

# Diodes.

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Lecture 05

# Midterm exam

Where: In the lab

When: During the first hour of the lab

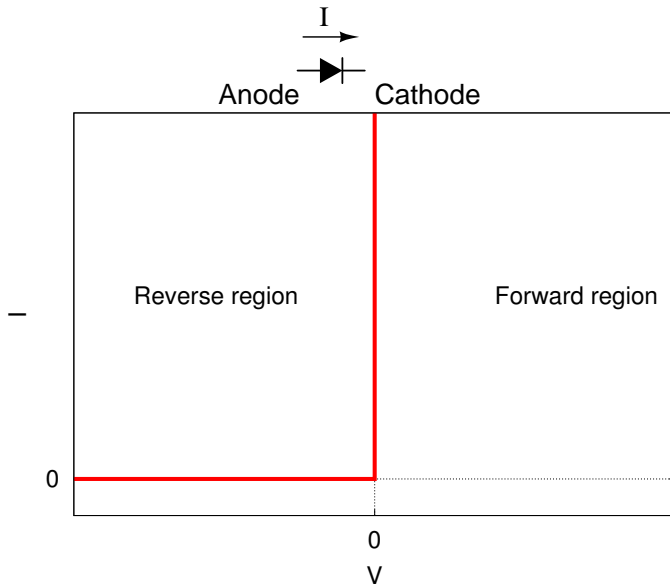
Material:

- everything from first 4 weeks of class
- Resistors, capacitors, inductors, and transformers.
- Kirchhoff's laws
- Complex impedances.
- Thévenin's theorem
  - Source impedance and voltage
- Voltage divider in various forms
- Filters

Lab will follow the midterm.

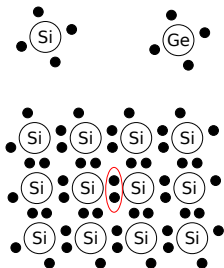
You can skip design exercise preparation prior to the lab. However, at the time of log book submission it must be fully done. Treat it as a home work.

# Ideal diode



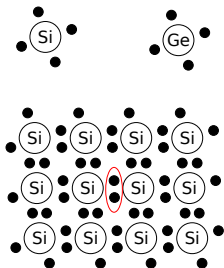
# Semiconductors and doping

## Pure semiconductor

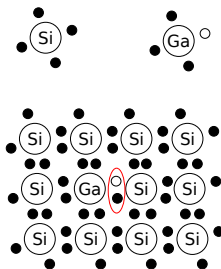


# Semiconductors and doping

Pure semiconductor

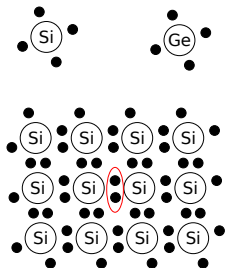


P-doped

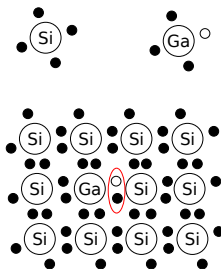


# Semiconductors and doping

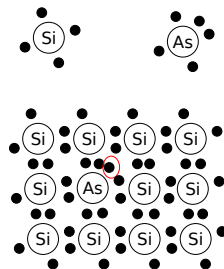
Pure semiconductor



P-doped

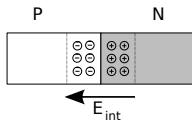


N-doped



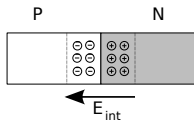
# PN-junction

No bias

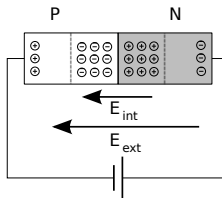


# PN-junction

No bias



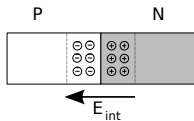
Reverse bias



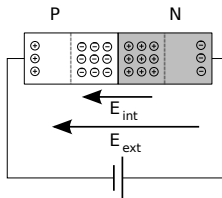


# PN-junction

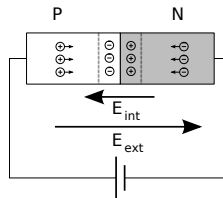
No bias



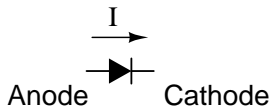
Reverse bias



Forward bias



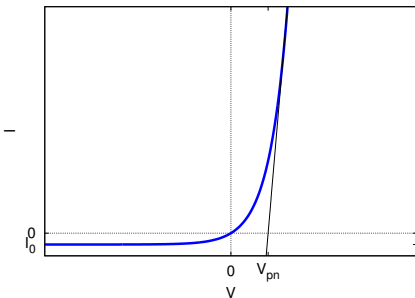
# Real diode



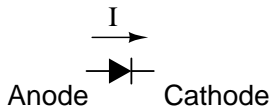
$$I(V) = I_0 \left( e^{V/(nV_T)} - 1 \right)$$

## Typical parameters

- saturation current  
 $I_0 = 1 \text{ nA}$
- thermal voltage  
 $V_T = \frac{kT}{q} = 25.85 \text{ mV at } 300 \text{ K}$
- emission coefficient  
 $n = 1..2$



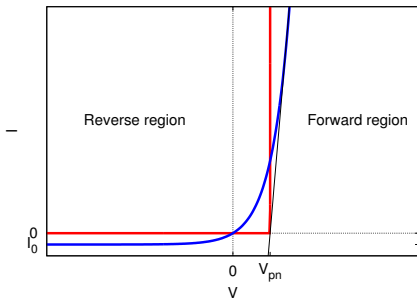
# Real diode



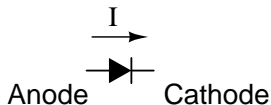
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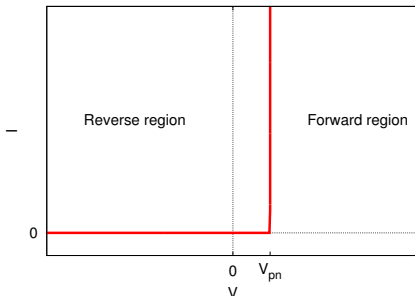


# Simplified diode

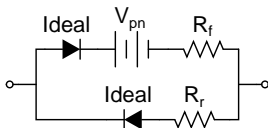


$V_{pn}$  diode P-N junction opening voltage

- $V_{pn} = 0.6$  V for Si
- $V_{pn} = 0.3$  V for Ge



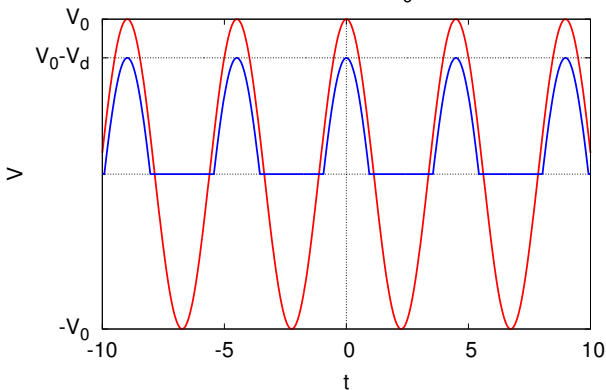
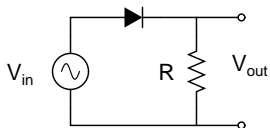
A bit more realistic diode ( $R_r \gg R_f$ )



# Diodes applications

- Circuit Protection
- Rectification
  - current gate
  - half wave rectifier
  - full wave rectifier
  - Power Supplies
- Frequency manipulation
  - Frequency multiplier
  - Mixers
- and more ...
  - Voltage clamps
  - light emitting diodes (LED)
  - photo-diode

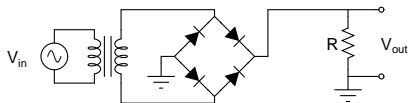
# Half-wave rectifier, current gate



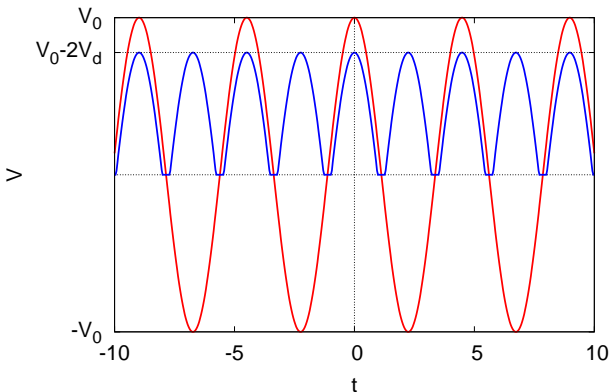
$V_{in}(t) = V_0 \cos(\omega t)$  ———

$V_{out}(t)$  ———

# Full-wave rectifier: $V_{in} \gg V_d \rightarrow V_{out} \approx |V_{in}|$



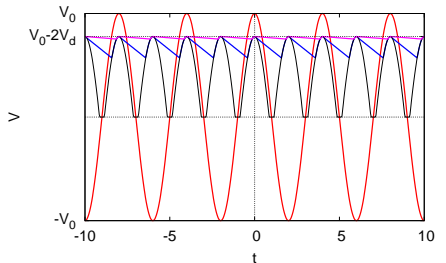
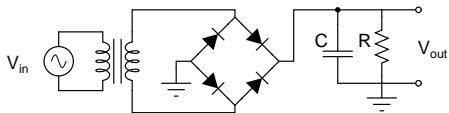
Why  
 $\max(V_{out}) = V_0 - 2V_d$  ?



$V_{in}(t) = V_0 \cos(\omega t)$  — red line

$V_{out}(t)$  — blue line

# Full-wave rectifier filtered - power supply



$V_{in}(t) = V_0 \cos(\omega t)$  — red line  
 $V_{out}(t), C1$  — blue line  
 $V_{rec}(t)$  — black line  
 $V_{out}(t), C2 > C1$  — magenta line

Ripples size

$$V(t) = \frac{Q(t)}{C} = \frac{Q_{max} - \int_0^t I dt}{C}$$

$$= V_{max} - \int_0^t \frac{I}{C} dt$$

$$\Delta V = V_{max} - V(t) = \int_0^t \frac{I}{C} dt$$

$$I \leq I_{max} = \frac{V_{max}}{R}$$

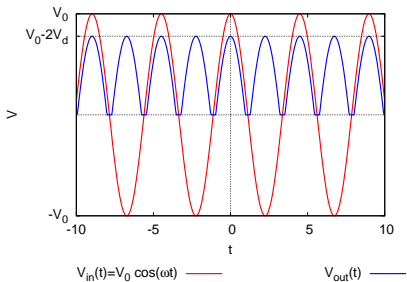
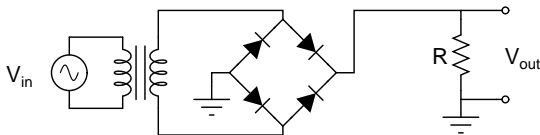
$$t \leq T = \frac{1}{2f_{in}}$$

$$T \ll RC$$

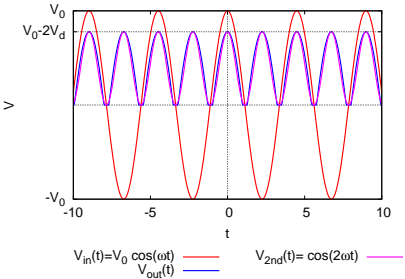
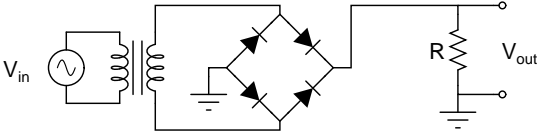
$$\Delta V \leq \frac{V_{max}}{2RCf_{in}}$$



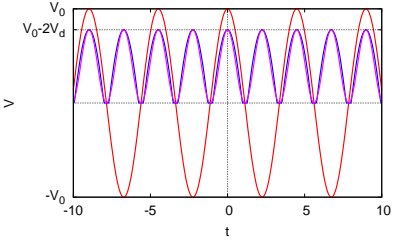
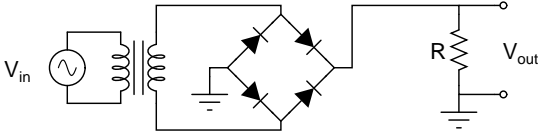
# Full-wave rectifier as Frequency doubler



# Full-wave rectifier as Frequency doubler



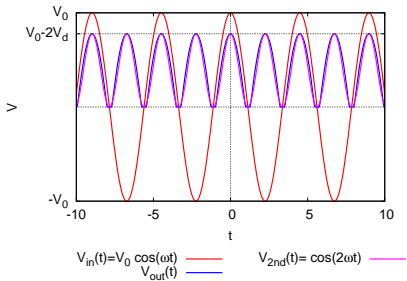
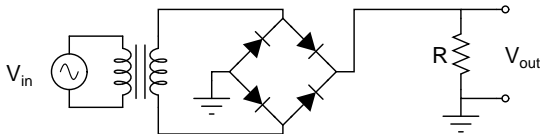
# Full-wave rectifier as Frequency doubler



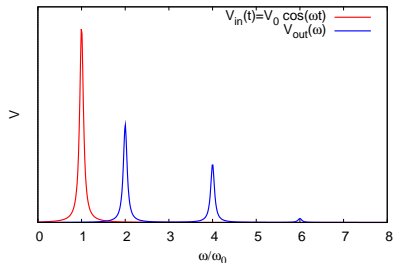
FFT  
⇒

$V_{in}(t) = V_0 \cos(\omega t)$  — red line  
 $V_{out}(t)$  — blue line  
 $V_{2nd}(t) = \cos(2\omega t)$  — purple line

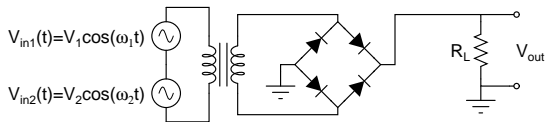
# Full-wave rectifier as Frequency doubler



FFT  
→



# Full-wave rectifier as Frequency adder



$$\begin{aligned}V_{out}(t) &= |V_{in}(t)| = \sqrt{V_{in}^2(t)} = \sqrt{(V_1 \cos(\omega_1 t) + V_2 \cos(\omega_2 t))^2} \\ &= \sqrt{V_1^2 \cos^2(\omega_1 t) + 2V_1 V_2 \cos(\omega_1 t) \cos(\omega_2 t) + V_2^2 \cos^2(\omega_2 t)}\end{aligned}$$

Assuming  $V_1 \gg V_2$

$$\begin{aligned}V_{out}(t) &\approx \sqrt{V_1^2 \cos^2(\omega_1 t) + 2V_1 V_2 \cos(\omega_1 t) \cos(\omega_2 t) + \cancel{V_2^2 \cos^2(\omega_2 t)}} \\ &\approx V_1 \left( \cos(\omega_1 t) + \frac{V_2}{V_1} \cos(\omega_1 t) \cos(\omega_2 t) \right) \\ &\approx V_1 \left( \cos(\omega_1 t) + \frac{V_2}{V_1} \frac{\cos((\omega_1 + \omega_2)t) + \cos((\omega_1 - \omega_2)t)}{2} \right)\end{aligned}$$