

$$F_{b1} = W_b + W_s = \rho_w g V_{\text{water displaced}_1} \Rightarrow V_{w.d.1} \text{ displaced water}$$

$$F_{b2} = W_b = \rho_w g V_{\text{water displaced}_2} \Rightarrow V_{w.d.2} + V_s$$

$$V_{w.d.1} = \frac{W_b + W_s}{\rho_w g} = \boxed{\frac{W_b}{\rho_w g}} + \frac{W_s}{\rho_w g} = \boxed{\phantom{\frac{W_b}{\rho_w g}}} + \frac{m_s}{\rho_w}$$

$$V_{w.d.2} = \frac{W_b}{\rho_w g} = \frac{W_b}{\rho_w g} \quad V \text{ smaller}$$

$$V_{\text{total}} = V_{w.d.2} + V_s = \boxed{\frac{W_b}{\rho_w g}} + \frac{m_s}{\rho_s} = \boxed{\phantom{\frac{W_b}{\rho_w g}}} + \frac{m_s}{\rho_s}$$

compare

$\rho = \text{const} = \text{incompressible!}$



flow rate

$$Q = \frac{\Delta V}{\Delta t} = \text{const} = \frac{A_1 \cdot \Delta L_1}{\Delta t} = A_1 \cdot v_1 = A_2 \cdot v_2$$

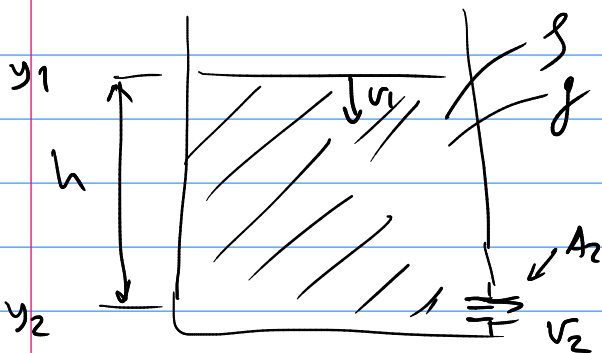
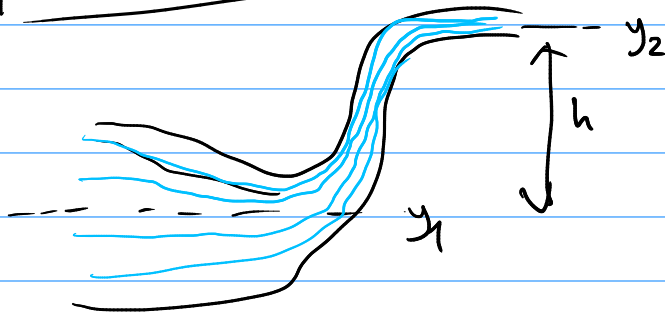
$$\Delta K = \frac{m v_2^2}{2} - \frac{m v_1^2}{2} = W_{\text{ext}} = F_1 \cdot \Delta L_1 - F_2 \Delta L_2$$

$$= P_1 \underbrace{A_1 \Delta L_1}_{\Delta V} - P_2 \underbrace{A_2 \Delta L_2}_{\Delta V}$$

$$\frac{\Delta K}{\Delta V} = \frac{\underbrace{m}_{\rho} v_2^2}{2 \underbrace{\Delta V}_{\rho \Delta V}} - \frac{\underbrace{m}_{\rho} v_1^2}{2 \underbrace{\Delta V}_{\rho \Delta V}} = P_1 - P_2$$

$$\rho g y_2 + P_2 + \rho \frac{v_2^2}{2} = P_1 + \rho \frac{v_1^2}{2} + \rho g y_1 = \text{const}$$

laminar flow



$$A_2 \ll A_1 \Rightarrow v_1 \approx 0$$

$$\therefore \rho g y_1 + \rho \frac{v_1^2}{2} = \rho g y_2 + \rho \frac{v_2^2}{2} : 2$$

$$g \underbrace{(y_1 - y_2)}_h = \frac{v_2^2}{2}$$

$$v_2 = \sqrt{2gh}$$

