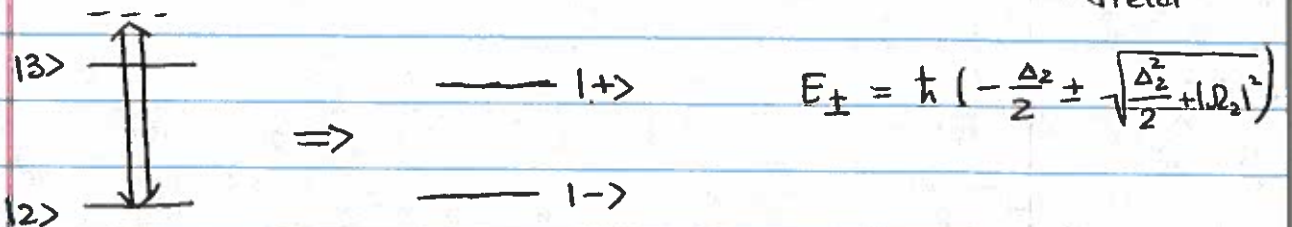


Physical interpretation of two-photon resonances

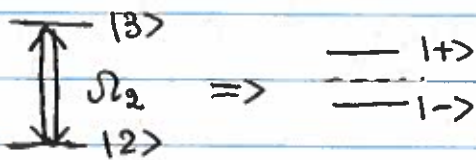
1: Dressed-state picture for the atom + control field



Resonant case $\Delta_2 = 0$

$$E_{\pm} = \pm \hbar |\Omega_2|$$

$$|\pm\rangle = \frac{1}{\sqrt{2}} \left(\frac{|\Omega_2|}{\Omega_2} |2\rangle \pm |3\rangle \right)$$



Far-detuned case $\Delta_2 \gg |\Omega_2|$

$$E_{-} \approx -\hbar \Delta_2 - \hbar \frac{|\Omega_2|^2}{\Delta_2}$$

$$|-\rangle \approx |3\rangle + \underbrace{\frac{|\Omega_2|^2 / \Delta_2}{\Delta_2}}_{\ll 1} |2\rangle$$

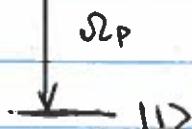
$$E_{+} \approx \hbar \frac{|\Omega_2|^2}{\Delta_2}$$

$$|+\rangle \approx |2\rangle - \underbrace{\frac{\Omega_2}{\Delta_2}}_{\ll 1} |3\rangle$$

① Off-resonant control field + probe

$|-\rangle \approx |3\rangle$ - strongly decaying, width $\sim \gamma_{31}$

$|+\rangle \approx |2\rangle$ - no/small decay, width $\sim \gamma_{21}$

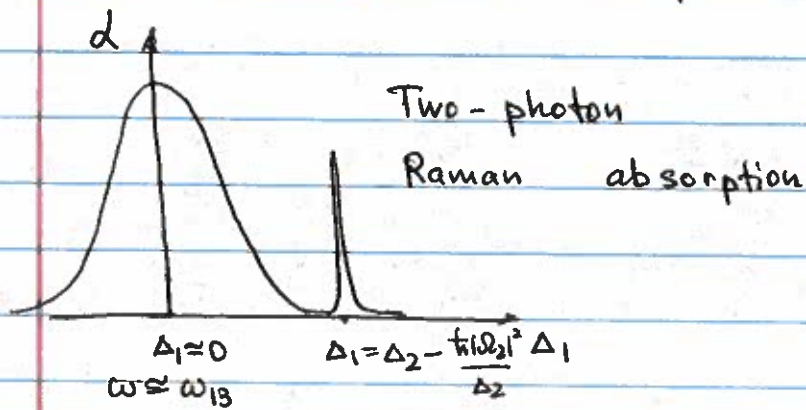


Two absorption resonances

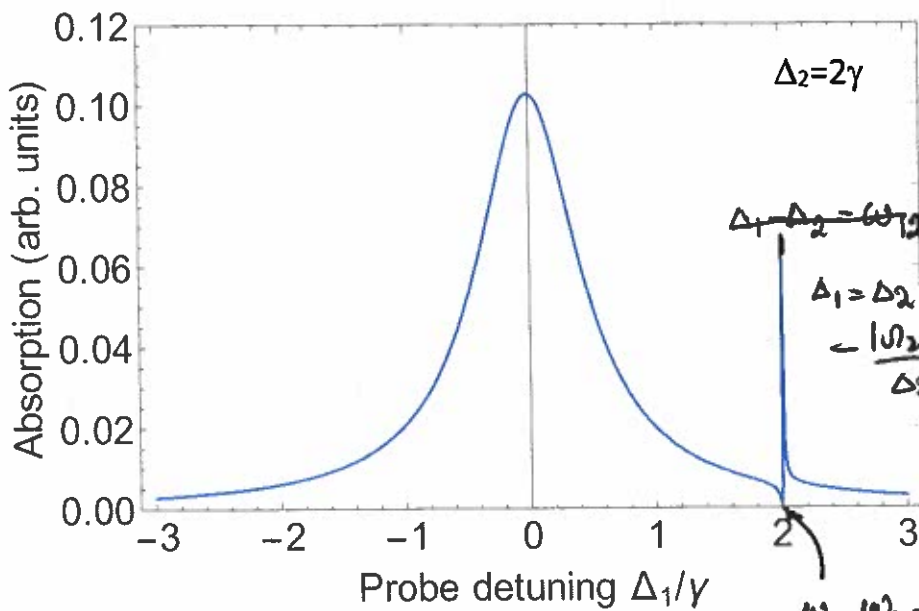
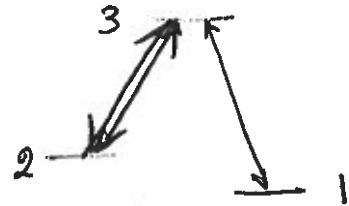
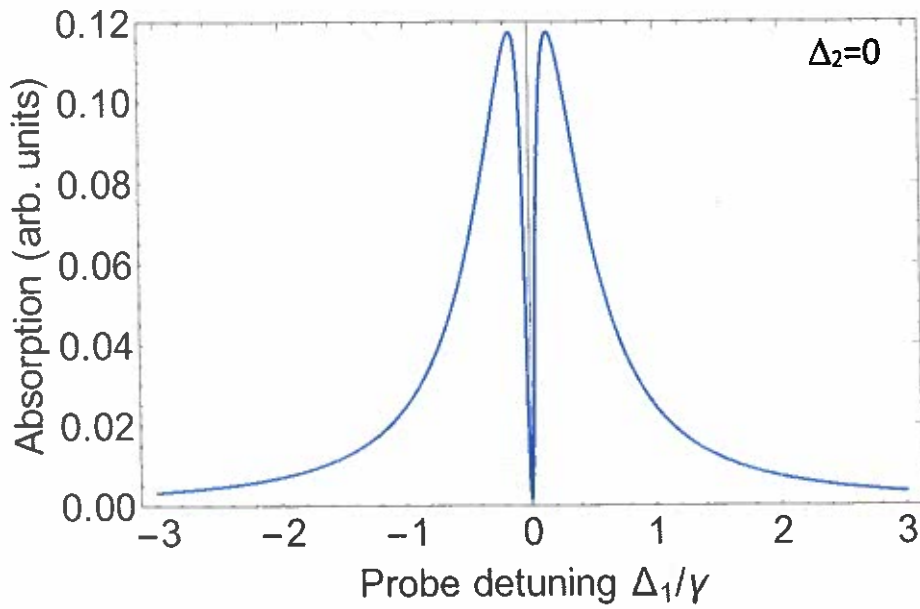
$|1\rangle \rightarrow |+\rangle \Rightarrow$ almost like $|1\rangle \rightarrow |3\rangle$, "normal" one-photon absorption

$|1\rangle \rightarrow |-\rangle$

$|1\rangle \rightarrow |+\rangle \Rightarrow$ almost $|1\rangle - |2\rangle$ coupling
via a two-photon transition

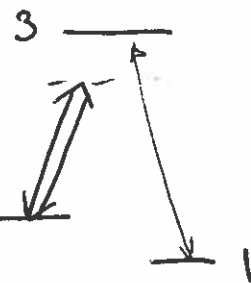


Two-photon process enables transitions b/w two ground states with minimum involvement of the excited state (~~is~~ virtually zero population of the excited state, thus the properties of the probe field susceptibility determined by the parameters of the two ground states $|1\rangle$ & $|2\rangle$).

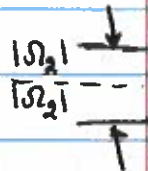


$\Delta_1 - \Delta_2 = \omega_{12}$
 $\Delta_1 = \Delta_2 + \omega_{12}$
 $= \frac{|\omega_{12}|^2}{\Delta_2}$

$\omega_1 = \omega_2 = \omega_{12}$

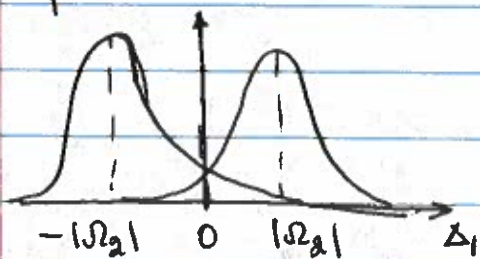


Resonant case $\Delta_2 = 0$ (Ω_2 - real)



$|+\rangle = \frac{1}{\sqrt{2}} (|2\rangle + |3\rangle)$
 $|-\rangle = \frac{1}{\sqrt{2}} (|2\rangle - |3\rangle)$

Naively, we would expect observing two overlapping absorption peaks for the probe field



Autler - Towns splitting
Observed for low/no ground-state coherence

However, if the two-photon interaction is coherent, the probe interactions with the two symmetric transitions ($\Delta_2 = \Delta_1 = 0$) destructively interfere, eliminating possibility of excitation to the state $|3\rangle$ and absorption. (Actually, such destructive interference exists for any Δ_2 , but it is less intuitive)

