

$$\vec{r}(t) = \vec{r}_0 + \vec{v}_0 t + \frac{\vec{a} t^2}{2}$$

$$\vec{a} = \{0, 0, -g\} \quad z(t) = 0 + 0t + \frac{0 \cdot t^2}{2} = 0$$

$$x(t) = 0$$

$$y(t) = 0 + v_{0y} \cdot t + \frac{a_y t^2}{2} =$$

$$-h = 0 + v_{0y} t + \frac{-g t^2}{2}$$

$$-\frac{g t^2}{2} + v_{0y} t + h = 0$$

$$A t^2 + B t + C = 0$$

$$t = \frac{-B \pm \sqrt{B^2 - 4 \cdot A \cdot C}}{2A}$$

$$t = \frac{-v_{0y} \pm \sqrt{v_{0y}^2 - 4\left(-\frac{g}{2}\right) \cdot h}}{2 \cdot \left(-\frac{g}{2}\right)}$$

$$v_{0y} = 4 \text{ m/s}$$

$$h = 1 \text{ m}$$

$$g = 9.8 \frac{\text{m}}{\text{s}^2} \approx 10 \frac{\text{m}}{\text{s}^2}$$

$$t = \frac{-4 \pm \sqrt{16 - 4 \cdot \frac{-10}{2} \cdot 1}}{-10}$$

$$= \frac{-4 \pm \sqrt{36} \approx 6}{-10}$$

$$= \frac{-4 \pm 6}{-10} = 1 \text{ s}; -0.2 \text{ s}$$

$$\vec{v}(t) = \vec{v}_0 + \vec{a} \cdot t$$

$$y: v_y(t) = v_{0y} + a_y \cdot t$$

$$v_y(t=1s) = 4 \frac{m}{s} + (-10 \frac{m}{s^2}) \cdot 1s$$

hit the floor

$$= -6 \text{ m/s}$$

$$y_f - y_0 = \frac{v_{fy}^2 - v_{0y}^2}{2 \cdot a_y}$$

$$-1 = \frac{-1}{-1} - 0 = \frac{v_{fy}^2 - (-4)^2}{2 \cdot (-10)}$$

$$-1 = \frac{v_{fy}^2 - 16}{-20} \Rightarrow v_{fy}^2 = 36$$

$$v_{fy} = \pm \sqrt{36} = \pm 6$$

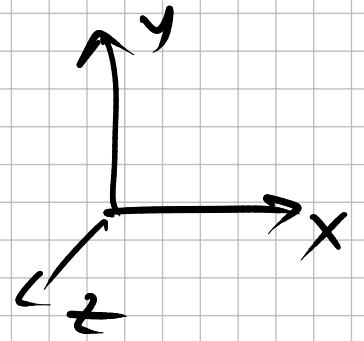
our choice

$$25 \frac{\text{mi}}{\text{h}} = \frac{25 \text{ mi} \cdot 1600 \frac{\text{m}}{\text{mi}}}{1 \text{ h} \cdot \frac{3600 \text{ s}}{\text{h}}} = 11.1 \frac{\text{m}}{\text{s}}$$

$$-|h| = \frac{v_{fy}^2}{-2g} = \frac{11^2}{-2 \cdot 10} = -\frac{121}{20} = -6.05 \text{ m}$$

$$\vec{r}(t) = \vec{r}_0 + \vec{v}_0 t + \frac{\vec{a} \cdot t^2}{2}$$

$$\vec{a} = \{0, -g, 0\}$$



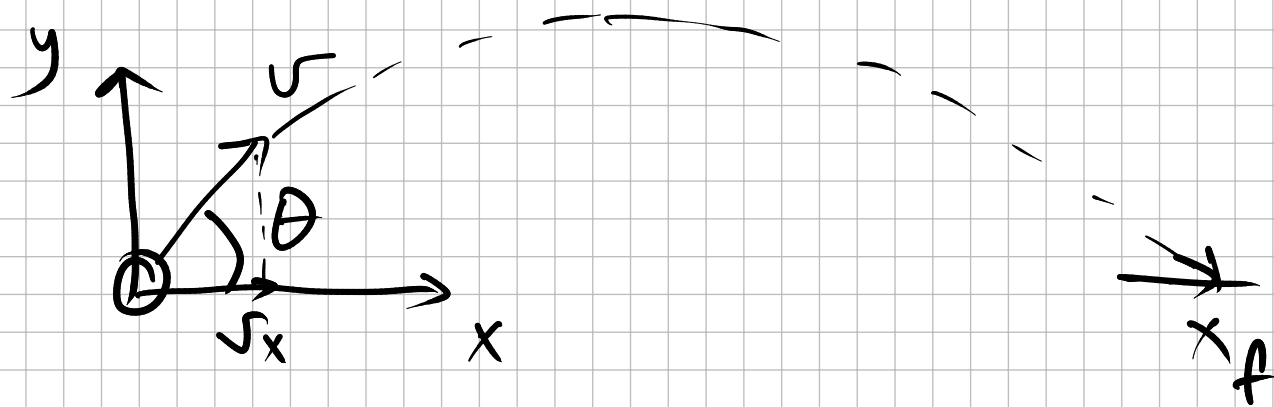
$$x(t) = x_0 + v_{0x} \cdot t + \frac{a_x t^2}{2} \rightarrow 0$$

$$y(t) = y_0 + v_{0y} t + \frac{a_y t^2}{2}$$

$$= y_0 + v_{0y} t - \frac{g t^2}{2}$$

$$v_x(t) = \frac{dx(t)}{dt} = 0 + v_{0x} = v_{0x}$$

$$v_y(t) = \frac{dy(t)}{dt} = 0 + v_{0y} - a_y t$$



$$v_{x_0} = v \cdot \cos \theta$$

$$v_{y_0} = v \cdot \sin \theta$$

hit the ground time

$$0 = 0 + v_{y_0} t - \frac{gt^2}{2}$$

$$t = 0 ; \frac{2v_{y_0}}{g} = \frac{2v \sin \theta}{g}$$

$$X = X_0 \overset{=0}{=} + v_{0x} \cdot t = v \cdot \cos\theta \cdot \frac{2v \sin\theta}{g}$$
$$= \frac{v^2}{g} \cdot 2 \cos\theta \cdot \sin\theta = \frac{v^2}{g} \sin(2\theta)$$

if $v = 400 \frac{\text{m}}{\text{s}}$ $X = \frac{400^2}{10} \cdot 1 = 16 \cdot 1000 \text{ m}$
 $= 16 \text{ km}$
 $= 10 \text{ mi.}$