Sorting continued

Eugeniy E. Mikhailov

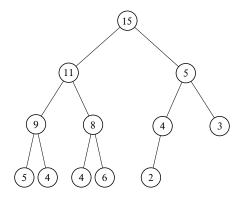
The College of William & Mary



Lecture 09

Heap

Heap is a structure where parent element is larger or equal to its children.



The top most element of the heap is called root.

Heap sorting method

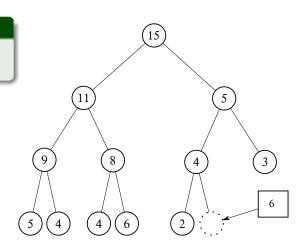
- Fill the heap from the input vector elements
 - take the element and place it at the bottom of the heap
 - 2 sift-up (bubble up) this element
 - do the same with the next element
- remove the root element since it is the largest
- rearrange the heap i.e. sift-down
 - take the last bottom element
 - place it at the root
 - check if parent is larger then children
 - find the largest child element
 - if the largest children is larger then parent swap them and repeat the check
- repeat step 2 until no elements left in the heap

Heap sorting complexity $\mathcal{O}(N \log_2 N)$



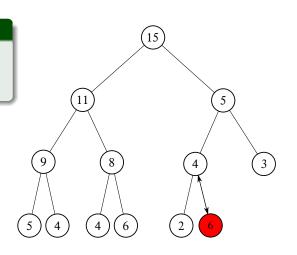
Step 1

Place new element at the bottom of the heap



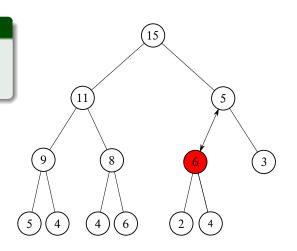
Step 2

Check if parent is larger then child. If so swap them and repeat step 2.



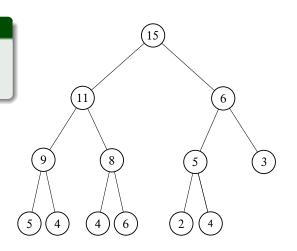
Step 2

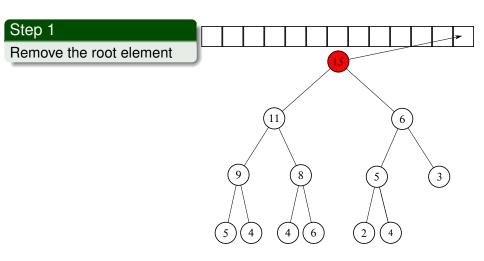
Check if parent is larger then child. If so swap them and repeat step 2.



Step 2

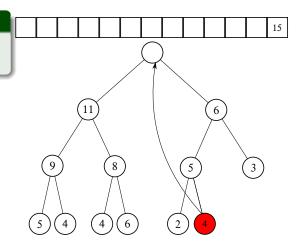
Check if parent is larger then child. If so swap them and repeat step 2.





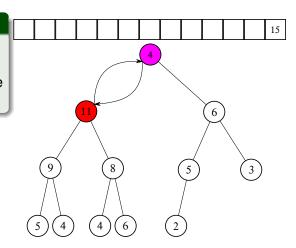
Step 2

Place the last element of the heap to the root



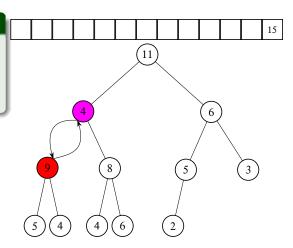
Step 3

Check if parent is smaller than the largest child. If so swap and repeat step 3 else go to step 1

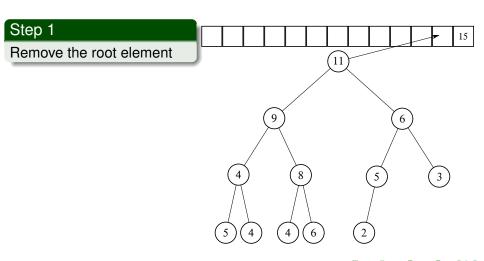


Step 3

Check if parent is smaller than the largest child. If so swap and repeat step 3 else go to step 1



Sequence repeats



Vector heap representation

- Heap nodes are numbered consequently these numbers represent the node position in the vector.
- notice that parent and children have very simple relationship
 - if parent node index is i
 - child 1 index is 2i
 - child 2 index is 2i + 1
 - if we know child index (i) then
 - parent index is floor(i/2)

