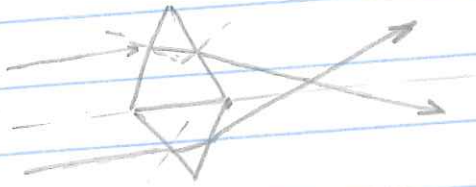
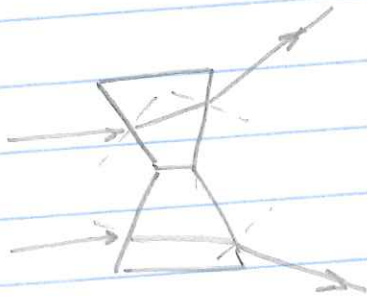


Reminder: a flat slab of material displaces beams, without changing their directions.

A prism can bend them



beams are directed toward the center (converging)



beams are directed away from the center (diverging)

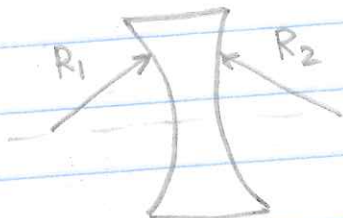
Typical lens consists of two pieces of a spherical surfaces, or one flat and one spherical surfaces



converging lens

An optical axis passes through the centers of the two "spheres"

$$\frac{1}{f} = (n-1) \left( \frac{1}{R_1} + \frac{1}{R_2} \right)$$



diverging lens

This formula works for all cases, but

$R > 0$

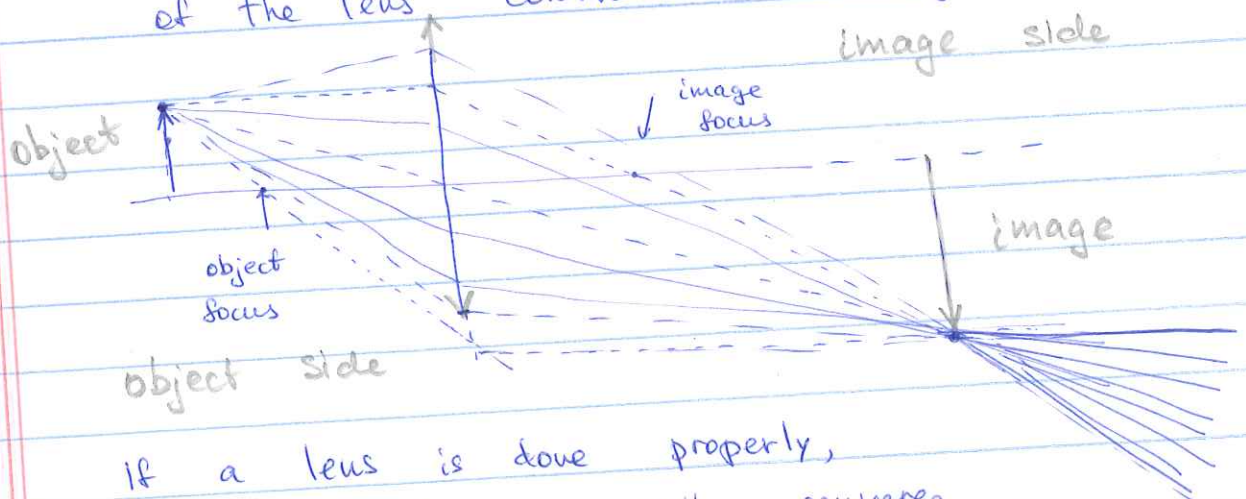
thicker at the center

$R < 0$

thinner at the center

For calculations we are going to think about ideal thin lenses. How do we know where the image is going to be

1. a beam which is parallel to the optical axis will go through the <sup>image</sup> focus
2. a beam which originates from the <sup>object</sup> focal point is going to continue parallel to the optical axis
3. The beam that travels through the center of the lens continues unchanged



If a lens is done properly, all the beams will converge in a point

on a computer make diagrams for more points to show how the image is formed.

lens equation

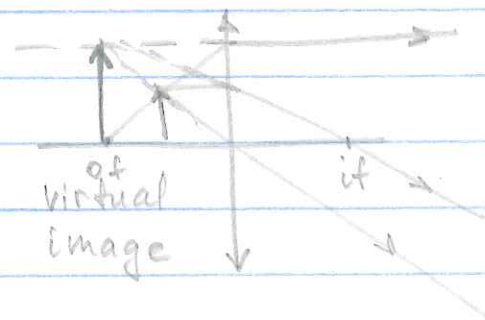
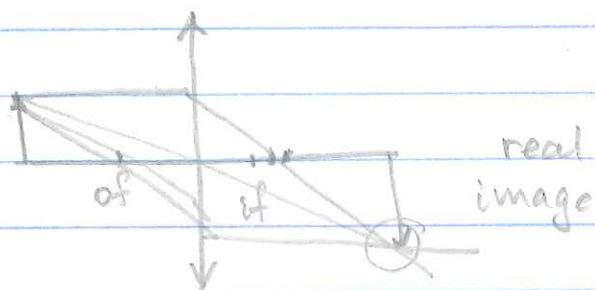
$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}$$

$$m = -\frac{d_i}{d_o} = \frac{h_i}{h_o}$$



If the rays emitted from an object, converge after lens, they form a real image

If they do not converge, but can be traced back to a point behind the lens, they form a virtual image



Lens formula

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}$$

$d_o$  - distance from the lens to the object

$d_i$  - distance from the lens to the image

$d_o, d_i, f$  can be both positive or negative

$d_o > 0$  an object is on the object side

$d_i > 0$  a ~~real~~ image is on the image side

$d_i < 0$  an image on the object side

For the positive lens  $f > 0$ , so an object/image & focus are at the corresponding side; for a negative lens an object focus is on the image side, (after the lens) and the image focus is on the object half.