Sorting

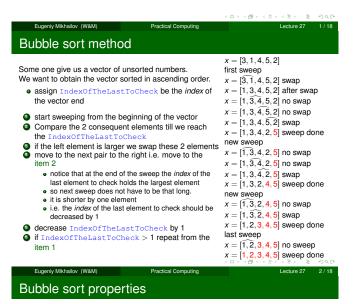
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Lecture 27



- This is the worst of all working algorithm!
- ullet The execution time of this algorithm is $\mathcal{O}(N^2)$
- Never use it in the real life!
- However it is very simple to program, and does not require extra memory for execution.



Quick sort method

Much better yet simple algorithm Let's discuss recursive realization We will name our sorting function as qsort.

- choose a pivot point value
 - let's choose the pivot at the middle of the vector
 - pivotIndex=floor(N/2)
 - pivotValue=x(pivotIndex)
- create two vectors which hold lesser and larger than pivotValue elements of the input vector.
- now concatenate the result of xs=[qsort(lesser), pivotValue, qsort(larger)]
- done

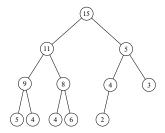
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Quick sort summary

- usually fast
- typical execution time $\mathcal{O}(N \log_2 N)$
- but it is not guaranteed
 - However for certain input vectors execution time could be as long as $\mathcal{O}(N^2)$

Heap

Heap is a structure where parent element is larger or equal to its children.



The top most element of the heap is called root.

Heap sorting method

- Fill the heap from the input vector elements
 - take the element and place it at the bottom of the heap
 - a sift-up (bubble up) this element
 - 3 do the same with the next element
- remove the root element since it is the largest
- rearrange the heap i.e. sift-down
 - take the last bottom element

 - place it at the root
 check if parent is larger then children

 - find the largest child element
 if the largest child is larger then parent swap them and repeat the
- repeat step 2 until no elements left in the heap

Heap sorting complexity $\mathcal{O}(N \log_2 N)$

Filling (sift-up) the heap

Step 1 (15) Place new element at the bottom of the heap

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Filling (sift-up) the heap

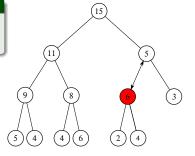
Step 2 Check if parent is larger then child. If so swap them and repeat step 2.

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Filling (sift-up) the heap

Step 2

Check if parent is larger then child. If so swap them and repeat step 2.

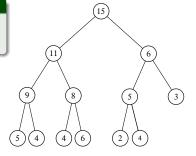


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Filling (sift-up) the heap

Step 2

Check if parent is larger then child. If so swap them and repeat step 2.



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Removing from the heap (sift-down) the heap

Step 1 Remove the root element 9 8 5 4 4 6 2 4

4 m > 4 m >

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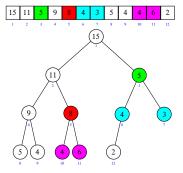
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Removing from the heap (sift-down) the heap Notes Step 2 Place the last element of the heap to the root Removing from the heap (sift-down) the heap Notes Step 3 Check if parent is smaller than the largest child. If so swap and repeat step 3 else go to step 1 Removing from the heap (sift-down) the heap Notes Step 3 Check if parent is smaller than the largest child. If so (11) swap and repeat step 3 else go to step 1 Removing from the heap (sift-down) the heap Notes Sequence repeats Step 1 Remove the root element (11)

Vector heap representation

- Heap nodes are numbered consequently these numbers represent the node position in the vector.
- notice that parent and children have very simple relationship
 - if parent node index is i
 - child 1 index is 2i
 - child 2 index is 2i + 1
 - if we know child index (i) then
 - parent index is floor(i/2)



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Matlab built in 'issorted

Easy check if an array is sorted can be done with <code>issorted</code> which returns true or false.

```
>> x=[1,2,3];
>> issorted(x)
ans =
```

issorted checks only for ascending order, for example

```
>> x=[3,2,1];
>> issorted(x)
ans =
```

Recall that '0' is equivalent of false in Matlab

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