Physics 722, Spring 2016Problem Set 7Due Thursday, March 31.

Renormalizability

a) We argued that in four spacetime dimensions, a theory of spin-0 and spin-1/2 fields is generally not renormalizable if the Lagrangian contains operators of mass-dimension > 4, and is renormalizable if it contains all operators (possibly constrained by symmetries) of mass-dimension ≤ 4 . What is the corresponding statement in d spacetime dimensions?

b) Is a theory of fermions with a $(\overline{\psi}\psi)^2$ interaction renormalizable in four dimensions? In three dimensions?

c) Assuming that from the perspective of momentum power counting, gauge fields behave like scalars, do you expect QED to be renormalizable in 4+1 dimensions?