Notes

Data interpolation Eugeniy E. Mikhailov The College of William & Mary

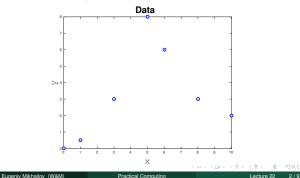


Lecture 22

Eugeniy Mikhailov (W&M) Data interpolation - filling the voids

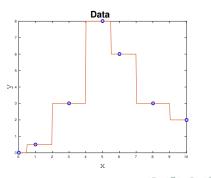
There is rarely enough data. It often takes a lot of time to get a data point. It might be expensive. Nevertheless, we would like to have some representation of the system in the voids.

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The nearest neighbor interpolation

The name says it all. For each interpolated point $(x_{interpolated})$, find the nearest neighbor along the x_i axis in the data set and use its y_i value.

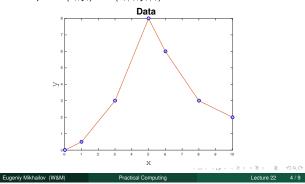


Linear interpolation

Eugeniy Mikhailov (W&M)

We will split our data set with N points to N - 1 intervals and interpolate the values in the given interval as a line passing through the border points (x_i, y_i) and (x_{i+1}, y_{i+1})

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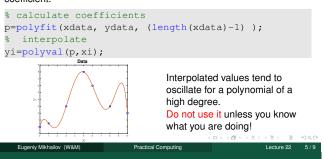
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Polynomial fit

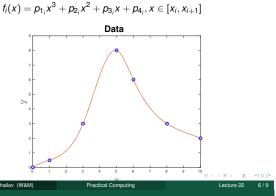
You can always find a polynomial of N - 1 degree passing through N data points.

 $P_N(x) = p_1 x^N + p_2 x^{N-1} + \dots + p_N x + p_{N+1}$ Matlab has the 'polyfit' function which returns the polynomial coefficient.



Cubic spline interpolation

We will interpolate N data points by a polynomial of 3rd degree for each *i*th interval between data point



Cubic spline interpolation demystified

We will interpolate N data points by a polynomial of 3rd degree for each *i*_{th} interval between data point

$$f_i(x) = \rho_{1_i} x^3 + \rho_{2_i} x^2 + \rho_{3_i} x + \rho_{4_i}, x \in [x_i, x_{i+1}]$$

Interpolation must pass through data points

$$f_i(x_i) = y_i$$

$$f_i(x_{i+1}) = y_{i+1}$$

The two above equations are not sufficient to constrain the four polynomial coefficients. We request $f_i(x)$ to have continuous 1st derivative at the borders

Additionally, we specify the 2nd derivatives at end points. Common choice is to set it to 0. This is the, so-called, natural cubic spline.

 $f'_i(x_{i+1}) = f'_{i+1}(x_{i+1})$ $f_i'(x_i) = f_{i-1}''(x_i)$

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 $f_1''(x_1) = 0$ $f_{N-1}''(x_N) = 0$

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Matlab built in interpolation

Notes

Use matlab interpl(xdata, ydata, xi, method) for some of above methods Where ${\tt method}\ could\ be$

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'nearest' Nearest neighbor interpolation

- 'linear' Linear interpolation (default)
- 'spline' Cubic spline interpolation
- other see more in help

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Do not extrapolate unless you have a physical model of the process!

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