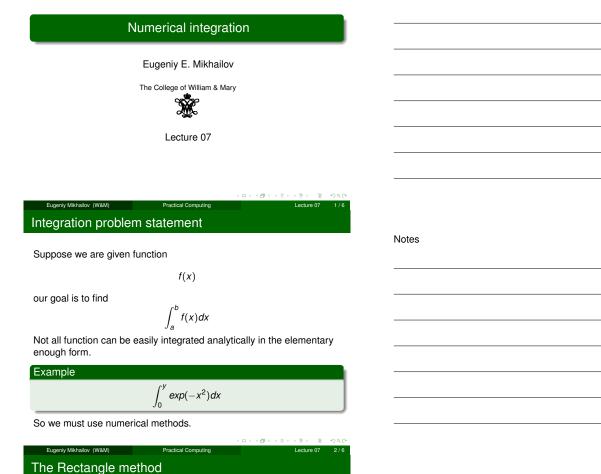
Notes



Lecture

Recall the Riemann integral definition our goal is to find

$$\int_{a}^{b} f(x) dx = \lim_{N \to \infty} \sum_{i=1}^{N-1} f(x_i) h$$

where *N* is the number of points, h = (b - a)/(N - 1) is the distance between points.

The Rectangle method continued

Riemann rule is almost direct recipe.

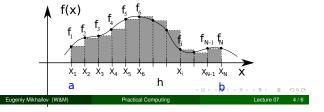
Rectangle method

ugeniy Mikhailov (W&M)

$$\int_{a}^{b} f(x) dx \approx \sum_{i=1}^{N-1} f(x_{i})h, \text{ where } h = \frac{b-a}{N-1} \text{ and } x_{i} = a + (i-1)h$$

Practical Computing

We just need to remember about round off errors so h should not be too small or equivalently N should not be to big.

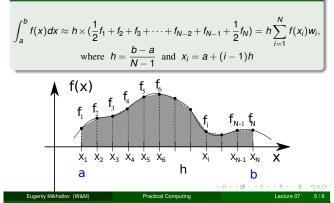


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Trapezoidal method

Trapezoidal method



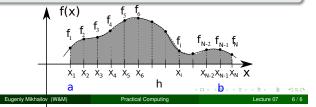
Simpson method

Simpson method - approximation by parabolas

$$\int_{a}^{b} f(x) dx \approx h \frac{1}{3} \times (f_{1} + 4f_{2} + 2f_{3} + 4f_{4} + \dots + 2f_{N-2} + 4f_{N-1} + f_{N})$$

= $h \sum_{i=1}^{N} f(x_{i}) w_{i}$, where $h = \frac{b-a}{N-1}$ and $x_{i} = a + (i-1)h$

note that N must be in special form N = 2k + 1 i.e. odd



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