

Giant Edelstein effect in topological-insulator–graphene heterostructures

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The control of a ferromagnet's magnetization via only electric currents requires the efficient generation of current-driven spin torques. In magnetic structures based on topological insulators (TIs) current-induced spin-orbit torques can be generated. Here we show that the addition of graphene, or bilayer graphene, to a TI-based magnetic structure greatly enhances the current-induced spin-density accumulation and significantly reduces the amount of power dissipated. We find that this enhancement can be as high as a factor of 100, giving rise to a giant Edelstein effect. Such a large enhancement is due to the high mobility of graphene (bilayer graphene) and to the fact that the graphene (bilayer graphene) sheet very effectively screens charge impurities, the dominant source of disorder in topological insulators. Our results show that the integration of graphene in spintronics devices can greatly enhance their performance and functionalities.

DOI: [10.1103/PhysRevB.96.235419](https://doi.org/10.1103/PhysRevB.96.235419)**I. INTRODUCTION**

The ability to generate and control spin currents in condensed-matter systems has led to several discoveries of great fundamental and technological interest [1,2]. In recent years the discovery of whole new classes of materials with strong spin-orbit coupling, such as topological insulators (TIs) [3,4], has allowed the realization of novel basic spin-based phenomena [5–8].

In a system with spin-orbit coupling (SOC), a charge current I can induce a spin-Hall effect (SHE) [2], i.e., a pure spin-polarized current. A companion effect to the SHE, also arising from the SOC, is the inverse spin-galvanic effect (ISGE), where a current induces a nonequilibrium uniform spin accumulation [2,9–11]. In a magnetic system this current-driven spin accumulation results in a spin-orbit torque (SOT) acting on the magnetization \mathbf{M} and therefore can be exploited to realize current-driven magnetization dynamics. The SOT $\boldsymbol{\tau}_{SO}$ can be either an (anti)damping torque [2,12], i.e., have the same functional form as the Gilbert damping term, or *fieldlike* [2], i.e., have the form $\boldsymbol{\tau}_{SO} = \gamma \mathbf{B}_{SO} \times \mathbf{M}$, where \mathbf{B}_{SO} is an effective spin-orbit field and γ is the gyromagnetic ratio. The presence of a current-driven SOT on the surface of TIs has been predicted [13–17], and it has been recently measured in TI-ferromagnet bilayers [18] and magnetically doped TIs [19].

The two-dimensional nature of single-layer graphene (SLG) and bilayer graphene (BLG) [20–22] and the fact that their room-temperature mobilities are higher than in any other known material [23] make them extremely interesting

for transport phenomena. However, the SOC in graphene is extremely small, and as a consequence, graphene alone is not very interesting for spintronics applications, except as a spin conductor. Several methods have been proposed to induce larger SOC in graphene [24]. Recent experiments on TI-graphene heterostructures seem to demonstrate the injection of spin-polarized current from a TI into graphene [25,26].

In this work we show that the combination of a particular class of three-dimensional (3D) TIs and graphene allows the realization of devices in which a charge current induces a spin-density accumulation that can be up to a factor of 100 larger than in any previous system, i.e., a *giant Edelstein effect*. We find that for most of the experimentally relevant conditions considered, the SOT in TI-graphene van der Waals (vdW) heterostructures should be higher than the already very large values observed in TI-ferromagnet bilayers [18] and magnetically doped TIs [19]. In Ref. [18], for $I = 7.7$ mA, a $B_{SO} = 3 \times 10^{-2}$ mT was measured; in Ref. [19], for $I = 4$ μ A, $B_{SO} = 80$ mT was measured [27]. Assuming that our work is able to capture the key elements affecting the SOT in TI-graphene systems, we find that in these systems the SOT could be ten times larger than the values found in Refs. [18,19]. We also find that TI-SLG and TI-BLG systems have conductivities much higher than TI surfaces and would therefore allow the realization of spintronics effects with dramatically lower dissipation than in TIs alone.

The rest of the paper is organized as follows: in Sec. II we introduce the effective model for the TI-graphene heterostructure, describe the treatment of disorder, and outline

the calculation of the current-induced spin-density response function; in Sec. III we present our results. Finally, in Sec. IV we present our conclusions.

II. THEORETICAL FRAMEWORK

In vdW heterostructures [28], the different layers are held together by vdW forces. This fact greatly enhances the type of heterostructures that can be created given that the stacking is not fixed by the chemistry of the elements forming the heterostructure. With $a = 2.46 \text{ \AA}$ being the lattice constant of graphene and a_{TI} being the lattice constant of the 111 surface of a TI in the tetradymite family, we have $a_{TI}/a = \sqrt{3}(1 + \delta)$, where $\delta < 1\%$ for Sb_2Te_3 , $\delta = -3\%$ for Bi_2Se_3 , and $\delta = 3\%$ for Bi_2Te_3 . As a consequence, graphene and the 111 surface of Sb_2Te_3 , Bi_2Se_3 , and Bi_2Te_3 , to very good approximation, can be arranged in a $\sqrt{3} \times \sqrt{3}$ commensurate pattern [29–31]. When the stacking is commensurate, the hybridization between graphene's and the TI's surface states is maximized. This property of graphene, combined with its high mobility, its intrinsic two-dimensional nature, and its ability at finite dopings to effectively screen the dominant source of disorder in TIs, makes graphene the ideal material to consider for creating a TI heterostructure with a very large Edelstein effect.

TI-graphene heterostructures can be formed via mechanical transfer [26,32,33]. As a consequence, the stacking pattern and the shift are fixed by the exfoliation-deposition process and can be controlled [34]. Density functional theory (DFT) results show that the binding energy between graphene and the TI surface depends only very weakly on the rigid shift [29,35–37]. Among the commensurate configurations with free energy close to the minimum, as obtained from DFT calculations [29], we consider the stacking configuration shown in Fig. 1(c). For this configuration, we expect the Edelstein effect to be the smallest because the graphene bands split into Rashba-like bands [see Figs. 1(d) and 1(e)] that give an Edelstein effect with the sign opposite to the one given by TI-like bands [18]. Therefore, to be conservative, in the remainder of this paper we consider both the commensurate case for which the Edelstein effect is expected to be the weakest (i.e., the case in the graphene sublattice symmetry is broken) and the extreme case in which the tunneling strength between the TI and graphene is set to zero.

At low energies, the Hamiltonian for the system can be written as $H = \sum_{\mathbf{k}} \psi_{\mathbf{k}}^\dagger H_{\mathbf{k}} \psi_{\mathbf{k}}$, where $\psi_{\mathbf{k}}^\dagger$ ($\psi_{\mathbf{k}}$) is the creation (annihilation) spinor for a fermionic excitation with momentum \mathbf{k} , and

$$H_{\mathbf{k}} = \begin{pmatrix} \hat{H}_{\mathbf{k}}^{G,K} & 0 & \hat{T}^\dagger \\ 0 & \hat{H}_{\mathbf{k}}^{G,K'} & \hat{T}^\dagger \\ \hat{T} & \hat{T} & \hat{H}_{\mathbf{k}}^{TI} \end{pmatrix}, \quad \hat{T} = \begin{pmatrix} t & 0 & 0 & 0 \\ 0 & 0 & t & 0 \end{pmatrix}, \quad (1)$$

where $\hat{H}_{\mathbf{k}}^{G,K}$ ($\hat{H}_{\mathbf{k}}^{G,K'} = [\hat{H}_{\mathbf{k}}^{G,K}]^*$) is the Hamiltonian describing graphene's low-energy states around the K (K') of the Brillouin zone. For SLG $\hat{H}_{\mathbf{k}}^{G,K} = \hat{H}^{SLG,K}$, and for BLG $\hat{H}_{\mathbf{k}}^{G,K} = \hat{H}^{BLG,K}$. $\hat{H}_{\mathbf{k}}^{TI}$ is the Hamiltonian describing the TI's surface states, and \hat{T} is the matrix describing spin- and momentum-conserving tunneling processes between the graphene layer and the TI's surface [31], with t being the tun-

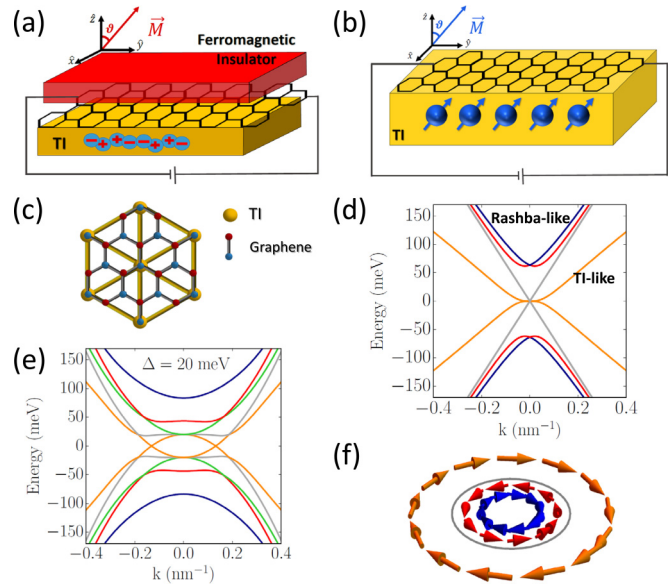


FIG. 1. Sketch of (a) a TI-graphene-FM and (b) a magnetically doped TI-graphene heterostructure. In (a) the random charges are shown. In (b) the spheres represent the magnetic dopant; the random charges are not shown explicitly. (c) Atom arrangement for the commensurate stacking considered. (d) Bands for TI-SLG for $\Delta = 0$, $\delta\mu = 0$. (e) Bands for TI-BLG for $\Delta = 20 \text{ meV}$ and $\delta\mu = 0$. (f) Spin texture on the Fermi surface formed by the bands shown in (d) for $\epsilon_F = 100 \text{ meV}$.

neling strength. The TI's bulk states are assumed to be gapped. This condition is realized, for example, in novel ternary or quaternary tetradymites, such as $\text{Bi}_2\text{Te}_2\text{Se}$ and $\text{Bi}_{2-x}\text{Sb}_x\text{Te}_{3-y}\text{Se}_y$, for which it has been shown experimentally that the bulk currents have been completely eliminated [38–45]. For SLG we have $\hat{H}_{\mathbf{k}}^{SLG,K} = \hbar v_g k \sigma_0 [\cos(\phi_{\mathbf{k}})\tau_x + \sin(\phi_{\mathbf{k}})\tau_y] - \mu_g$, where $v_g \approx 10^6 \text{ m/s}$ is graphene's Fermi velocity, $k = |\mathbf{k}|$, $\phi_{\mathbf{k}} = \arctan(k_y/k_x)$, σ_i and τ_i are the Pauli matrices in spin and sublattice space, respectively, and μ_g is the chemical potential. For BLG we have $\hat{H}_{\mathbf{k}}^{BLG,K} = \hbar^2 k^2 / (2m^*) \sigma_0 [\cos(2\phi_{\mathbf{k}})\tau_x + \sin(2\phi_{\mathbf{k}})\tau_y] - \mu_g$, where $m^* \approx 0.035m_e$ is the electron's effective mass. For the TI's surface states, we have $\hat{H}_{\mathbf{k}}^{TI} = \hbar v_{TI} (k_y \sigma_x - k_x \sigma_y) - \mu_{TI} \sigma_0$, where $v_{TI} \approx v_g/2$ and μ_{TI} is the chemical potential on the TI's surface. In the following the Fermi energy ϵ_F is measured from the neutrality point of the SLG (or the BLG), and $\delta\mu \equiv \mu_{TI} - \mu_g$.

In a magnetically doped TI, below the Curie temperature, the low-energy Hamiltonian for the TI-graphene quasiparticles, Eq. (1), has an additional term, H_{ex} , describing the exchange interaction between the quasiparticles and the magnetization \mathbf{M} . $H_{\text{ex}} = \Delta \int_{\Omega} \hat{\mathbf{m}} \cdot \hat{\mathbf{s}} \, d\mathbf{r} / \Omega$, where Δ is the strength of the exchange interaction, $\hat{\mathbf{m}} \equiv \mathbf{M}/|\mathbf{M}|$, $\hat{\mathbf{s}} \equiv \mathbf{s}/|\mathbf{s}|$, with \mathbf{s} being the TI-graphene spin-density operator, and Ω is the two-dimensional (2D) area of the sample. For a TI-graphene-ferromagnet heterostructure the ferromagnet (FM) will also cause simply the addition of the term H_{ex} to the Hamiltonian for the quasiparticles, Eq. (1), as long as the FM is an insulator and is placed on graphene or bilayer graphene via mechanical exfoliation, likely with a large twist

angle to minimize hybridization. Recent experiments have studied Bi_2Se_3 -EuS systems [46,47]. In the remainder of this paper, for TI-graphene-FM heterostructures we assume the FM is an insulator.

To maximize the effect of the current-induced spin accumulation on the dynamics of the magnetization, it is ideal to have \mathbf{M} perpendicular to the TI's surface. This is the case for magnetically doped TIs such as $\text{Cr}_{2x}(\text{Bi}_{0.5}\text{Sb}_{0.5-x})_2\text{Te}_3$ [19]. For TI-graphene-FM trilayers this can be achieved, for example, by using a thin film of $\text{BaFe}_{12}\text{O}_{19}$, a magnetic insulator with high T_c and large perpendicular anisotropy [48].

By comparing the bands for TI-SLG at low energies obtained from Eq. (1) [Fig. 1(d)] with the ones obtained using DFT [29,36,37], we find that the effective value of t is ~ 45 meV. For this reason, most of the results that we show in the following were obtained assuming $t = 45$ meV. Figure 1(d) clearly shows that, in general, the hybridization of graphene's and the TI's states preserves a TI-like band and induces the formation of spin-split Rashba bands. The TI and Rashba nature of the bands can clearly be evinced from the winding of the spins, as shown in Fig. 1(f). The same qualitative features can be observed in Fig. 1(e), which shows the low-energy bands of a TI-BLG system with $\Delta = 20$ meV and $\delta\mu = 0$.

In the following, we restrict our analysis to the case in which ϵ_F is such that the system is metallic. In this case contributions to the Edelstein effect from interband transitions [49] can be neglected, and the SOT is primarily fieldlike. For most of the conditions of interest, quantum interference effects can be assumed to be negligible due to dephasing effects at finite temperatures and the large dimensionless conductance of the system. The SOT can be obtained by calculating the current-induced spin-density accumulation $\delta s^i = \chi^{s_i J_j}(\mathbf{q}, \omega) E^j$, where E^j is the electric field applied in the j direction and the spin-density response function $\chi^{s_i J_j}(\mathbf{q}, \omega)$, within the linear response regime, is equal to the spin-current correlation function. Considering that the SOT is given by $\mathbf{B}_{\text{so}} \times \mathbf{M}$, where $\mathbf{B}_{\text{so}} = \delta \mathbf{s}$ is the effective spin-orbit field due to the Edelstein effect, and that the response function depends weakly on the gap Δ induced by \mathbf{M} (as we demonstrate later), the angular dependence of the torque is mainly geometrical. Without loss of generality, we can assume the external current is in the y direction, so that $\delta \mathbf{s} \parallel \hat{x}$, and therefore, $\boldsymbol{\tau}_{\text{SO}} \approx |\mathbf{M}| \delta s^x \cos \vartheta [-\hat{y} + \hat{z} \tan \vartheta \sin \phi]$, where ϑ is the angle formed by the magnetization and the TI's surface [see Fig. (1 a)] and ϕ is the angle with respect to \hat{x} in the TI surface plane.

The unavoidable presence of disorder induces a broadening of the quasiparticle states and vertex corrections that are captured by the diagrams shown in Fig. 2. In TIs charge impurities appear to be the dominant source of disorder [50], so it is expected that they will also be in TI-graphene heterostructures. We therefore model the disorder as a random potential created by an effective 2D distribution of uncorrelated charge impurities with zero net charge placed at an effective distance d below the TI's surface. Direct imaging experiments [51] suggest $d \approx 1$ nm, consistent with transport results [50,52].

In momentum space, the bare potential $v(q)$ created on the TI's surface by a single charge impurity is $v(q) = 2\pi e^2 e^{-qd} / (\kappa q)$, where $\kappa = (\kappa_{\text{TI}} + \kappa_0) / 2$ is the average di-

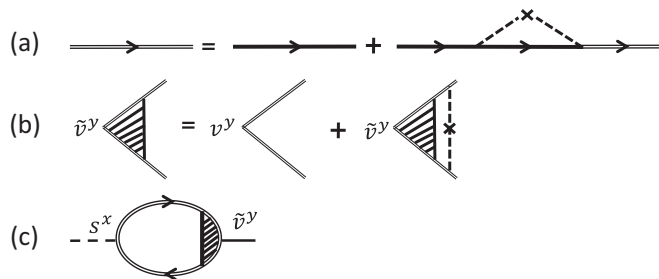


FIG. 2. Diagrams used to calculate the charge conductivity and the spin-current response.

electric constant, with $\kappa_{\text{TI}} \approx 100$ [50–54] being the dielectric constant for the TI and $\kappa_0 = 1$ being the dielectric constant of vacuum [55]. The screened disorder potential is $v(q)/\epsilon(q)$, where $\epsilon(q)$ is the dielectric function [23,56,57]. To obtain the current-driven SOT in the dc limit and for temperatures T much lower than the Fermi temperature T_F , to very good approximation we can assume $\epsilon(q) \approx 1 + v_c(q)v(\epsilon_F)$, where $v_c(q) = 2\pi e^2 / (\kappa q)$ and $v(\epsilon_F)$ is the density of states at the Fermi energy.

The lifetime $\tau_{0a}(\mathbf{k})$ of a quasiparticle in band a with momentum \mathbf{k} is given by

$$\frac{\hbar}{\tau_{0a}(\mathbf{k})} = 2\pi \sum_{a' \mathbf{q}} n_{\text{imp}} \left| \frac{v(q)}{\epsilon(q)} \right|^2 |\langle a' \mathbf{k} + \mathbf{q} | a \mathbf{k} \rangle|^2 \delta(\epsilon_{a, \mathbf{k}} - \epsilon_{a', \mathbf{k} + \mathbf{q}}), \quad (2)$$

where n_{imp} is the impurity density and $|a \mathbf{k}\rangle$ is the Bloch state with momentum \mathbf{k} and band index a . In the remainder of the paper, we set $n_{\text{imp}} = 10^{12} \text{ cm}^{-2}$ [50]. The transport time $\tau_{\text{ta}}(\mathbf{k})$, which renormalizes the expectation value of the velocity operator, is obtained by introducing the factor $[1 - \mathbf{k} \cdot (\mathbf{k} + \mathbf{q})]$ under the sum on the right-hand side of Eq. (2) and, in general, differs from the lifetime $\tau_{0a}(\mathbf{k})$ [58–62].

For a charge current in the y direction the nonequilibrium spin density is polarized in the x direction. Due to the rotational symmetry of the system we have $\chi^{s_x J_y} = -\chi^{s_y J_x}$ and $\chi^{s_x J_x} = \chi^{s_y J_y}$. Without loss of generality we can assume the current is in the y direction. Within the linear response regime, taking into account the presence of disorder, the response function $\chi^{s_x J_y}$ of the system can be obtained by calculating the diagrams shown in Fig. 2. The diagram in Fig. 2(a) represents the equation for the self-energy in the first Born approximation, where the double line represents the disorder-dressed electrons' Green's function, the single line shows the electron's Green's function for the clean system, and the dashed lines indicate scattering events off the impurities. The diagram in Fig. 2(b) corresponds to the equation for the renormalized velocity vertex \tilde{v}_y , at the ladder level approximation. In the long-wavelength, dc limit we have

$$\chi^{s_x J_y} \approx \frac{e}{2\pi \Omega} \text{Re} \sum_{\mathbf{k}, a} s_{aa}^x(\mathbf{k}) \tilde{v}_{aa}^y(\mathbf{k}) G_{\mathbf{k}a}^A G_{\mathbf{k}a}^R, \quad (3)$$

where $s_{aa}^i(\mathbf{k}) \equiv \langle a \mathbf{k} | s_i | a \mathbf{k} \rangle$ is the expectation value of the i th component of the spin-density operator, $\tilde{v}_{aa}^i(\mathbf{k}) = (\tau_{\text{ta}} / \tau_{0a})_{\mathbf{k}} v_{aa}^i(\mathbf{k})$, with $v_{aa}^i(\mathbf{k}) \equiv \langle a \mathbf{k} | v_i | a \mathbf{k} \rangle$ being the expectation value of the i th component of the velocity operator

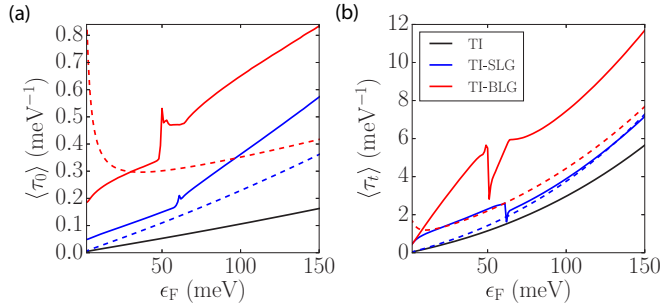


FIG. 3. (a) $\langle\tau_0(\epsilon_F)\rangle$ and (b) $\langle\tau_t(\epsilon_F)\rangle$ for $\Delta = 0$ meV, $\delta\mu = 0$ meV, and $n_{\text{imp}} = 10^{12}$ cm $^{-2}$. The solid lines correspond to $t = 45$ meV, while dashed lines correspond to the limit $t = 0$ meV.

$\mathbf{v} = \hbar^{-1} \partial H_{\mathbf{k}} / \partial \mathbf{k}$, and $G_{\mathbf{k}a}^{R/A} = [\epsilon_F - \epsilon_{\mathbf{k}a} \pm i\hbar/2\tau_{0a}(\mathbf{k})]^{-1}$ are the retarded and advanced Green's functions, respectively, for electrons with momentum \mathbf{k} and band index a .

III. RESULTS

In this section, we present our results for the transport properties and current-induced spin-density accumulation of TI-graphene heterostructures.

We define the average τ_0 and τ_t as $\langle\tau_{0(t)}(\epsilon_F)\rangle \equiv \sum_{\mathbf{k}a} \tau_{0a(ta)}(\mathbf{k}) \delta(\epsilon_F - \epsilon_{\mathbf{k}a}) / \sum_{\mathbf{k}a} \delta(\epsilon_F - \epsilon_{\mathbf{k}a})$. Figures 3(a) and 3(b) show $\langle\tau_0(\epsilon_F)\rangle$ and $\langle\tau_t(\epsilon_F)\rangle$, respectively, for a TI's surface, a TI-SLG heterostructure, and a TI-BLG heterostructure, with $\Delta = 0$ meV. We see that the presence of a graphene layer strongly increases both $\langle\tau_0(\epsilon_F)\rangle$ and $\langle\tau_t(\epsilon_F)\rangle$ and that such an increase is dramatic for the case when the layer is BLG. $\langle\tau_0(\epsilon_F)\rangle$ and $\langle\tau_t(\epsilon_F)\rangle$ are larger in BLG-TI than TI-SLG because, especially at low energies, BLG has a larger density of states than SLG, causing $\varepsilon(q)$, which enters in the denominator in Eq. (2), and therefore $\langle\tau_0(\epsilon_F)\rangle$ and $\langle\tau_t(\epsilon_F)\rangle$ to be larger in BLG than in SLG. Notice that τ_0 and τ_t increase after adding a graphene layer even in the limit when $t = 0$, as shown by the dashed lines in Fig. 3. This is due to the fact that the graphene layer screens the dominant source of disorder in the TI even when $t = 0$. Changes in Δ have only minor quantitative effects as long as $\Delta < (t, \epsilon_F)$.

Figure 4(a) shows the dependence of $\chi^{s_x J_y}$ on ϵ_F for TI, TI-SLG, and TI-BLG for $t = 45$ meV, $\delta\mu = 0$, and $\Delta = 20$ meV with out-of-plane magnetization $\hat{m} = \hat{z}$ (solid lines). The dashed lines corresponds to the case $\Delta = 0$. The inset shows a sketch of the system, with charge flowing in the y direction. The direction of the spin accumulation on the top and bottom layers is indicated by the arrows on the electrons. The insertion of a graphene layer strongly enhances the current-induced spin-density response and therefore the SOT. Now, we consider in-plane magnetization. In this case, the Fermi surface is not isotropic like for out-of-plane magnetization, which makes the computation of scattering time, transport time, and the Edelstein effect more challenging. For concreteness, we assume the magnetization direction to be $\hat{m} = \hat{x}$ (\parallel). Figure 4(b) shows $\chi^{s_x J_y}$ as a function of ϵ_F for in-plane $\hat{m} = \hat{x}$ (\parallel) magnetization and $\Delta = 20$ meV (dashed lines). The red lines correspond to a TI-BLG-FM, and the black lines correspond to a TI-FM heterostructure. We obtained an

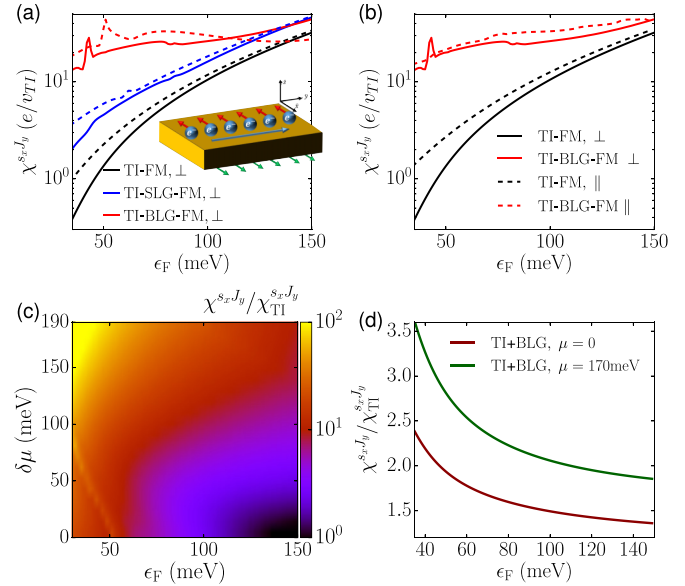


FIG. 4. (a) $\chi^{s_x J_y}$ as a function of ϵ_F for $\delta\mu = 0$, $t = 45$ meV, and $\Delta = 20$ meV ($\Delta = 0$) with out-of-plane magnetization $\hat{m} = \hat{z}$ (\perp), shown by solid (dashed) lines. Inset: sketch showing the spin-density accumulation on the top and bottom surfaces of a TI induced by a current in the y direction. (b) $\chi^{s_x J_y}$ as a function of ϵ_F for in-plane $\hat{m} = \hat{x}$ (\parallel) [out-of-plane $\hat{m} = \hat{z}$ (\perp)] magnetization and $\Delta = 20$ meV, shown by dashed (solid) lines. The other parameters are the same as in (a). (c) Enhancement of $\chi^{s_x J_y}$ in a TI-BLG system compared to TI alone as a function of ϵ_F and $\delta\mu$ for $\Delta = 0$. (d) $\chi^{s_x J_y}$ for TI-BLG when $t = 0$. In all the panels, the disorder parameters are $n_{\text{imp}} = 10^{12}$ cm $^{-2}$ and $d = 1$ nm.

enhancement as large as the one obtained for out-of-plane magnetization $\hat{m} = \hat{z}$ (\perp ; solid lines).

We find that changes in $\delta\mu$ have a strong impact on $\chi^{s_x J_y}$. Figure 4(c) shows that by increasing $\delta\mu$ the enhancement of the SOT can be raised to values as high as 100 in TI-BLG heterostructures due to the flattening and consequent increase of the DOS of the TI-like bands (see Appendix A). The results of Fig. 4 show that in TI-SLG and TI-BLG heterostructures the current-induced SOT can be expected to be much higher than in TI surfaces alone. They show that for TI-BLG systems there is a large range of values of $\delta\mu$ and ϵ_F for which the enhancement of $\chi^{s_x J_y}$ due to the presence of the BLG is consistently close to 10 or larger [Fig. 4(c)].

We also find that the strong enhancement of $\chi^{s_x J_y}$ is not affected significantly by the value of Δ , as shown in Fig. 5, where we plot $\chi^{s_x J_y}$ as a function of Δ at $\epsilon_F = 60$ meV. In Fig. 5(a) we plot $\chi^{s_x J_y}$ for TI-FM, while Fig. 5(b) shows the response function $\chi^{s_x J_y}$ for TI-SLG-FM and TI-SLG-FM normalized to the response in a TI-FM system.

In addition, in a TI-graphene heterostructure, by placing the source and drain on the graphene (BLG) and taking into account the high mobility of graphene (BLG), it is possible to force most of the current to flow within graphene (BLG) and the TI's surface adjacent to it. Therefore, we can minimize the amount of spin-density accumulation with opposite polarization that a current flowing in the TI's bottom surface generates. This fact should further increase the net SOT.

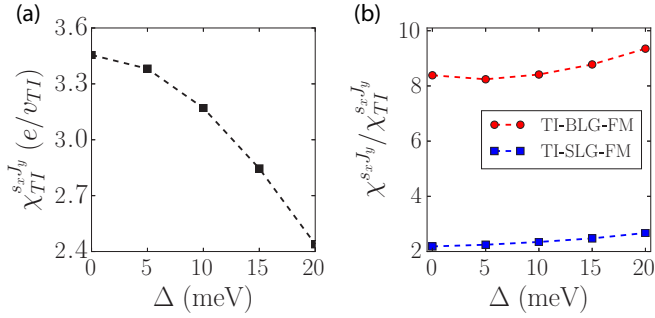


FIG. 5. (a) $\chi^{s_x J_y}$ as a function of the exchange interaction Δ for a TI-FM heterostructure at $\epsilon_F = 60$ meV. (b) Ratio $\chi^{s_x J_y} / \chi_{TI}^{s_x J_y}$ of the TI-BLG-FM (red circles) and TI-SLG-FM (blue squares) responses to the TI-FM response. The magnetization direction is out of plane, $\hat{m} = \hat{z} (\perp)$.

The large enhancement of the spin-density accumulation in TI-graphene systems is due to two main reasons: (i) the survival, after hybridization, of TI-like bands well separated from Rashba bands and (ii) the strong enhancement of the relaxation time τ_0 and transport time τ_t due to the additional screening by the graphene layer of the dominant source of disorder. It is important to notice that the presence of the Rashba bands (see Fig. 1) not only is not essential for the enhancement of the spin-density accumulation but can be detrimental given that the Rashba bands give $\chi^{s_x J_y}$ with a sign opposite that of the TI-like bands. This fact can be seen at large Fermi energies for BLG-TI in Fig. 4(a): for $\epsilon_F \gtrsim 140$ meV the Fermi surface intersects the Rashba bands, which by giving a contribution to $\chi^{s_x J_y}$ opposite to that of the TI-like bands makes the net SOT of TI-BLG slightly lower than the SOT of TI alone. Point (ii) explains the fact $\chi^{s_x J_y}$, at low energies, is always larger in TI-BLG than in TI-SLG given that τ_0 and τ_t are larger in TI-BLG than in TI-SLG. In addition, it explains the fact that even in the limit where there is no hybridization between the TI and the graphene bands, i.e., $t = 0$ due, for example, to a large twist angle (see Appendix B), the spin-current correlation function in TI-graphene systems is still larger than in TIs alone for the experimentally relevant case where charge impurities are the dominant source of disorder, as shown in Fig. 4(d).

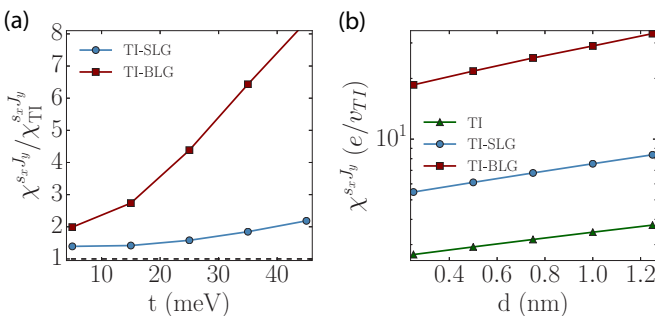


FIG. 6. (a) $\chi^{s_x J_y} / \chi_{TI}^{s_x J_y}$ as a function of the tunneling amplitude t for TI-SLG and TI-BLG heterostructures at $\epsilon_F = 60$ meV and $\delta\mu = 0$. (b) $\chi^{s_x J_y} / \chi_{TI}^{s_x J_y}$ as a function of the effective distance to the impurities d for TI-SLG and TI-BLG heterostructures at $\epsilon_F = 60$ meV and $\delta\mu = 0$.

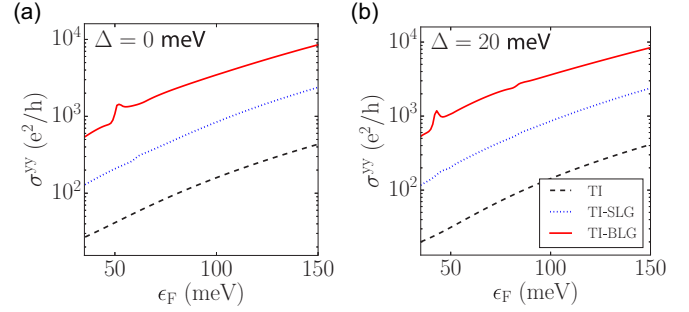


FIG. 7. $\sigma^{yy}(\epsilon_F)$ for TI (dashed line), TI-SLG (dotted line), and TI-BLG (solid line) for (a) $\Delta = 0$ and (b) $\Delta = 20$ meV with out-of-plane magnetization, $\hat{m} = \hat{z} (\perp)$. $t = 45$ meV, $\delta\mu = 0$, and $n_{\text{imp}} = 10^{12} \text{ cm}^{-2}$.

In Fig. 6(a), we show the current-induced spin-density accumulation response function dependence on the tunneling amplitude t , normalized to the TI response. As t is increased, TI and graphene hybridize more strongly, leading to a larger SOT. However, even at vanishing tunneling, an enhancement is still present.

In Fig. 6(b), we plot $\chi^{s_x J_y}$ as a function of the effective distance from the TI surface to the effective layer of impurities d . The farther away the impurities are located, the weaker the disorder is, and therefore, the larger the expected SOT is.

To estimate the efficiency of the current-induced SOT in TI-graphene heterostructures, we calculate the associated dc longitudinal conductivity σ^{ii} for the same parameters. In the linear-response, long-wavelength regime we have

$$\sigma^{ii} \approx \frac{e^2}{2\pi\Omega} \text{Re} \sum_{\mathbf{k}, a} v_{aa}^i(\mathbf{k}) \bar{v}_{aa}^i(\mathbf{k}) G_{\mathbf{k}a}^A G_{\mathbf{k}a}^R. \quad (4)$$

Figure 7(a) shows σ^{yy} for TI, TI-SLG, and TI-BLG as a function of ϵ_F in the limit $\Delta = 0$. We see that the presence of a graphene layer enhances the conductivity of the system by an order of magnitude or more. Figure 7(b) shows that the exchange term H_{ex} does not affect σ^{yy} significantly. The results shown in Fig. 7(b) imply that in TI-graphene heterostructures not only can the current-induced SOT be much larger than in TIs alone but also the generation of the SOT is much less dissipative. For example, for an applied electric field of the order of $0.1 \text{ V}/\mu\text{m}$, we can reach a conservative spin-density accumulation $\delta s^x \approx 5 \times 10^7 \hbar \text{ cm}^{-2}$. For a typical carrier density in graphene ($n \approx 10^{11} \text{ cm}^{-2}$), we have $\delta s^x / n = 5 \times 10^{-4} \hbar$.

IV. CONCLUSIONS

In conclusion, we have shown that in magnetic TI-graphene heterostructures the nonequilibrium uniform spin-density accumulation induced by a charge current can be 10–100 times higher than in TIs alone, giving rise to a giant Edelstein effect. The reasons for these enhancements are (i) the additional screening by the graphene layer of the dominant source of disorder, (ii) the fact that graphene and the TI's surface are almost commensurate, making a strong hybridization of the TI's and graphene's states possible, (iii) the fact that the spin structure of the hybridized bands has a spin structure very similar to the one of the original TI's band for a large range

of dopings, and (iv) the fact that graphene is the ultimate 2D system, only one atom thick. These facts and our results suggest the TI-graphene systems are very good candidates to realize all-electric efficient magnetization switching.

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APPENDIX A: TI-BLG BAND STRUCTURE

As long as the interlayer tunneling t_{BLG} between the carbon atoms in bilayer graphene is much larger than the expected tunneling t between the TI's surface and the graphenic layer, any difference between the tunneling strength between the carbon layers forming BLG and the TI will give very negligible effects. Considering that in bilayer graphene the interlayer tunneling is 350 meV and the fact that for the TI-graphene tunneling t we consider only values smaller than 45 meV, for all our results $t \ll t_{BLG}$. In this limit, at low energies ($\lesssim 350$ meV), BLG can be treated as a 2D system with the effective Hamiltonian H^{BLG} presented in the main text.

Figure 1(e) in the main text shows the bands of a TI-BLG system for which the exchange field $\Delta = 20$ meV and $\delta\mu = 0$. Figure 3 shows that the strongest enhancement of the SOT happens for TI-BLG systems when $\delta\mu \neq 0$. It is therefore interesting to see how the low-energy bands of TI-BLG are affected by a nonzero value of $\delta\mu$. Figure 8 shows the band structure of TI-BLG for the case when $\delta\mu = 125$ meV in

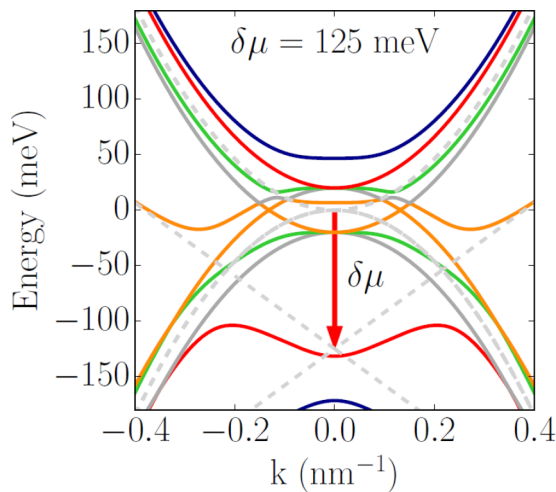


FIG. 8. TI-BLG band structure for $\delta\mu = 125$ meV and tunneling amplitude $t = 45$ meV.

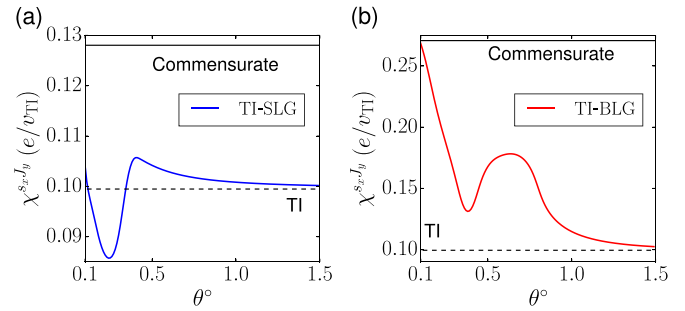


FIG. 9. (a) $\chi^{s_x J_y}$ as a function of twist angle θ for TI-SLG. (b) Same as (a) for TI-BLG.

the absence of any exchange field. We see that one of the TI-like bands (shown in orange) becomes much flatter: the high density of states of this band explains the high values of SOT for TI-graphene systems when $\delta\mu \neq 0$.

APPENDIX B: INVERSE SPIN-GALVANIC EFFECT IN TWISTED TI-GRAPHENE HETEROSTRUCTURES

It can be expected that even when the stacking of the graphenic layer and the TI's surface is incommensurate, the screening of the charge impurities by the graphenic layer will lead to a strong enhancement of τ_0 and τ_t and therefore of the SOT. The accurate treatment of the realistic case in which the main source of disorder is charge impurities for incommensurate stackings requires the calculation of the dielectric constant for incommensurate structures, a task that is beyond the scope of the present work. For this reason, to exemplify how the presence of a small twist angle θ between the graphenic layer and the TI surface, giving rise to an incommensurate stacking, affects the calculation of the SOT, we consider a very simple model for the effect of the disorder: we simply assume that the disorder gives rise to a constant quasiparticle broadening.

Let $|\mathbf{q}| \equiv q = 2K_D \sin(\theta/2)$, where K_D is the magnitude of the graphene K point. The dimensionless parameter $\gamma \equiv \frac{t'}{\hbar v_{TI} q}$, where $t' = t/3$, measures the strength of the coupling between the graphenic layer and the TI. For $\gamma < 1$ we can obtain the electronic structure using the weak-coupling theory for twisted systems [63–65] that, for the case of TI-graphene heterostructures, we presented in Ref. [31]. After obtaining the electronic structure in the regime $\gamma < 1$, we can obtain $\chi^{s_x J_y}$. To understand how the responses between the commensurate and the incommensurate regimes differ, we have calculated $\chi^{s_x J_y}$ assuming a constant quasiparticle broadening $1/(2\tau_0) = 2$ meV, with $t' = 15$ meV, $\delta\mu = 0$, and $\epsilon_F = 10$ meV for a range of values of θ for which the weak-coupling theory is valid. The dependence of $\chi^{s_x J_y}$, per valley, as a function of θ for TI-SLG and TI-BLG is shown in Fig. 9. As is to be expected, the results show that in the incommensurate case the response is smaller than in the commensurate case. However, they also show, particularly for the case in which the graphenic layer is BLG, that a TI-graphene heterostructure is expected to have stronger $\chi^{s_x J_y}$ and therefore a stronger inverse spin-galvanic effect, even in the incommensurate regime and for the case in which the disorder is modeled very simply.

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