great why did we learn transistors?

- some times one transistor is enough and op-amps are more expensive
- op-amps are made of transistors so to understand their limits we need to know how transistors behave
- op-amps require bipolar power supply
- remember that op-amps cannot source a lot of current/power while transistors can (recall our transistor voltage controlled switch for a bulb)

So, combine op-amps and transistors for a power circuits. Otherwise do your circuit with op-amps.

Very very bad amplifier !!!



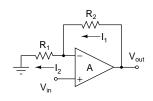
Gain

$$V_{out} = AV_{in}$$

But A depends on everything

- temperature
- power supply voltage
- input voltage
- frequency
- ... and so on

Non-inverting amplifier



$$V_{out} = \left(1 + \frac{R_2}{R1}\right) V_{in} \frac{A}{A + \left(1 + \frac{R_2}{R_1}\right)}$$

Gain and impedances of ideal Op-Amp ($A \gg 1$)

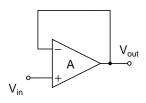
$$G_{ideal} = 1 + \frac{R_2}{R_1}$$

$$Z_{in} = \infty, Z_{out} = 0$$

notice that with negative feedback $\mathit{V}_{+} pprox \mathit{V}_{-}$



Follower or Buffer



$$V_{out} = \frac{A}{A+1}V_{in}$$

Gain and impedances of ideal Op-Amp $(A \gg 1)$

$$G_{ideal} = 1$$

$$Z_{in} = \infty, Z_{out} = 0$$

notice that with negative feedback $V_+ \approx V_-$



Op-amps golden rules

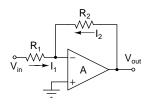
If negative feedback is applied and $A(f) \gg 1$ (open circuit gain at the frequency of interest)

- there is no current into the inputs
- $V_{-} = V_{+}$

Gain of non ideal Op-Amp $(A \gg 1)$

$$G = G_{ideal} || A = rac{G_{ideal} A}{G_{ideal} + A}$$

Inverting amplifier



Gain and impedances of ideal Op-Amp $(A \gg 1)$

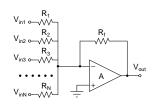
$$G_{ideal} = -rac{R_2}{R_1}$$

$$Z_{in} = R_1, Z_{out} = 0$$

notice that with negative feedback $\mathit{V}_{+} pprox \mathit{V}_{-}$



Summing inverting amplifier

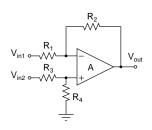


for ideal Op-Amp $(A \gg 1)$

$$V_{out} = -\left(rac{V_{in1}}{R_1} + rac{V_{in2}}{R_2} + rac{V_{in3}}{R_3} + \dots + rac{V_{inN}}{R_N}
ight)R_f$$
 $Z_{inN} = R_N, Z_{out} = 0$



Differential amplifier



for ideal Op-Amp $(A \gg 1)$

$$V_{out} = rac{R_4}{R_1} rac{R_1 + R_2}{R_3 + R_4} V_{in2} - rac{R_2}{R_1} V_{in1} \ Z_{out} = 0$$

