Notes

Data interpolation

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Lecture 23

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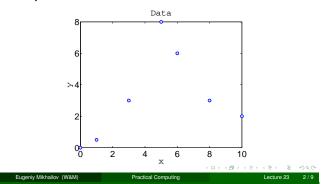
Lecture 23

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Eugeniy Mikhailov (W&M) Data interpolation - filling the voids

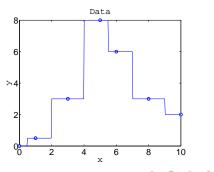
Very rarely there is enough data. Often taking a data point takes a lot of time or it is expensive. But we would like to have some presentation of the system in the voids.

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Nearest neighbor interpolation

The name says it, for each interpolated point x_{interpolated} find its nearest neighbor along the x_i axis in the data set and use its y_i value.

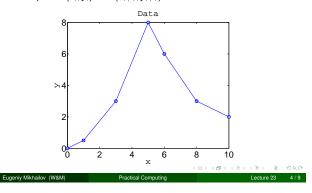


Linear interpolation

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We will split our data set with N points to N - 1 intervals and interpolate the values in the given interval as a line passing through the border points (x_i, y_i) and (x_{i+1}, y_{i+1})

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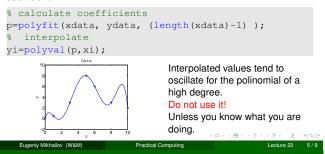
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Polynomial fit

You can always find a polynomial of N-1 degree passing through N data points.

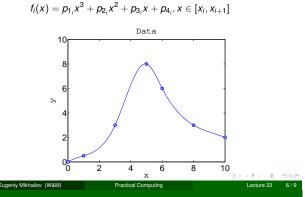
 $y(x) = p_1 x^n + p_2 x^{n-1} + \dots + p_n x + p_{n+1}$

Matlab has the <code>'polyfit'</code> function which returns the polynomial coefficient.



Cubic spline interpolation

We will interpolate N data points by a polynomial of 3rd degree for each i_{th} interval between data point



Cubic spline interpolation demystified

We will interpolate N data points by a polynomial of 3rd degree for each i_{th} interval between data point

$$f_i(x) = p_{1_i}x^3 + p_{2_i}x^2 + p_{3_i}x + p_{4_i}, x \in [x_i, x_{i+1}]$$

Interpolation must pass through data points

 $f_i(x_i) = y_i$ $f_i(x_{i+1}) = y_{i+1}$

Two data points (at the interval border) are not enough to set equations for 4 polynomial coefficients.

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So we will request twice continuous differentiable

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At the end points second derivative must be set to 0 (so called natural cubic spline)

 $\begin{array}{rcl} f_i'(x_{i+1}) &=& f_{i+1}'(x_{i+1}) \\ f_i''(x_{i+1}) &=& f_{i+1}''(x_{i+1}) \end{array}$

natural cubic spline) $f_1''(x_1) = 0$

Matlab built in interpolation

Use matlab interpl(xdata, ydata, xi, method) for some of above methods Where method could be 'nearest' Nearest neighbor interpolation 'linear' Linear interpolation (default) 'spline' Cubic spline interpolation other see more in help Notes

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Do not extrapolate!!! Unless you have a physical model of the process.

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