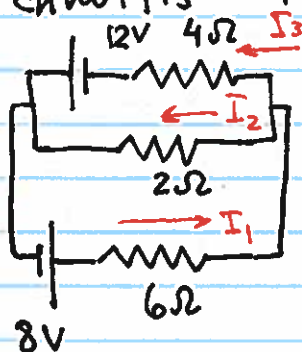
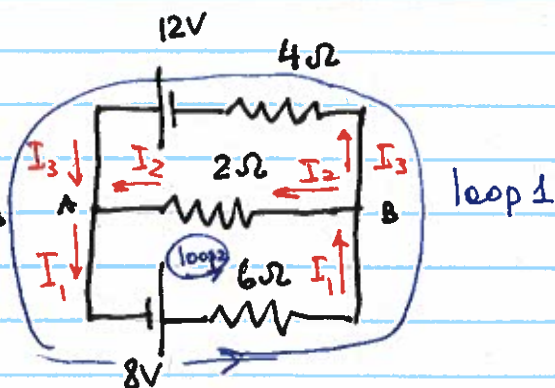


What if a complex circuit with multiple batteries cannot be simplified as a single loop?

Kirchhoff's Rules



same as



Kirchhoff's rule #1

At any junction, the sum of currents flowing in is equal to the sum of currents flowing out

$$\underline{I_1 = I_2 + I_3}$$

Kirchhoff's rule #2

Sum of all potential differences across all elements around any closed loop must be zero

$$\begin{aligned} V_A - V_B &= 12V + 4\Omega \cdot I_3 \\ &= 2\Omega \cdot I_2 \\ &= +8V - 6\Omega I_1 \end{aligned}$$

$$\text{loop 1: } 8V - 6\Omega \cdot I_1 - 4\Omega \cdot I_3 + 12V = 20V - 6\Omega \cdot I_1 - 4\Omega \cdot I_3 = 0$$

$$\text{loop 2: } 8V - 6\Omega \cdot I_1 - 2\Omega \cdot I_2 = 0$$

Three equations to find three currents

$$\begin{cases} I_1 = I_2 + I_3 \\ 20V - 6\Omega \cdot I_1 - 4\Omega \cdot I_3 = 0 \\ 8V - 6\Omega I_1 - 2\Omega I_2 = 0 \end{cases}$$

$$I_1 = \frac{18}{11} \text{ A} \quad I_2 = -\frac{10}{11} \text{ A} \quad I_3 = \frac{28}{11} \text{ A}$$

Actually, the current through 2Ω resistor is in the opposite direction.