

# Quantum electrodynamics

Interactions of charged particles + quantized e-m field

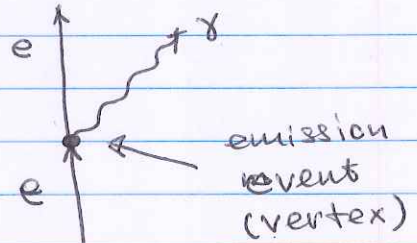
Electrons interact via exchange of virtual photons

Feynman diagrams: visualization of e-m interactions

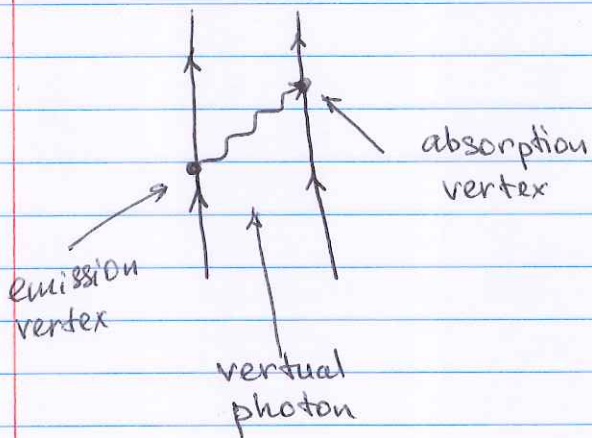
world line of a stationary  
electron



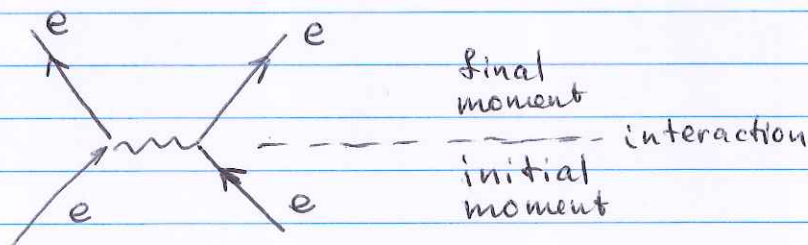
electron emitting a photon



(impossible process by itself)



Two electrons became aware of each other (interacted) via the exchange of a (virtual) photon



Charged particles - solid line with arrows

$\uparrow$   $e$   
(particle)

$\downarrow$   $e^+$   
(anti-particle)

Photons - wavy lines. When attached to a vertex they designate absorption or emission

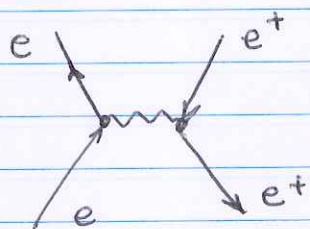


Region below the vertex - initial state  
—  $\leftarrow$  — above —  $\rightarrow$  — - final state

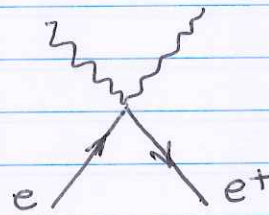
Any line b/w two vertices represent a virtual particle

Any process that follow these rules, and whose final state and initial state obey conservation laws is a possible physical process!

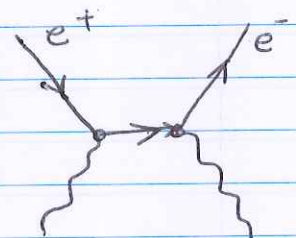
Possible electron-positron interaction



Coulomb interaction



electron-positron annihilation

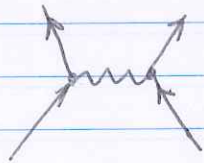


electron-positron pair production

Feynman diagrams are more than funny pictures, they are prescriptions for very precise calculations.

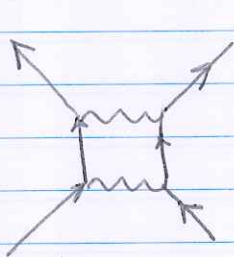
For example - e-e scattering

First-order effect (involves 1 photon)



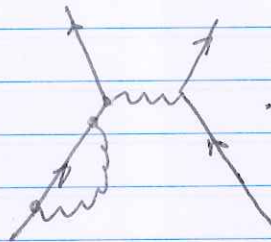
one possible contribution

Second-order effect (involves 2 photons)

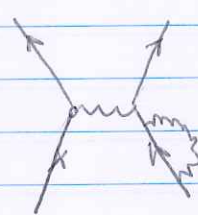


two-photon exchange

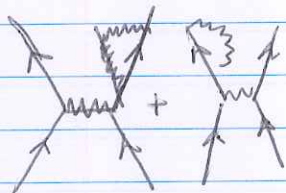
and



+

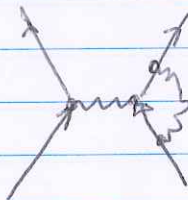


+



electron self-interaction

and

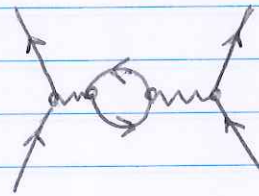


+



vertex correction

and



vacuum polarization

It is necessary to Each pair of vertices in calculations introduces a factor of  $\alpha = 1/137$  (fine structure constant)

Thus, higher order processes give weaker contributions compare to the first order effects. Still, they are necessary to conduct precise measurements

For example: electron magnetic moment

$$\vec{\mu} = \frac{q}{2m} \vec{S} \vec{B} - \text{classical (incorrect) assumption}$$

$$\vec{\mu} = g \frac{q}{2m} \vec{S} \vec{B} \quad g=2 \text{ from Dirac equation}$$

experiment

$$g = 2.0023193048 \pm 4 \cdot 10^{-10}$$

theory

$$g = 2.0023193048 \pm 8 \cdot 10^{-10}$$