Sorting

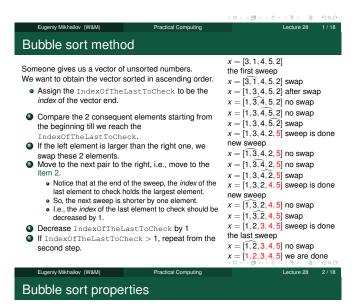
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Lecture 28



- \bullet The execution time of this algorithm is $\mathcal{O}(\textit{N}^2)$
- This is the worst of all working algorithms!
- Never use it in real life!
- However, it is quite intuitive and a very simple to program.
- It does not require extra memory during the execution.

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Quick sort method

A much better, yet still simple algorithm. We will discuss the recursive realization.

The name of our sorting function is ${\tt qsort.}$

- Choose a pivot point value
 - let's choose the pivot at the middle of the vector
 - pivotIndex=floor(N/2)
 - pivotValue=x(pivotIndex)
- Create two vectors which hold the lesser and larger than pivotValue elements of the input vector.
- Now, concatenate the result as xs=[qsort(lesser), pivotValue, qsort(larger)]
- The sorting is done.

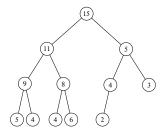
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Quick sort summary

- It is very easy to implement.
- It is usually fast.
- A typical execution time is $\mathcal{O}(N \log_2 N)$.
- This is not guaranteed.
 - For certain input vectors the execution time could be as long as $\mathcal{O}(N^2)$.

Heap

The heap is a structure where a parent element is larger or equal to its children.



The top most element of a heap is called the root.

Heap sorting method

- Fill the heap from the input vector elements.
 - Take an element and place it at the bottom of the heap.
 - Sift-up (bubble up) this element.
 - 3 Do the same with every following element.
- Remove the root element, since it is the largest.
- Rearrange the heap i.e. sift-down.
 - Take the last bottom element.

 - Place it at the root.Check if parent is larger then children.

 - Find the largest child element.
 If the largest child is larger then parent, swap them and repeat the check in the sub heap of this child element.
- Repeat step 2 until no elements are left in the heap.

The heap sorting complexity is $\mathcal{O}(N \log_2 N)$.

Filling (sift-up) the heap

Step 1 Place a new element at the bottom of the heap.

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Filling (sift-up) the heap

Step 2 Check if the parent is larger then the child. If so, swap them and repeat the step 2.

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Filling (sift-up) the heap

Step 2 Check if the parent is larger then the child. If so, swap them and repeat the step 2.

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Filling (sift-up) the heap

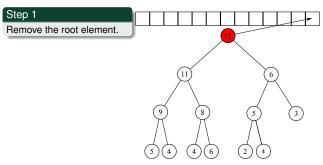
Step 2
Check if the parent is larger then the child. If so, swap them and repeat the step 2.

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Removing from the heap (sift-down) the heap



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Removing from the heap (sift-down) the heap

Step 2 Place the last element of the heap to the root position.

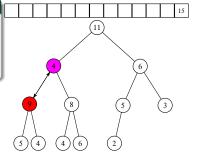
Removing from the heap (sift-down) the heap

Step 3 Check if the parent is smaller than the largest child. If so, swap and repeat the step 3, otherwise go to the step 1.

Removing from the heap (sift-down) the heap

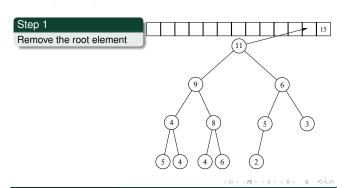
Step 3 Check if the parent is smaller than the largest

child. If so, swap and repeat the step 3, otherwise go to the step 1.



Removing from the heap (sift-down) the heap

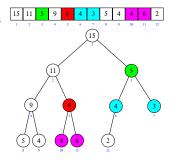
The sequence repeats.



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The vector heap representation

- Heap nodes are numbered consequently. These numbers represent the nodes positions in the vector (i.e., the linear array).
- Notice that the parent and its children have a very simple relationship
 - ullet if a parent node index is ${\tt i}$
 - the 1st child index is 2i
 - the 2nd child index is
 - If we know a child index (i) then
 - the parent index is floor(i/2)



Matlab built-ins 'issorted' and 'sort'

An easy check if an array is sorted can be done with ${\tt issorted}$ which returns true or false.

```
>> x=[1,2,3];
>> issorted(x)
ans = 1
```

 ${\tt issorted} \ \textbf{checks only for the ascending order, for example}$

```
>> x=[3,2,1];
>> issorted(x)
ans = 0
% Recall that '0' is equivalent of false in Matlab
```

Also, if you want to sort an array, the Matlab has the sort function to do it.

```
>> sort([5,3,2])
ans = 2
```

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