

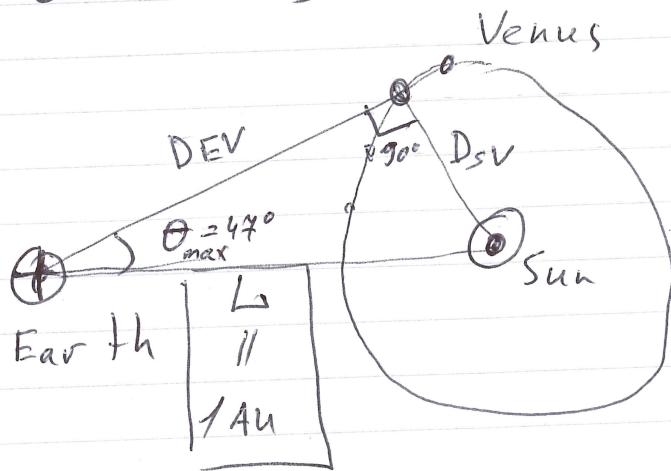
Lecture 2

* Stellarium demo to show planets motion

* Did Greeks knew distances to known planets?

Yes! for inner planets, but relative to $\oplus \leftrightarrow \odot$ distances

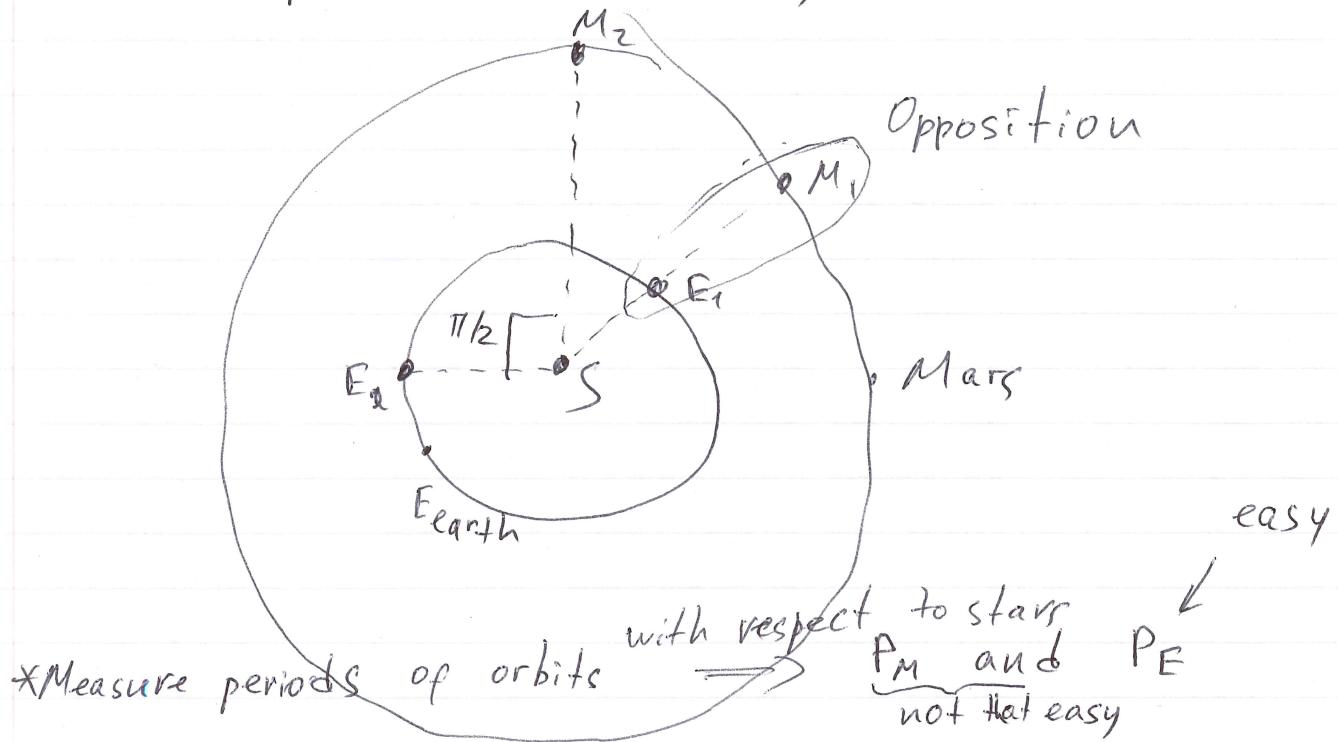
Idea:



$$\begin{aligned} D_{SV} &= L \cdot \sin \theta_{\max} = \\ &= 0.73 \text{ AU} \end{aligned}$$

(P2)

Outer planets are tricky but doable too!



** Wait for opposition, then wait for another one, let's call this time S (synodic)

Time S is the same to make 2π arc with respect to another planet

Assuming circular orbits with respect to stars each planet makes arc = $\frac{2\pi}{P} \cdot t$

$$\text{So } \frac{2\pi}{P_E} S - \frac{2\pi}{P_M} S = 2\pi$$

$$\Rightarrow \boxed{\frac{1}{S} = \frac{1}{P_E} - \frac{1}{P_M}}$$

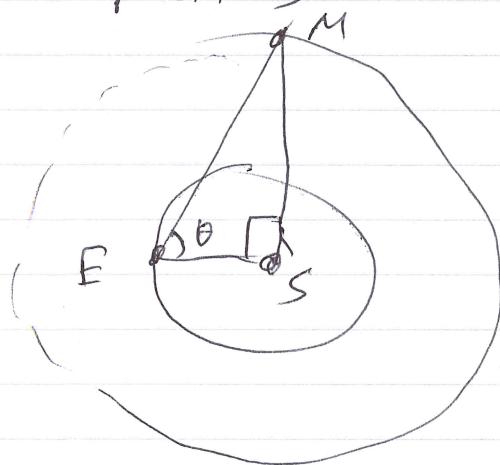
flip sign if planet is an inner one

Mars is just an example true for any other planet

(P3)

Now we have P_M and P_E

So if we wait time $t_{\pi/2}$ necessary to have arc difference of $\pi/2$ after an opposition we will get $\pi/2$ angle between a planet \rightarrow sun directions.



Measure θ and we will know distance to Mars

$$\frac{\pi}{2} = \frac{2\pi}{P_E} t_{\pi/2} - \frac{2\pi}{P_M} t_{\pi/2}$$

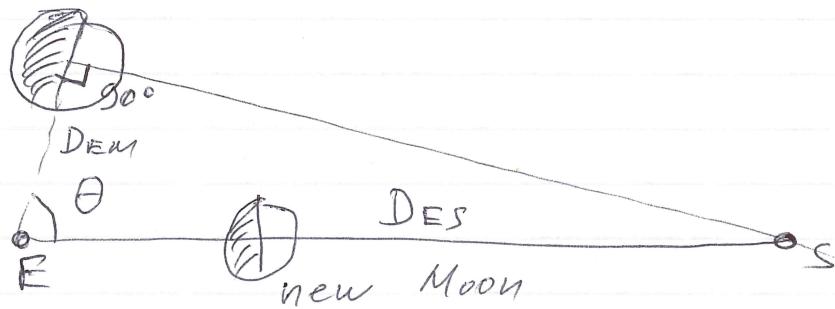
$$\frac{\pi}{2} = 2\pi \frac{1}{S} t_{\pi/2}$$

$$\Rightarrow t_{\pi/2} = \frac{S}{4}$$

$$D_{SM} = \tan \circ \tan \theta$$

How to measure distance to the moon?
 Idea from Aristarchus (310 - 230 BC)
 who by the way suggested (Heliocentric)
 sun model

Half
Moon
position



$$\frac{D_{EM}}{D_{ES}} = \cos \theta$$

$$\Rightarrow D_{EM} = \cos \theta \cdot \underline{D_{ES}}$$

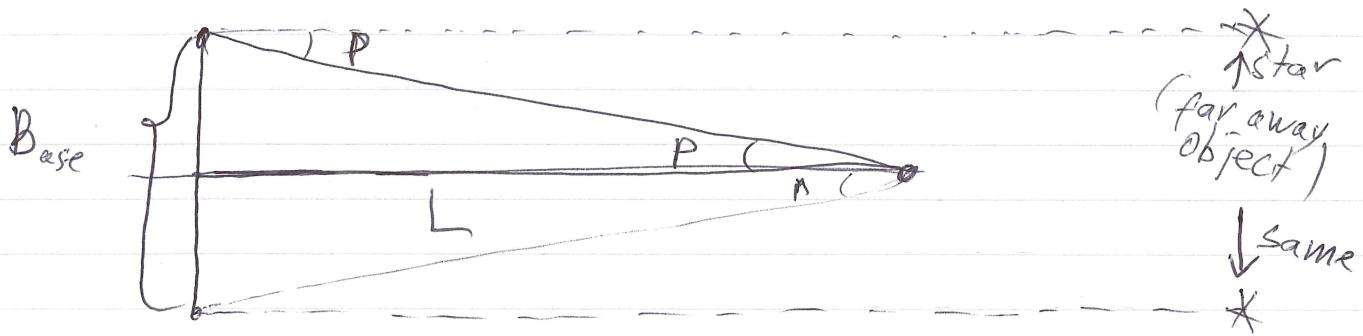
~~Aristarchus~~

Aristarchus estimate of $\theta \approx 87^\circ$
 modern day values $= 89^\circ 50'$
 $\cos \theta = 0.003$

(P5)

There is still a problem:
what is 1au?

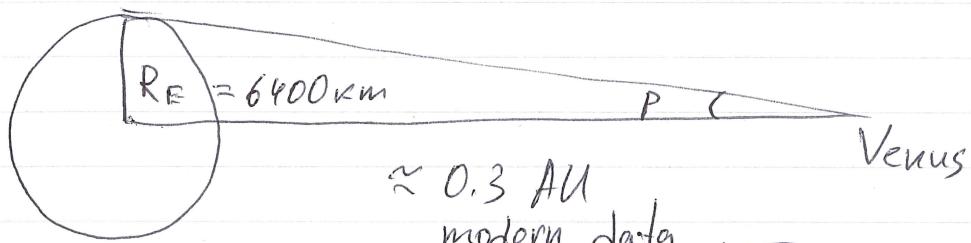
How can we measure distance
 to the far object



$$L = \frac{B}{2} \cdot \frac{1}{\tan \alpha} = |P \ll 1| = \frac{B}{2 \alpha}$$

So why 1au is hard?

the largest Base on Earth is its diameter



$$P = \frac{6400 \text{ km}}{0.3 \cdot 1.5 \cdot 10^{11}} = \frac{6400}{4.5 \cdot 10^{11}} = 1.4 \cdot 10^{-4} \text{ rad} \cdot \frac{180^\circ}{\pi} \cdot \frac{60'}{70} =$$

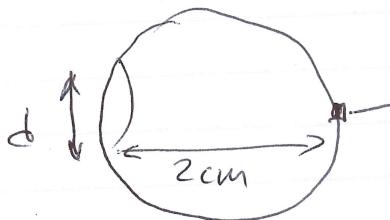
$$= 0.49' \uparrow \text{arc. minutes}$$

(P6)

r' is it small or big?

Eye

Physiological limit



'pixel' size of the rods and cones
 $\approx 2\text{ }\mu\text{m}$

$$\theta_{\min} = \frac{2\text{ mm}}{2\text{ cm}} = \frac{2 \cdot 10^{-6}}{2 \cdot 10^{-2}} \approx 10^{-4} \text{ rad}$$

$$\approx 0.34'$$

Best possible
condition

There is also diffraction limit (wave optics)

$$\theta_{\min} = 1.22 \frac{\lambda}{d} = 1.22 \frac{500\text{ nm}}{5\text{ mm}} = 1.22 \cdot \frac{500 \cdot 10^{-9}}{5 \cdot 10^{-3}} =$$

$$= 1.22 \cdot 10^{-4} = 0.4'$$

Amazingly close to physiological limit

All of above is for the best possible conditions.

So when Tycho Brahe reported 4'
resolution, it was impressively good.

But not enough to measure distance to
Venus, even with 1.R_E base (unavailable at
that time, 1546-1601).