

## Physics 722, Spring 2021

### Problem Set 7

Due Thursday, April 1.

#### 1. *Renormalizability*

a) We argued that in four spacetime dimensions, a theory of spin-0 and spin-1/2 fields is generally not renormalizable if the Lagrangian contains operators of mass-dimension  $> 4$ , and is renormalizable if it contains all operators of positive mass-dimension  $\leq 4$ .

What is the corresponding statement in  $d$  spacetime dimensions?

b) Is a theory of fermions with a  $(\bar{\psi}\psi)^2$  interaction renormalizable in four dimensions? In three dimensions?

c) Assuming that the same rule applies to gauge theories, do you expect QED to be renormalizable in 4+1 dimensions?