Test 3

Name: _____

This test is administered under the rules and regulations of the Honor Code of William & Mary.

Signature: _____

Problem Session (circle one):

Wed. 9:00 am (Prof. Cooke)
Wed. 3:00 pm (Prof. Aubin)
Thurs. 1:00 pm (Prof. Sher)
Thurs. 3:30 pm (Prof Krakauer)
Tues. 1:00 pm (Prof. Mikhailov)
Thurs. 2:00 pm (Prof. Vahala)

- 1. _____ (25 points)
- 2. _____ (25 points)
- 3. _____ (25 points)
- 4. _____ (25 points)

Total

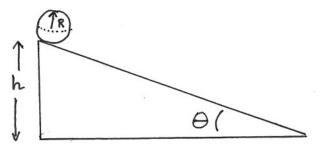
Problem 1.

Your clothes washer is rotating at a rate of 800 revolutions per minute during the spin cycle. The power is switched off, and it then smoothly slows down to come to a complete stop; this takes 10 seconds.

- a) What is the magnitude of its angular acceleration?
- b) How many rotations did it complete after the power was switched off?

Problem 2.

A solid bowling ball of mass M and radius R rolls (without slipping, and starting from rest) down an incline with an angle θ from an initial height of h. The moment of inertia of a solid sphere about an axis through its center is $I = \frac{2}{5}MR^2$.



a) What is the magnitude of the angular velocity of the sphere when it reaches the bottom of the incline? Give your answer in terms of any of these: M, R, θ, h, g .

b) If, instead, a basketball of the same radius R was rolled down the incline (without slipping), would it reach the bottom of the incline faster, slower, or in the same time as the bowling ball? Briefly explain why. The moment of inertia of a hollow sphere about an axis through its center is $I = \frac{2}{3}MR^2$.

Problem 3.

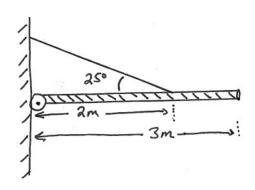
A uniform thin rod of length 3 m and mass 15 kg is attached to a wall by a hinge and is held horizontal and stationary by a rope attached to the rod a distance of 2 m from the wall, at an angle of 25° .

a) Find the magnitude of the tension in the rope.

b) Find the force (horizontal and vertical components) exerted on the rod by the hinge.

c) If the rope is suddenly cut, find the initial angular accel-

eration (magnitude and direction) of the rod as it begins to rotate about the hinge. Note: the moment of inertia of a thin rod about an axis through one end is $I = \frac{1}{3}ML^2$.



Problem 4.

One day, humanity may colonize Mars.

a) Assume you wish to place a communications satellite in orbit around Mars. What must the radius of the satellite's orbit be such that it could stay fixed in the Martian sky (above a particular location on the surface of Mars) as Mars rotates? In other words, so that it orbits Mars once per Martian day.

b) What is the value of the gravitational acceleration " g_{mars} " (due to Mars' gravity) that this satellite would experience while in orbit?

Possibly useful values: Radius of Mars = 3400 km; mass of Mars = $6.4 \times 10^{23} \text{ kg}$; length of the Martian day = 24.6 hours; length of the Martian year = 687 days; mass of the satellite = 42 kg; revenue of the film "The Martian" in its first weekend of release = \$55 million.