

## Homework 08

Name: \_\_\_\_\_

### Problem 1 (10 points)

Selection rules: Assume that electric field in the form  $\vec{E}(t) = E_o \cos(\omega t) \hat{z}$  acts on a hydrogen atom (here  $\hat{z}$  is the unit vector along  $z$  direction). Recall, that  $\hat{H}_1(t) = e\vec{E}(t) \cdot \vec{r}$  and find probabilities to transfer to either of 4 degenerate sublevels of  $n = 2$  energy level from the ground level as a function of time. Hint: start with calculation  $\langle f | \hat{H}_1 | i \rangle$ . Do not go beyond 1st order perturbation treatment.

### Problem 2 (10 points)

No external time dependent fields. The hydrogen atom at the initial time is occupying  $|n = 2, l = 0, m = 0\rangle$ . How long does it take to build up probability of transition to the ground level to be 0.5? Hint: the previous problem should help.

(In reality it is not that long since there are other mechanism for population transfer, i.e. change of probability of being in the given state).

### Problem 3 (10 points)

Consider two level atom under perturbation where

$$\hat{H}_{1_{ab}} = \hat{H}_{1_{ba}} = \frac{\alpha}{\sqrt{\pi\tau}} e^{-(t/\tau)^2} \quad (1)$$

$$\hat{H}_{1_{aa}} = \hat{H}_{1_{bb}} = 0 \quad (2)$$

- At the initial time  $t_i = -\infty$  the  $c_a = 1, c_b = 0$ , what is the probability to find the system at state  $|b\rangle$  at time  $t = \infty$ ?
- Same question at the limit  $\tau \rightarrow 0$  resulting in  $\hat{H}_{1_{ab}} = \alpha\delta(t)$
- Same question in adiabatic regime  $\omega_0\tau \gg 1$